

# Mandelbrot Set

For each complex number  $c$  we define a quadratic map

$$f_c : \mathbb{C} \rightarrow \mathbb{C}, \quad f_c(z) = z^2 + c.$$

We consider the orbit of  $0$  under this map, that is, the sequence

$$0, \ f_c(0), \ f_c^2(0), \ f_c^3(0), \ \dots$$

The **Mandelbrot set**  $\mathbf{M}$  is the set of all complex numbers  $c$  for which this sequence is bounded.