

Complex Numbers

$$\mathbb{C} = \{a + bi : a, b \in \mathbb{R}\},$$

where i is the imaginary unit, satisfying $i^2 = -1$.

There is a one-to-one correspondence between complex numbers and points on the xy -plane: $a + bi \longleftrightarrow (a, b)$

$$\text{Addition: } (a + bi) + (c + di) = (a + c) + (b + d)i$$

$$\text{Multiplication: } (a + bi)(c + di) = (ac - bd) + (ad + bc)i$$

$$\text{Modulus or absolute value: } |a + bi| = \sqrt{a^2 + b^2} = \text{distance to } 0$$

$$\text{For any } z, w \in \mathbb{C}, \quad |zw| = |z| |w| \quad \text{and} \quad |z^n| = |z|^n$$

$$\text{The complex conjugate of } c = a + bi \text{ is } \bar{c} = a - bi, \text{ and } |\bar{c}| = |c|.$$