

Evalúe cada uno de los siguientes límites si estos existen

$$\lim_{x \rightarrow -2} \frac{x+2}{x^2+8}$$

$$= \lim_{x \rightarrow -2} \frac{\cancel{x+2}}{(x+2)(x^2-2x+4)}$$

$$= \lim_{x \rightarrow -2} \frac{1}{x^2-2x+4}$$

$$= \frac{1}{(-2)^2 - 2(-2) + 4} = \frac{1}{12}$$

$$\lim_{t \rightarrow 0} \frac{\sqrt{1+t} - \sqrt{1-t}}{t}$$

$$= \lim_{t \rightarrow 0} \frac{0}{0} = 0$$

El límite no existe

$$\lim_{h \rightarrow 0} \frac{\sqrt{9+h} - 3}{h} \cdot \frac{\sqrt{9+h} + 3}{\sqrt{9+h} + 3}$$

$$= \lim_{h \rightarrow 0} \frac{1}{\sqrt{9+h} + 3}$$

$$= \frac{1}{\sqrt{0+9} + 3} = \frac{1}{6}$$

$$\lim_{h \rightarrow 0} \frac{(x+h)^3 - x^3}{h}$$

$$= \lim_{h \rightarrow 0} \frac{x^3 + 3hx^2 + 3h^2x + h^3 - x^3}{h}$$

$$= \lim_{h \rightarrow 0} \frac{h(3x^2 + 3hx + h^2)}{h}$$

$$= \lim_{h \rightarrow 0} 3x^2 + 3hx + h^2$$

$$= 3x^2 + 3(0)x + 0^2 = 3x^2$$

$$\lim_{x \rightarrow -4}$$

$$\frac{\frac{1}{4} + \frac{1}{x}}{4 + x}$$

$$\frac{x+4}{4x} \cdot \frac{x+4}{4+x}$$

$$= \lim_{x \rightarrow -4}$$

$$\frac{1}{4x}$$

$$= \frac{1}{4(-4)} = -\frac{1}{16}$$