

MATH 312 Sections 1 & 2 Concepts of Real Analysis Fall 2023 Schedule

| Lec. | Date | Section | Topic |
|------|----------|---------|---|
| 1 | 8/21 | 2, 3 | Introduction. Rational numbers. Ordered fields. |
| 2 | 8/23 | 3, 4 | Absolute value. Maximum and minimum. Upper and lower bounds. |
| 3 | 8/25 | 4 | Supremum and infimum. Completeness Axiom. |
| 4 | 8/28 | 4, 5 | Quiz 1. Archimedean property. Denseness of \mathbb{Q} in \mathbb{R} . Symbols ∞ and $-\infty$. |
| 5 | 8/30 | 7, 8 | Sequences. Limits of sequences. Definition and examples. |
| 6 | 9/1 | 7, 8, 9 | Uniqueness of the limit. Diverging sequences. Bounded sequences. |
| - | 9/4 | | <i>Labor Day - no classes.</i> |
| 7 | 9/6 | 9 | Quiz 2. Limit theorems for sequences: constant multiple, sum, product. |
| 8 | 9/8 | 9 | Limit of a quotient. Squeeze Lemma (Ex. 8.5). Binomial Theorem (Ex. 1.12). |
| 9 | 9/11 | 9 | Quiz 3. Basis examples. Sequences diverging to ∞ and $-\infty$. |
| 10 | 9/13 | | Team Worksheet 1. |
| 11 | 9/15 | 10 | Monotone sequences. |
| 12 | 9/18 | 10 | Quiz 4. \liminf and \limsup . |
| 13 | 9/20 | 10 | Cauchy sequences. |
| 14 | 9/22 | 11 | Subsequences. Bolzano - Weierstrass Theorem. |
| 15 | 9/25 | 11 | Quiz 5. Limits of subsequences. |
| 16 | 9/27 | | Team Worksheet 2. |
| 17 | 9/29 | | Review |
| 18 | 10/2 | | Exam 1: Real numbers and sequences. |
| 19 | 10/4 | 14 | Series: definitions and examples. Decimals. |
| 20 | 10/6 | 14 | Cauchy Criterion. Absolute convergence. Comparison Test. |
| 21 | 10/9 | 14 | Quiz 6. Root Test and Ratio Test. |
| 22 | 10/11 | 23, 15 | Power series. Alternating Series Theorem. |
| 23 | 10/13 | | Team Worksheet 3. |
| 24 | 10/16 | 17 | Quiz 7. Continuous functions. Two definitions of continuity |
| 25 | 10/18 | 17 | Examples of continuous and discontinuous functions. |
| 26 | 10/20 | 17 | Continuity of kf , $ f $, $f + g$, fg , f/g , and $g \circ f$. |
| 27 | 10/23 | 18 | Quiz 8. Properties of continuous functions. |
| 28 | 10/25 | 19 | Uniform continuity. |
| 29 | 10/27 | 20 | Limits of functions. (Notes.) |
| 30 | 10/30 | | Quiz 9. More on limits and continuity. (Notes.) |
| 31 | 11/1 | | Team Worksheet 4. |
| 32 | 11/3 | | Review. |
| 33 | 11/6 | | Exam 2: Series and continuous functions. |
| 34 | 11/8 | 28 | Derivative: definition and examples. Continuity and differentiability. |
| 35 | 11/10 | 28 | Sum, product, quotient, and chain rules. |
| 36 | 11/13 | 29 | Quiz 10. Zeros of the derivative. Mean Value Theorem. |
| 37 | 11/15 | 29, 18 | Corollaries of the MVT. Inverse function and its derivative. |
| 38 | 11/17 | | Linear approximation and Taylor polynomials. (Notes.) |
| | 11/19-25 | | <i>Thanksgiving break - no classes</i> |
| 39 | 11/27 | 32 | Quiz 11. The Riemann Integral: Darboux construction. |
| 40 | 11/29 | | |
| 41 | 12/1 | | |
| 42 | 12/4 | | Quiz 12. |
| 43 | 12/6 | | Team Worksheet 5. |
| 44 | 12/8 | | Review |

Final Exam: Thursday, December 14, 8:00-9:50 a.m. in 135 Reber Building.