Cryptography and Network Security
Block Ciphers and DES

Fifth Edition

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Content

- Block Cipher Principles
- The Data Encryption Standard
- DES Details
- DES Design Issues and Attacks
- 3DES, AES and Other Block Ciphers

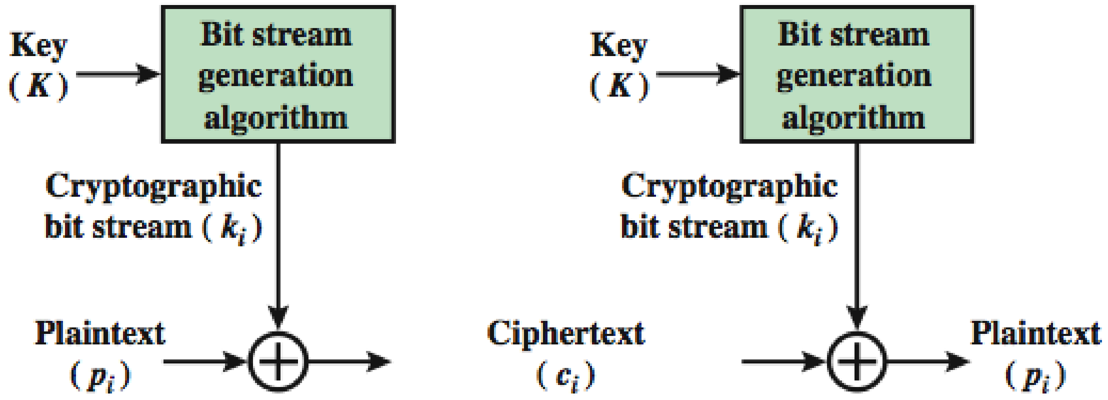
The objectives

- now look at modern block ciphers
- one of the most widely used types of cryptographic algorithms
- provide secrecy /authentication services
- focus on DES (Data Encryption Standard)
- to illustrate block cipher design principles

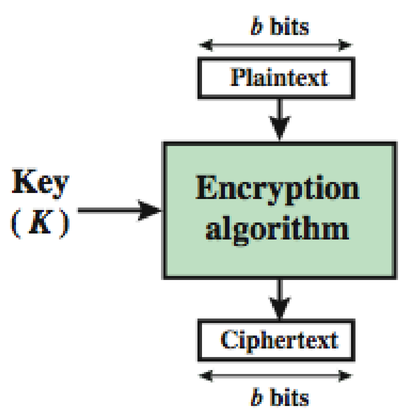
Block Ciphers

- Encrypt data one block at a time
- „Used in broader range of applications
- „Typical block size 64 – 128 bits
- „Most algorithms based on a structure referred to as Feistel block cipher

