Fórmulas de Integración

$$1. \int dx = x + c$$

$$2. \int k dx = kx + c$$

3.
$$\int x^n dx = \frac{x^{n+1}}{n+1} + c$$

$$4. \int kf dx = k \int f dx$$

5.
$$\int f^{n} f' dx = \frac{f^{n+1}}{n+1} + c$$

$$6. \int u dv = uv - \int v du$$

"una vaca sin cola vestida de uniforme"

$$7. \int \sin x dx = -\cos x + c$$

$$8. \int \cos x dx = \sin x + c$$

$$9. \int \tan x dx = \ln |\sec x| + c$$

$$10. \int \cot x dx = \ln |\sin x| + c$$

11.
$$\int \sec x dx = \ln \left| \sec x + \tan x \right| + c$$

12.
$$\int \csc x dx = \ln \left| \csc x - \cot x \right| + c$$

$$13. \int \sec^2 x dx = \tan x + c$$

$$14. \int \csc^2 x dx = -\cot x + c$$

15.
$$\int \sec^3 x dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln|\sec x + \tan x| + c$$
 30.
$$\int a^{kx} dx = \frac{a^{kx}}{k \ln a} + c$$

$$\int \sec^3 x dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln |\sec x + \tan x| + c$$

17.
$$\int \frac{dx}{\sqrt{1-x^2}} = \arcsin x + c$$

$$18. \int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + c$$

19.
$$\int \frac{f'dx}{\sqrt{a^2 - f^2}} = \arcsin \frac{f}{a} + c$$

$$20. \int \frac{dx}{1+x^2} = \arctan x + c$$

21.
$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \arctan \frac{x}{a} + c$$
 35.
$$\int \cosh x dx = \sinh x + c$$

22.
$$\int \frac{f' dx}{a^2 + f^2} = \frac{1}{a} \arctan \frac{f}{a} + c$$
 Sustitución universal

23.
$$\int \frac{dx}{x\sqrt{x^2 - 1}} = arc \sec x + c$$
37.
$$\sin x = \frac{2u}{1 + u^2}$$

24.
$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \arcsin \sec \frac{x}{a} + c$$
38.
$$\cos x = \frac{1 - u^2}{1 + u^2}$$

25.
$$\int \frac{f' dx}{f \sqrt{f^2 - a^2}} = \frac{1}{a} arc \sec \frac{f}{a} + c$$
39.
$$\tan x = \frac{2u}{1 - u^2}$$

$$26. \int e^x dx = e^x + c$$

$$27. \int e^{kx} dx = \frac{e^{kx}}{k} + c$$

$$28. \int e^f f' dx = e^f + c$$

$$29. \int a^x dx = \frac{a^x}{\ln a} + c$$

$$30. \int a^{kx} dx = \frac{a^{kx}}{k \ln a} + c$$

16.
$$\int \csc^3 x dx = -\frac{1}{2} \csc x \cot x + \frac{1}{2} \ln|\csc x - \cot x| + c \quad 31. \quad \int a^f f' dx = \frac{a^f}{\ln a} + c$$

18.
$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + c \qquad 32.$$
$$\int \frac{dx}{x} = \int \frac{1}{x} dx = \int x^{-1} dx = \ln|x| + c$$

$$33. \int \frac{f'}{f} dx = \ln |f| + c$$

$$34. \int \sinh x dx = \cosh x + c$$

$$35. \int \cosh x dx = \sinh x + c$$

36.
$$u = \tan(x/2)$$

$$37. \sin x = \frac{2u}{1 + u^2}$$

38.
$$\cos x = \frac{1 - u^2}{1 + u^2}$$

39.
$$\tan x = \frac{2u}{1 - u^2}$$

$$40. \ dx = \frac{2}{1 + u^2} du$$