

# SimBALink

## 1 Vehicle

This system models the forces acting on the vehicle.

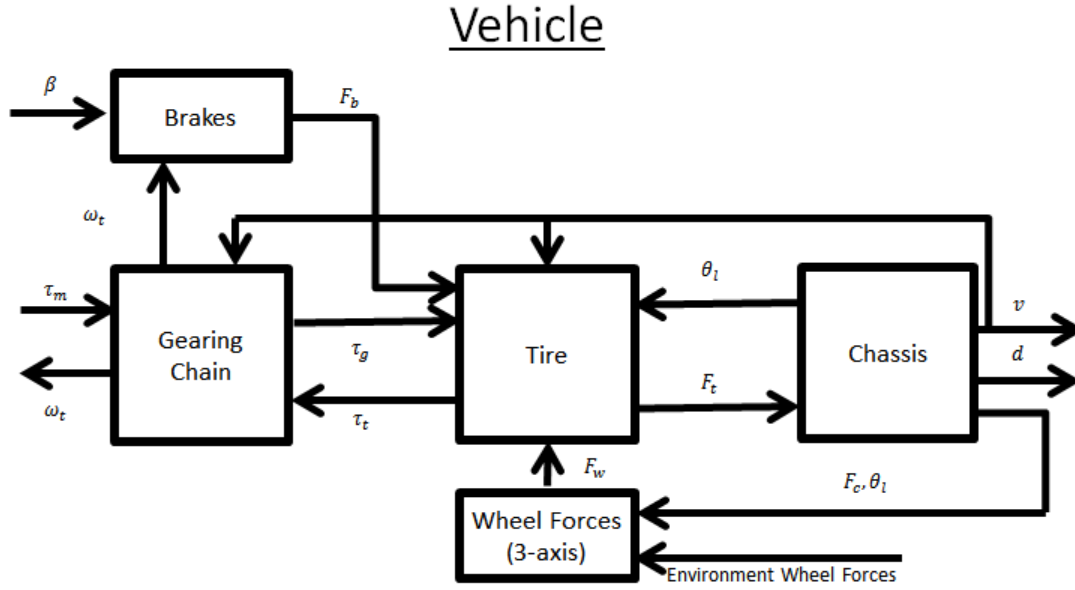


Figure 1: Vehicle Diagram

### 1.1 Gearing and Chain

This system models the gear and chain in such a way to allow for wheel slip.

### 1.2 Inputs and outputs

#### 1.2.1 Inputs

Input	Symbol	Unit
Motor Torque	$\tau_m$	Nm
Tire Torque	$\tau_t$	Nm

#### 1.2.2 Outputs

Output	Symbol	Unit
Tire Velocity	$\omega_t$	rad/s
Gear Torque	$\tau_g$	Nm

### 1.2.3 Background, rationale, modeling strategy

The tire, chain, gear, and motor are modeled as a lumped inertia that is accelerated by the motor torque and tire torque(modeled as a load). The chain is modeled lossey through an efficiency map. Gearing is modeled as a ratio that linearly changes motor torque to gear torque. This method of modeling allows for wheel slip down the line.

$$\dot{\omega}_t = \frac{\tau_m - \tau_t}{J_m + J_g + J_t + J_c} \quad (1)$$

$$\tau_g = \frac{\tau_m \eta_c(\omega_t)}{R_g} \quad (2)$$

### 1.2.4 States

State	Symbol	Unit
Tire Velocity	$\omega_t$	rad/s

### 1.2.5 Parameters

Parameters	Symbol	Unit
Motor inertia	$J_m$	$kg * m^2$
Gear inertia	$J_g$	$kg * m^2$
Chain inertia	$J_c$	$kg * m^2$
Tire inertia	$J_t$	$kg * m^2$
Gear Ratio	$R_g$	$\frac{\tau_m}{\tau_g}$

### 1.2.6 Functions

$\eta_c(\omega_t)$			
Type	Description	Symbol	Unit
Input	Wheel Speed	$\omega_t$	rad/s
Output	Chain Efficiency	n/a	%

The function is modeled as a look up table following the curve below described in the paper "Optimization of Chain Drives in Sports Motorcycles".