Block vs Stream Ciphers



(a) Stream Cipher Using Algorithmic Bit Stream Generator



(b) Block Cipher

Block cipher principles

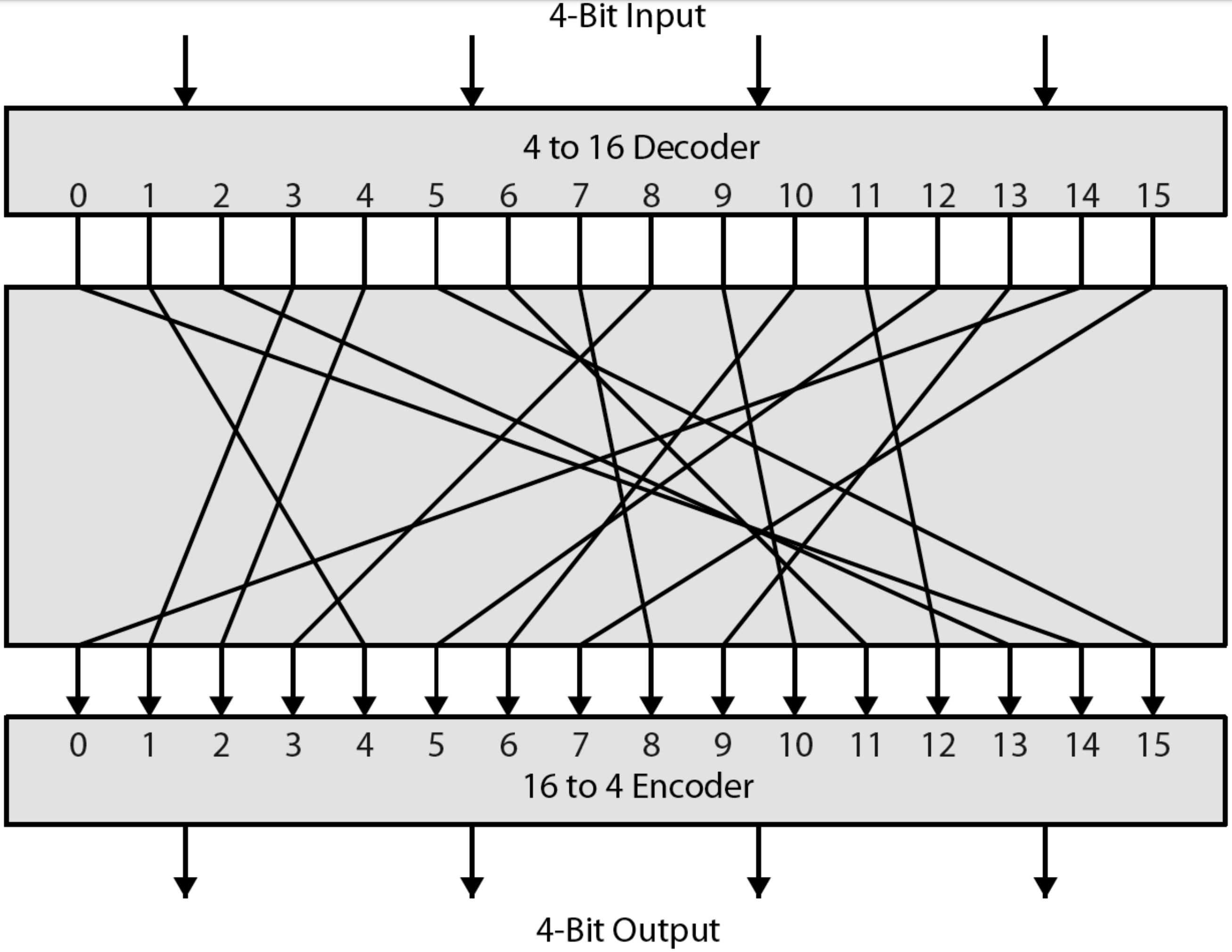
- n-bit block cipher takes n bit plaintext and produces n bit ciphertext
- 2^n possible different plaintext blocks
- Encryption must be reversible (decryption possible)
- Each plaintext block must produce unique ciphertext block
- Total transformations is $2^n!$

Reversible Mapping	
Plaintext	Ciphertext
00	11
01	10
10	00
11	01

Irreversible Mapping	
Plaintext	Ciphertext
00	11
01	10
10	01
11	01

Ideal Block Cipher

key is mapping ; Key length **16 × 4 bits = 64 bits** . i.e. concatenate all bits of ciphertext table



Encryption/decryption table

Plaintext	Ciphertext
0000	1110
0001	0100
0010	1101
0011	0001
0100	0010
0101	1111
0110	1011
0111	1000
1000	0011
1001	1010
1010	0110
1011	1100
1100	0101
1101	1001
1110	0000
1111	0111

Ciphertext	Plaintext
0000	1110
0001	0011
0010	0100
0011	1000
0100	0001
0101	1100
0110	1010
0111	1111
1000	0111
1001	1101
1010	1001
1011	0110
1100	1011
1101	0010
1110	0000
1111	0101

