

## Appendix A

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**Algorithm 1:** Auxiliary function for vertex selection of the instance generator

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```
1 function chooseVW( $V, L, E$ )
2   Let sortedVertices be a queue of vertices sorted by their colored degree
3   Let candidates be the first  $0.2 * N$  vertices of sortedVertices
4   for  $i \leftarrow 1$  to 101 do
5     Let  $v, w$  be two random distinct vertices from candidates
6     if  $(v, w, l') \notin E \mid \forall l' \in L$  then return  $(v, w)$ 
7     if  $i = 100$  then
8        $i \leftarrow 1$ 
9       candidates  $\leftarrow$  candidates  $\cup$  { next vertex of sortedVertices, if any }
```

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**Algorithm 2:** Auxiliary function for label selection of the instance generator

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```
1 function chooseLabel( $v, w, Klimit, V, L, E$ )
2   Let sortedLabels be a queue of labels sorted by the amount of edges associated with each of them
3   Let candidates be the first  $Klimit$  labels of sortedLabels
4   for  $i \leftarrow 1$  to 1000 do
5     Let  $l$  be a random label from candidates
6     if  $(v, w', l) \notin E \mid \forall w' \in L$  and  $(v', w, l) \notin E \mid \forall v' \in L$  then return  $l$ 
7     candidates  $\leftarrow$  candidates  $\cup$  { next label of sortedLabels, if any }
8   return a random label from  $L$ 
```

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**Algorithm 3:** G4 Instances Generator

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```
1 procedure G4Generator( $V, L, d, initialSizeOfSolution$ )
2   Let  $E \leftarrow \emptyset$  be the set of edges of the graph
3   Let  $LabelsOfSolution \leftarrow \emptyset$  be the set of labels of the non-trivial solution
4   Let  $leftPartitionSize$  be a random integer between 4 and  $|V|/4$ 
5   Let  $leftPartition$  be a set of size  $leftPartitionSize$  of randomly chosen vertices
6   for  $i \leftarrow 1$  to  $(d * |V| * (|V| - 1)/2)$  do
7     Let  $v, w \leftarrow chooseVW(V, L, E)$ 
8     if  $v \in leftPartition$  XOR  $w \in leftPartition$  then
9       if  $|LabelsOfSolution| = initialSizeOfSolution$  then
10         Let  $l$  be a random label from  $LabelsOfSolution$ 
11       else
12         Let  $l \leftarrow chooseLabel(v, w, |L|, V, L, E)$ 
13          $LabelsOfSolution \leftarrow LabelsOfSolution \cup \{l\}$ 
14     else Let  $l \leftarrow chooseLabel(v, w, 0.2 * |L|, V, L, E)$ 
15      $E \leftarrow E \cup \{(v, w, l)\}$ 
16   Let  $minTrivial \leftarrow \min(\text{Labeled degree of } v \mid \forall v \in V) - sizeOfSolution$ 
17   if  $minTrivial > 1$  then
18     for  $i \leftarrow 1$  to  $(\text{random integer between } minTrivial/2 \text{ and } minTrivial - 1)$  do
19       Let  $l_{out}$  be a random label such that  $l_{out} \in LabelsOfSolution$ 
20       Let  $l_{in}$  be a random label such that  $l_{in} \in L \setminus LabelsOfSolution$ 
21       Let  $P \leftarrow \{e = (v, w, l_{out}) \mid \forall v, w \in V, \text{ such that } v \in leftPartition \text{ XOR } w \in leftPartition\}$ 
22       for  $i \leftarrow 1$  to  $\text{random integer between } 1 \text{ and } 2$  do
23         if  $|P| > 1$  then
24           Let  $e' = (v', w', l_{out})$  be a random edge from  $P$ 
25            $P \leftarrow P \setminus \{e'\}$ 
26            $E \leftarrow E \cup \{(v', w', l_{in})\} \setminus \{e'\}$ 
27            $LabelsOfSolution \leftarrow LabelsOfSolution \cup \{l_{in}\}$ 
28   return  $E$ 
```

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