### 1.2.7 Assumptions

- The chain and gearing is rigid (no chain/gear dynamics)
- Chain efficiency is only a function of wheel speed

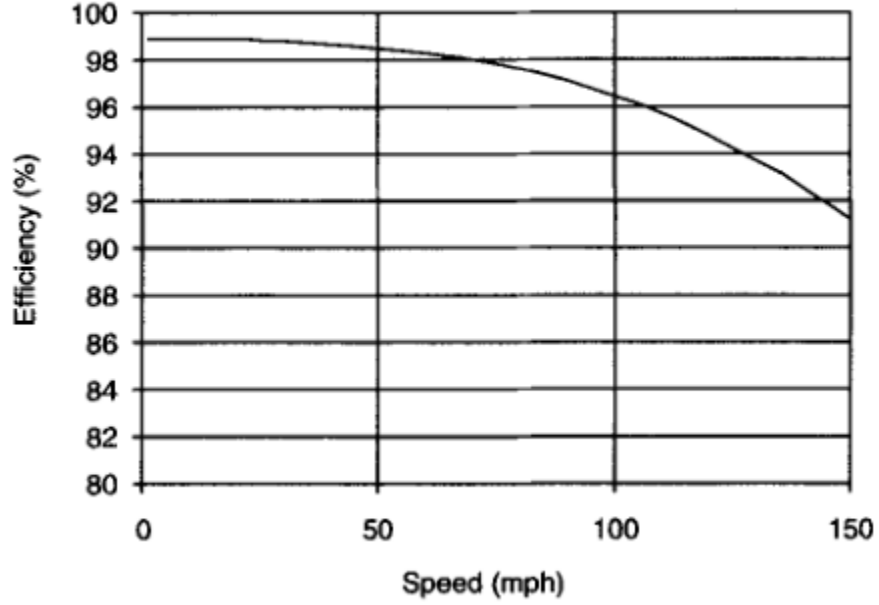


Figure 2: Estimated Chain Efficiency

### 1.3 Brakes

### 1.4 Inputs and outputs

#### 1.4.1 Inputs

Input	Symbol	Unit
Brake Command	$\beta$	%
Wheel Speed	$\omega_t$	rad/s

#### 1.4.2 Outputs

Output	Symbol	Unit
Brake Force on Tire	$F_b$	N

#### 1.4.3 Background, rationale, modeling strategy

The brake is modeled as a friction force and a constant that converts  $\beta$  to a force.

$$F_b = \mu_b \omega_t \beta k_b \quad (3)$$

#### 1.4.4 Variables

Var	Symbol	Unit
Brake Coefficient of Friction	$\mu_b$	$\frac{N}{rad/s}$
Force Constant	$k_b$	$\frac{N}{\%}$

#### 1.4.5 Assumptions

- Brake percentage to friction force is linear
- The tire never locks

### 1.5 Tires

#### 1.6 Inputs and outputs

##### 1.6.1 Inputs

Input	Symbol	Unit
Brake Force	$F_b$	N
Gear Torque	$\tau_g$	Nm
Wheel Forces[3]	$F_w$	N[3]
Vehicle Velocity	$v$	m/s
Lead Angle	$\theta_l$	rad

##### 1.6.2 Outputs

Output	Symbol	Unit
Tire Torque	$\tau_t$	Nm
Tire Reaction Force	$F_t$	N

##### 1.6.3 Background, rationale, modeling strategy

The tire is modeled in three parts, rolling resistance, Load and Torque, and Traction Limiting. Force directions are defined as longitudinal(long), lateral(lat), and normal(n). Longitudinal is along the direction of the motorcycle (when moving straight). Lateral is orthogonal to Longitudinal axis. Normal 3-D orthogonal to lateral and longitudinal, in general the axis to the road on no incline.