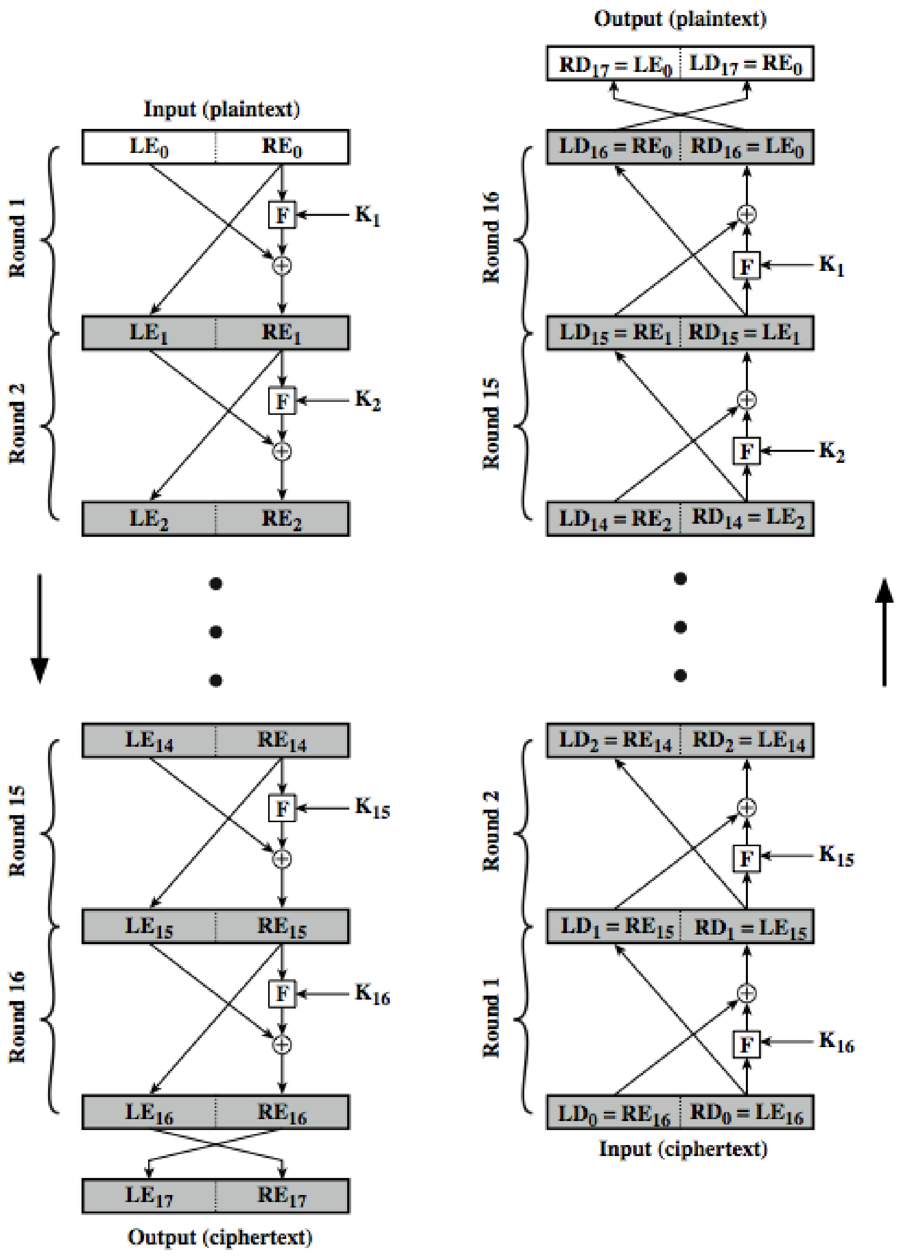
Ideal Block Cipher

- n-bit input maps to 2^n possible input states
- Substitution used to produce 2^n output states
- Output states map to n-bit output
- Ideal block cipher allows maximum number of possible encryption mappings from plaintext block
- Problems with ideal block cipher:
  - Small block size: equivalent to classical substitution cipher; cryptanalysis based on statistical characteristics feasible
  - Large block size: key must be very large; performance/implementation problems
- **Key length :**
  - In general, key length is $2^n \times n$
  - „Actual block size is at least 64 bit („**Key length will be $2^{64} \times 64 \approx 10^{21}$ „bits**)

Feistel Structure for Block Ciphers

- Feistel proposed applying two or more simple ciphers in sequence so final result cryptographically stronger than component ciphers
- **n-bit** block length; **k-bit** key length; $\mathbf{2^k}$ transformations (rather than 2^n !)
- Feistel cipher alternates: substitutions, transpositions (permutations)
- Applies concepts of diffusion and confusion
- Applied in many ciphers today
- Approach:
  - Plaintext split into halves
  - Subkeys (or round keys) generated from key
  - Round function, F, applied to right half
  - Apply substitution on left half using XOR
  - Apply permutation: interchange to halves
- implements Shannon's S-P net concept

Feistel Cipher Structur



Confusion and Diffusion

- **Diffusion**
  - Statistical nature of plaintext is reduced in ciphertext
  - E.g. A plaintext letter affects the value of many ciphertext letters
  - How: repeatedly apply permutation (transposition) to data, and then apply function
- **Confusion**
  - Make relationship between ciphertext and key as complex as possible
  - Even if attacker can find some statistical characteristics of ciphertext, still hard to find key
  - How: apply complex (non-linear) substitution algorithm

