# **SimBALink**

# 1 Vehicle

This system models the forces acting on the vehicle.

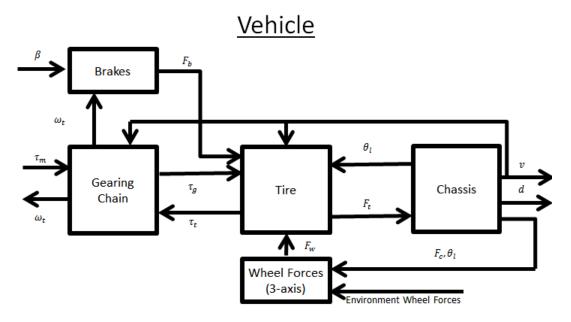


Figure 1: Vehicle Diagram

# 1.1 Gearing and Chain

This system models the gear and chain in such a way to allow for wheel slip.

# 1.2 Inputs and outputs

# 1.2.1 Inputs

| Input        | Symbol  | Unit |
|--------------|---------|------|
| Motor Torque | $	au_m$ | Nm   |
| Tire Torque  | $	au_t$ | Nm   |

# 1.2.2 Outputs

| Output        | Symbol     | Unit  |
|---------------|------------|-------|
| Tire Velocity | $\omega_t$ | rad/s |
| Gear Torque   | $	au_g$    | Nm    |

#### 1.2.3 Background, rationale, modeling strategy

The tire, chain, gear, and motor are modeled as a lumped inertia that is accelerated by the motor torque and tire torque (modeled as a load). The chain is modeled lossey through an efficiency map. Gearing is modeled as a ratio that linearly changes motor torque to gear torque. This method of modeling allows for wheel slip down the line.

$$\dot{\omega_t} = \frac{\tau_m - \tau_t}{J_m + J_g + J_t + J_c} \tag{1}$$

$$\tau_g = \frac{\tau_m \eta_c(\omega_t)}{R_g} \tag{2}$$

#### **1.2.4** States

| State         | Symbol     | Unit  |
|---------------|------------|-------|
| Tire Velocity | $\omega_t$ | rad/s |

#### 1.2.5 Variables

| Symbol | Unit                    |
|--------|-------------------------|
| $J_m$  | $kg*m^2$                |
| $J_g$  | $kg*m^2$                |
| $J_c$  | $kg*m^2$                |
| $J_t$  | $kg*m^2$                |
| $R_g$  | $\frac{\tau_m}{\tau_a}$ |
|        | $J_m$ $J_g$ $J_c$       |

#### 1.2.6 Functions

 $\eta_c(\omega_t)$ 

| Type   | Description      | Symbol     | Unit  |
|--------|------------------|------------|-------|
| Input  | Wheel Speed      | $\omega_t$ | rad/s |
| Output | Chain Efficiency | n/a        | %     |

The function is modeled as a look up table following the curve below described in the paper "Optimization of Chain Drives in Sports Motorcycles".

# 1.2.7 Assumptions

- The chain and gearing is rigid (no chain/gear dynamics)
- Chain efficiency is only a function of wheel speed

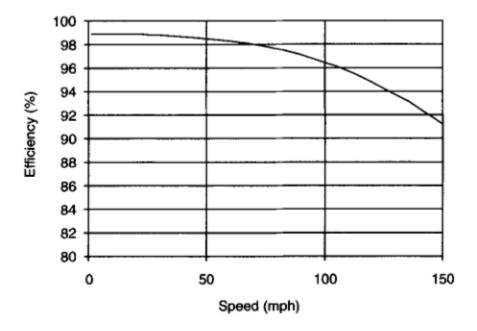


Figure 2: Estimated Chain Efficiency

# 1.3 Brakes

# 1.4 Inputs and outputs

# 1.4.1 Inputs

| Input         | Symbol               | Unit  |
|---------------|----------------------|-------|
| Brake Command | beta                 | %     |
| Wheel Speed   | $\mid \omega_t \mid$ | rad/s |

# 1.4.2 Outputs

| Output              | Symbol | Unit |
|---------------------|--------|------|
| Brake Force on Tire | $F_b$  | N    |

# 1.4.3 Background, rationale, modeling strategy

The brake is modeled as a friction force and a constant that converts  $\beta$  to a force.

$$F_b = \mu_b \omega_t \beta k_b \tag{3}$$

#### 1.4.4 Variables

| Var                           | Symbol  | Unit              |
|-------------------------------|---------|-------------------|
| Brake Coefficient of Friction | $\mu_b$ | $\frac{N}{rad/s}$ |
| Force Constant                | $k_b$   | $\frac{N}{\%}$    |