In general the tire model provides a load on the Gear/Chain and gives the vehicle a reaction force. Load is caused by the forces from the road(from the vehicle) and rolling resistance. the reaction force caused by traction limiting which is a function of wheel slip. The amount of reaction force is saturated at the maximum force the tire can apply given wheel slip.

### Rolling Resistance

$$K_t = \begin{cases} 0.0085 + \frac{0.18}{p_t} + \frac{1.59 \cdot 10^{-6}}{p_t} & : v_{kph} \leq 165(km/h) \\ \frac{0.18}{p_t} + \frac{2.91 \cdot 10^{-6}}{p_t} & : v_{kph} > 165(km/h) \end{cases} \quad (4)$$

### Wheel Slip

$$\kappa = -\frac{v - \omega_t r_t(\theta_l)}{v} \quad (5)$$

$$\mu_{t,gnd} = D_\kappa \sin(C_\kappa \arctan[B_\kappa \kappa - E_\kappa(B_\kappa \kappa - \arctan B_\kappa \kappa)]) \quad (6)$$

### Load and Torque

$$\tau_t = \tau_g - F_{w,long} r_t(\theta_l) - F_b r_b - K_t F_{w,n} v_{kph}^2 \quad (7)$$

### Traction Limiting

$$F_{max} = \mu_{t,gnd} F_{w,n} \quad (8)$$

$$F = \tau_t r_t(\theta_l) \quad (9)$$

$$F_t = \begin{cases} F & : F \leq F_{max} \\ -F & : -F_{max} \leq F \\ F_{max} & : F > F_{max} \\ -F_{max} & : -F_{max} > F \end{cases} \quad (10)$$

The tire coefficient ( $\mu_{t,gnd}$ ) is modeled using the "Magic Formula" as shown below. Where  $D_\kappa$  is the maximum tire coefficient of the tire.

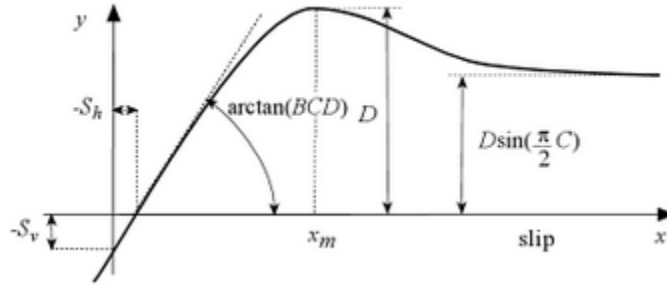


Figure 3: Magic Formula

#### 1.6.4 Variables

Var	Symbol	Unit
Tire Torque	$\tau_t$	Nm
Rolling Constant	$K_t$	n/a
Wheel Slip	$\kappa$	ratio
Tire coefficient	$\mu_{t,gnd}$	n/a
Max Force	$F_{max}$	N
Force	$F$	N

#### 1.6.5 Parameters

Param.	Symbol	Unit
Tire Pressure	$p_t$	<i>bar</i>
Brake Caliper Radius	$r_b$	m
<b>Magic Formula</b>	$A_\kappa, B_\kappa, C_\kappa, D_\kappa$	n/a

#### 1.6.6 Function

$r_t(\theta_l)$			
Type	Description	Symbol	Unit
Input	Lean Angle	$\theta_l$	rad
Output	Tire Radius	n/a	m

#### 1.6.7 Assumptions

- Maximum acceleration force should also depend on lateral forces on the vehicle. However this is not modeled because it requires modeling of high-side and low-side dynamics. The Rider model should control for a safe operating area of the motorcycle to compensate for this assumption.
- No tire deformation
- No tire temperature dynamics
- No change in rolling resistance with lean angle

### 1.7 Wheel Forces

Wheel Forces does nothing. It would allow for the environment to affect tire forces.

$$F_{\omega, long} = F_{c, long} \quad (11)$$

$$F_{\omega, n} = F_{c, n} \quad (12)$$

## 1.8 Chassis

This system models the chassis of the motorcycle including the velocity of the motorcycle and forces on the road.