Using the Feistel Structure

- Exact implementation depends on various design features
  - **Block size**, e.g. 64, 128 bits: larger values leads to more diffusion
  - **Key size**, e.g. 128 bits: larger values leads to more confusion, resistance against brute force
  - **Number of rounds**, e.g. 16 rounds
  - **Subkey generation algorithm**: should be complex
  - **Round function F**: should be complex
- Other factors include fast encryption in software and ease of analysis
- Tradeoff : **security vs performance**

Feistel Example

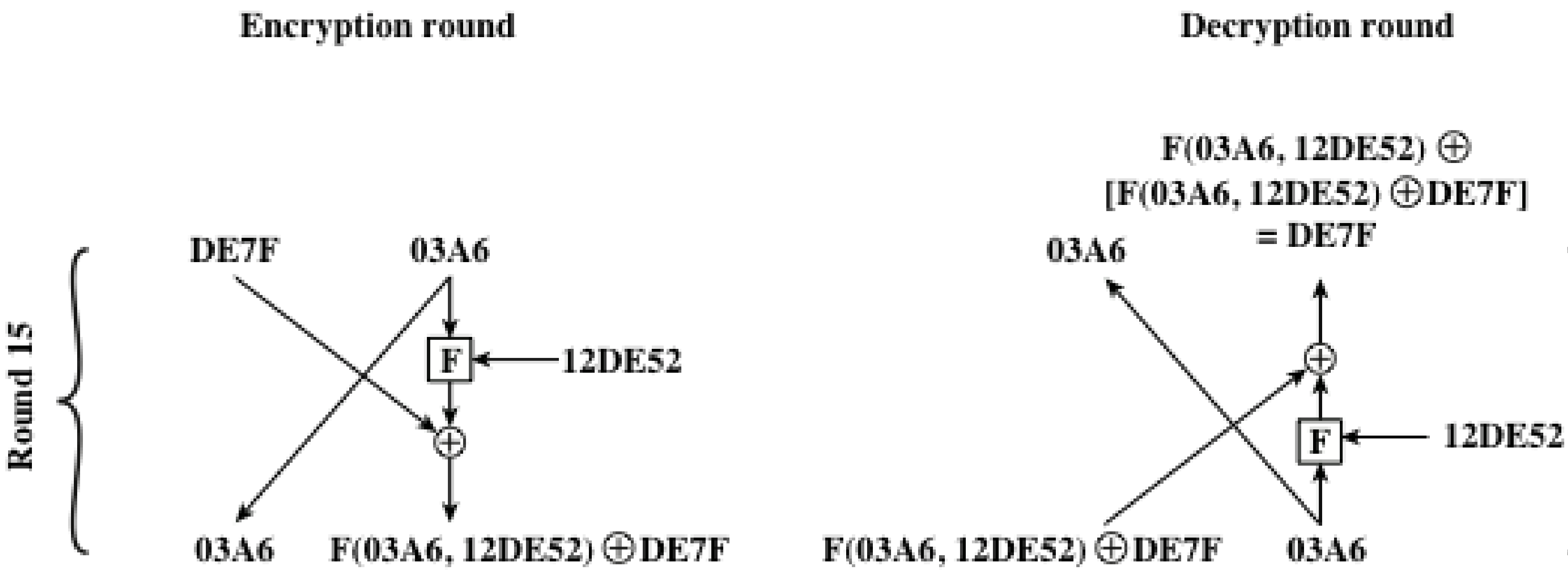


Figure 3.4 Feistel Example

Data Encryption Standard (DES)

- Symmetric block cipher
  - 56-bit key, 64-bit input block, 64-bit output block
- One of most used encryption systems in world
  - Developed in 1977 by NBS/NIST
  - Designed by IBM (Lucifer) with input from NSA
  - Principles used in other ciphers, e.g. 3DES, IDEA