#### 1.4.5 Assumptions

• Brake percentage to friction force is linear

# 1.5 Tires

# 1.6 Inputs and outputs

#### 1.6.1 Inputs

| Input            | Symbol     | Unit                 |
|------------------|------------|----------------------|
| Brake Force      | $F_b$      | N                    |
| Gear Torque      | $	au_g$    | Nm                   |
| Wheel Forces[3]  | $F_w$      | N[3]                 |
| Vehicle Velocity | v          | m/s                  |
| Lead Angle       | $\theta_l$ | $\operatorname{rad}$ |

# 1.6.2 Outputs

| Output              | Symbol          | Unit |
|---------------------|-----------------|------|
| Tire Torque         | $  	au_t  $     | Nm   |
| Tire Reaction Force | $\mid F_t \mid$ | N    |

# 1.6.3 Background, rationale, modeling strategy

The tire is modeled in three parts, rolling resistance, Load and Torque, and Traction Limiting. Force directions are defined as longitudinal(long), lateral(lat), and normal(n). Longitudinal is along the direction of the motorcycle (when moving straight). Lateral is orthogonal to Longitudinal axis. Normal 3-D orthogonal to lateral and longitudinal, in general the axis to the road on no incline.

In general the tire model provides a load on the Gear/Chain and gives the vehicle a reaction force. Load is caused by the forces from the road(from the vehicle) and rolling resistance. the reaction force caused by traction limiting which is a function of wheel slip. The amount of reaction force i saturated at the maximum force the tire can apply given wheel slip.

### Rolling Resistance

$$K_{t} = \begin{cases} 0.0085 + \frac{0.18}{p_{t}} + \frac{1.59*10^{-6}}{p_{t}} &: v_{kph} \le 165(km/h) \\ \frac{0.18}{p_{t}} + \frac{2.91*10^{-6}}{p_{t}} &: v_{kph} > 165(km/h) \end{cases}$$
(4)

#### Wheel Slip

$$\kappa = \frac{v - \omega_t r_t(\theta_l)}{v} \tag{5}$$

$$\mu_{t,gnd} = D_{\kappa} \sin(C_{\kappa} \arctan[B_{\kappa}\kappa - E_{\kappa}(B_{\kappa}\kappa - \arctan B_{\kappa}\kappa)])$$
 (6)

# Load and Torque

$$\tau_t = \tau_g - F_{w,long} r_t(\theta_l) - F_b r_b - K_t F_{w,n} v_{kph}^2 \tag{7}$$

#### **Traction Limiting**

$$F_{max} = \mu_{t,gnd} F_{w,n} \tag{8}$$

$$F = \tau r_t((\theta_l) \tag{9}$$

$$F_t = \begin{cases} F & : -F_{max} \le F \le F_{max} \\ F_{max} & : -F_{max} > F > F_{max} \end{cases}$$
 (10)

The tire coefficient  $(\mu_{t,gnd})$  is modeled using the "Magic Formula" as shown below. Where  $D_{\kappa}$  is the maximum tire coefficient of the tire.

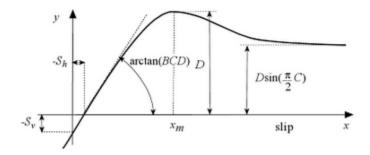


Figure 3: Magic Formula

#### 1.6.4 Variables

| Var                  | Symbol | Unit |
|----------------------|--------|------|
| Tire Pressure        | $p_t$  | bar  |
| Brake Caliper Radius | $r_b$  | m    |

#### 1.6.5 Parameters

| Param.        | Symbol   | Unit |
|---------------|--|------|
| Magic Formula |  |      |
|               | $A_{\kappa}, B_{\kappa}, C_{\kappa}, D_{\kappa}$ | n/a  |

#### 1.6.6 Function

 $r_t(\theta_l)$ 

| Type   | Description | Symbol     | $\operatorname{Unit}$ |
|--------|-------------|------------|-----------------------|
| Input  | Lean Angle  | $\theta_l$ | rad                   |
| Output | Tire Radius | n/a        | m                     |

#### 1.6.7 Assumptions

- Maximum acceleration force should also depend on lateral forces on the vehicle. However this is not modeled because it requires modeling of high-side and low-side dynamics. The Rider model should control for a safe operating area of the motorcycle to compensate for this assumption.
- No tire deformation
- No tire temperature dynamics
- No change in rolling resistance with lean angle

#### 1.7 Wheel Forces

Wheel Forces does nothing. It would allow for the environment to affect tire forces.

$$F_{\omega,long} = F_{c,long} \tag{11}$$

$$F_{\omega,n} = F_{c,n} \tag{12}$$

#### 1.8 Chassis

This system models the chassis of the motorcycle including the velocity of the motorcycle and forces on the road.