The forces have a notation of Longitudinal (long), Normal(n) , and Lateral (lat). Longitudinal being the direction the motorcycle is moving. Lateral at a 2D right angle to Longitudinal direction. Normal is orthogonal to others.

## 1.9 Inputs and outputs

### 1.9.1 Inputs

Input	Symbol	Unit
Tire Force	$F_t$	N
Air Density	$\rho$	$kg/m^3$
Road Gradient	$\theta_r$	rad

### 1.9.2 Outputs

Output	Symbol	Unit
Vehicle Velocity	$v$	m/s
Distance Traveled	$d$	m
Lean Angle	$\theta_l$	rad
Chassis Forces	$F_c$	N[3]

### 1.9.3 Background, rationale, modeling strategy

The Chassis is modeled point mass with drag.

$$F_a = \frac{1}{2} \rho C_d A v^2 \quad (13)$$

$$F_{c,long} = F_a + gm \sin(\theta_r) \quad (14)$$

$$F_{c,n} = mg \cos(\theta_r) \quad (15)$$

$$\dot{v} = m F_t \quad (16)$$

$$\dot{d} = v \quad (17)$$

$$\theta_l = \theta_l(d) \quad (18)$$

### 1.9.4 States

State	Symbol	Unit
Distance	$d$	m
Velocity	$v$	m/s

### 1.9.5 Variables

Output	Symbol	Unit
Drag Force	$F_a$	N

### 1.9.6 Parameters

Param.	Symbol	Unit
Drag Area	$C_d A$	$\frac{N}{rad/s}$
Gravity	$g$	$m/s^2$
Mass of Motorcycle	$m$	$kg$

### 1.9.7 Look Up table

$\theta_l(d)$

Type	Description	Symbol	Unit
Input	Distance Traveled	$d$	m
Output	Lean Angle	n/a	rad

### 1.9.8 Assumptions

- The full weight of the motorcycle is always on the correct tire for braking or acceleration. That is not a bad assumption because maximum braking or acceleration will happen at wheelie or stoppie when there is only one tire on the ground.
- Lean angle does not affect Aero Drag
- No lateral forces

## 2 Environment

This system models the environment of the motorcycle is riding in.

Force directions are defined as longitudinal(long), lateral(lat), and normal(n). Longitudinal is along the direction of the motorcycle (when moving straight). Lateral is orthogonal to Longitudinal axis. Normal 3-D orthogonal to lateral and longitudinal, in general the axis to the road on no incline.

### 2.1 Inputs and outputs

#### 2.1.1 Inputs

Input	Symbol	Unit
Distance Travel	$d$	m



### 2.1.2 Outputs

Output	Symbol	Unit
Environment Forces on Tire[3]	$F_t$	N[3]
Road Gradient	$\theta_r$	rad
Ambient Temperature	$T_{amb}$	K
Air Pressure	$P$	Pa
Air Density	$\rho$	$kg/m^3$

### 2.1.3 Background, rationale, modeling strategy

The Environment only models air density, air temperature, and road gradient.

$$\theta_r = \frac{d}{dd} h(d) \quad (19)$$

$$T_{amb} = T_0 - Lh(d) \quad (20)$$

$$P = P_0 \left( 1 - \frac{Lh(d)}{T_0} \right)^{\frac{gM}{RL}} \quad (21)$$

$$\rho = \frac{PM}{1000RT} \quad (22)$$

### 2.1.4 Parameters

Parameter	Symbol	Unit
Temperature Lapse	$L$	$K/m$
Initial Pressure	$P_0$	$Pa$
Initial Temperature	$T_0$	K
Gravity	$g$	$m/s^2$
Molar mass of Dry Air	$M$	kg/mol
Ideal Gas Constant	$R$	$\frac{J}{mol*K}$

### 2.1.5 Look up Table

$h(d)$			
Type	Description	Symbol	Unit
Input	Distance Travel	$d$	m
Output	height	n/a	m

### 2.1.6 Assumptions

- The air is dry
- Temperature lapse rate right is correct (no inversion)