# 1.9 Inputs and outputs

# 1.9.1 Inputs

| Input         | Symbol    | Unit     |
|---------------|-----------|----------|
| Tire Force    | $F_t$     | N        |
| Air Density   | ho        | $kg/m^3$ |
| Road Gradient | $	heta_r$ | rad      |

#### 1.9.2 Outputs

| Output            | Symbol     | Unit |
|-------------------|------------|------|
| Vehicle Velocity  | v          | m/s  |
| Distance Traveled | d          | m    |
| Lean Angle        | $\theta_l$ | rad  |

# 1.9.3 Background, rationale, modeling strategy

The Chassis is modeled point mass with drag.

$$F_a = \frac{1}{2}\rho C_d A v^2 \tag{13}$$

$$F_{c,long} = F_a + gm\sin(\theta_r) \tag{14}$$

$$F_{c,n} = mg\cos(\theta_r) \tag{15}$$

$$\dot{v} = mF_t \tag{16}$$

$$\dot{d} = v \tag{17}$$

#### 1.9.4 States

| State    | Symbol | Unit |
|----------|--------|------|
| Distance | d      | m    |
| Velocity | v      | m/s  |

### 1.9.5 Variables

| Output             | Symbol        | Unit    |
|--------------------|---------------|---------|
| Gravity            | g             | $m/s^2$ |
| Mass of Motorcycle | $\mid m \mid$ | kg      |

### 1.9.6 Parameters

| Param.    | Symbol | Unit              |
|-----------|--------|-------------------|
| Drag Area | $C_dA$ | $\frac{N}{rad/s}$ |

# 1.9.7 Look Up table

 $\theta_l(d)$ 

| Type   | Description       | $_{\text{Symbol}}$ | $\operatorname{Unit}$ |
|--------|-------------------|--------------------|-----------------------|
| Input  | Distance Traveled | d                  | m                     |
| Output | Lean Angle        | n/a                | $\operatorname{rad}$  |

# 1.9.8 Assumptions

• The full weight of the motorcycle is always on the correct tire for breaking or acceleration. That is not a bad assumption because maximum braking or

acceleration will happen at wheelie or stoppie when there is only one tire on the ground.

- Lean angle does not affect Aero Drag
- No lateral forces

# 2 Environment

This system models the environment of the motorcycle is riding in.

Force directions are defined as longitudinal(long), lateral(lat), and normal(n). Longitudinal is along the direction of the motorcycle (when moving straight). Lateral is orthogonal to Longitudinal axis. Normal 3-D orthogonal to lateral and longitudinal, in general the axis to the road on no incline.

# 2.1 Inputs and outputs

#### **2.1.1** Inputs

| Input           | Symbol | $\operatorname{Unit}$ |
|-----------------|--------|-----------------------|
| Distance Travel | d      | m                     |

# 2.1.2 Outputs

| Output                        | Symbol    | Unit     |
|-------------------------------|-----------|----------|
| Environment Forces on Tire[3] | $F_t$     | N[3]     |
| Road Gradient                 | $	heta_r$ | rad      |
| Ambient Temperature           | $T_{amb}$ | K        |
| Air Pressure                  | P         | Pa       |
| Air Density                   | ho        | $kg/m^3$ |

#### 2.1.3 Background, rationale, modeling strategy

The Environment only models air density, air temperature, and road gradient.

$$\theta_r = \frac{d}{dd}h(d) \tag{18}$$

$$T_a m b = T_0 - L h(d) \tag{19}$$

$$P = P_0 \left( 1 - \frac{Lh(d)}{T_0} \right)^{\frac{gM}{RL}} \tag{20}$$

$$\rho = \frac{PM}{1000RT} \tag{21}$$

# 2.1.4 Variables

| Output                | Symbol        | Unit              |
|-----------------------|---------------|-------------------|
| Temperature Lapse     | L             | K/m               |
| Initial Pressure      | $P_0$         | Pa                |
| Initial Temperature   | $T_0$         | K                 |
| Gravity               | $\mid g \mid$ | $m/s^2$           |
| Molar mass of Dry Air | M             | kg/mol            |
| Ideal Gas Constant    | R             | $\frac{J}{mol*K}$ |

# 2.1.5 Look up Table

h(d)

| Type   | Description     | Symbol | Unit |
|--------|-----------------|--------|------|
| Input  | Distance Travel | d      | m    |
| Output | height          | n/a    | m    |

# 2.1.6 Assumptions

- The air is dry
- $\bullet$  Temperature lapse rate right is correct (no inversion)