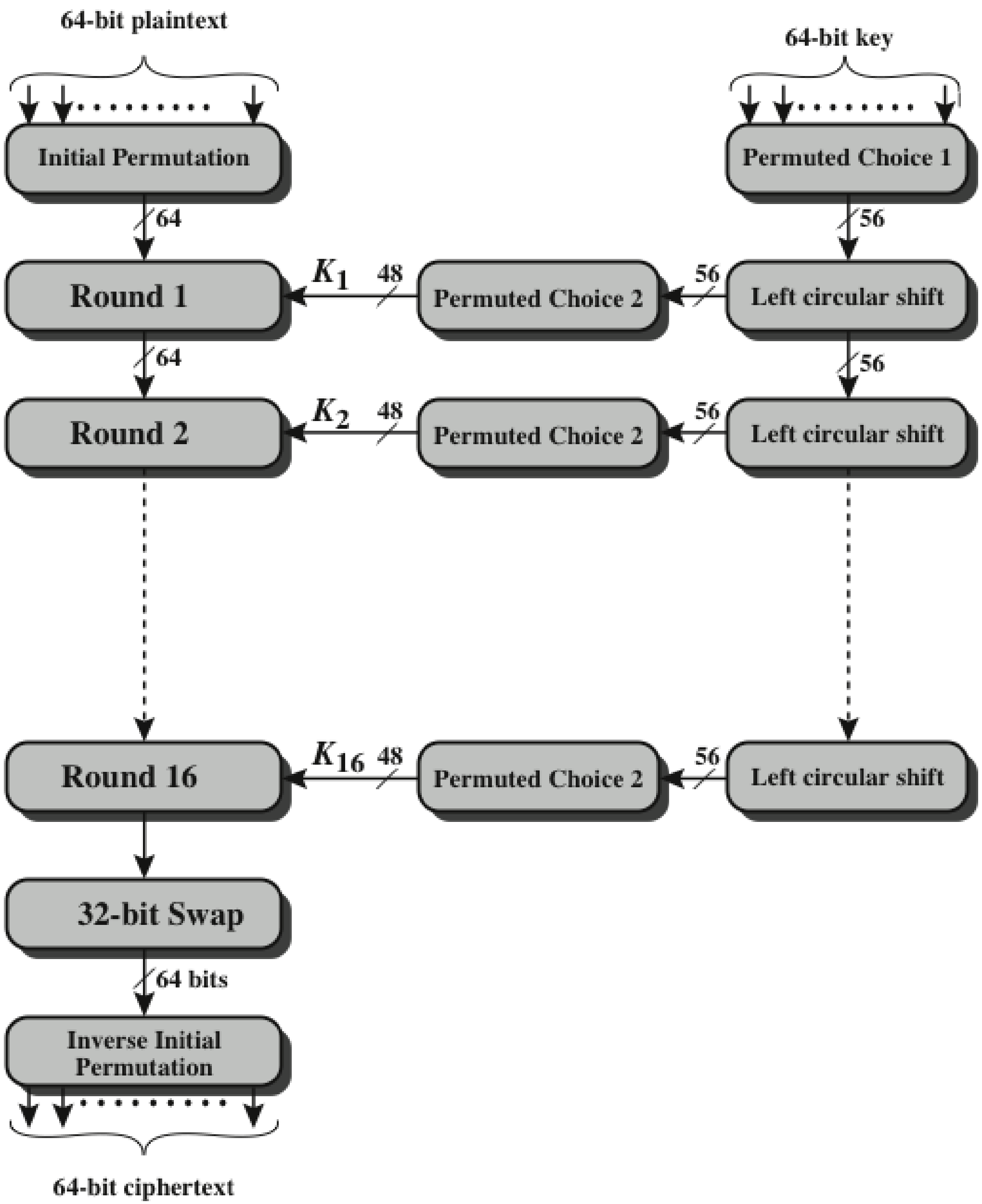


Figure 3.5 General Depiction of DES Encryption Algorithm

DES Encryption Algorithm

Permutation Tables for DES

(a) Initial Permutation (IP)

58	50	42	34	26	18	10	2
60	52	44	36	28	20	12	4
62	54	46	38	30	22	14	6
64	56	48	40	32	24	16	8
57	49	41	33	25	17	9	1
59	51	43	35	27	19	11	3
61	53	45	37	29	21	13	5
63	55	47	39	31	23	15	7

(b) Inverse Initial Permutation (IP^{-1})

40	8	48	16	56	24	64	32
39	7	47	15	55	23	63	31
38	6	46	14	54	22	62	30
37	5	45	13	53	21	61	29
36	4	44	12	52	20	60	28
35	3	43	11	51	19	59	27
34	2	42	10	50	18	58	26
33	1	41	9	49	17	57	25

Permutation Tables for DES

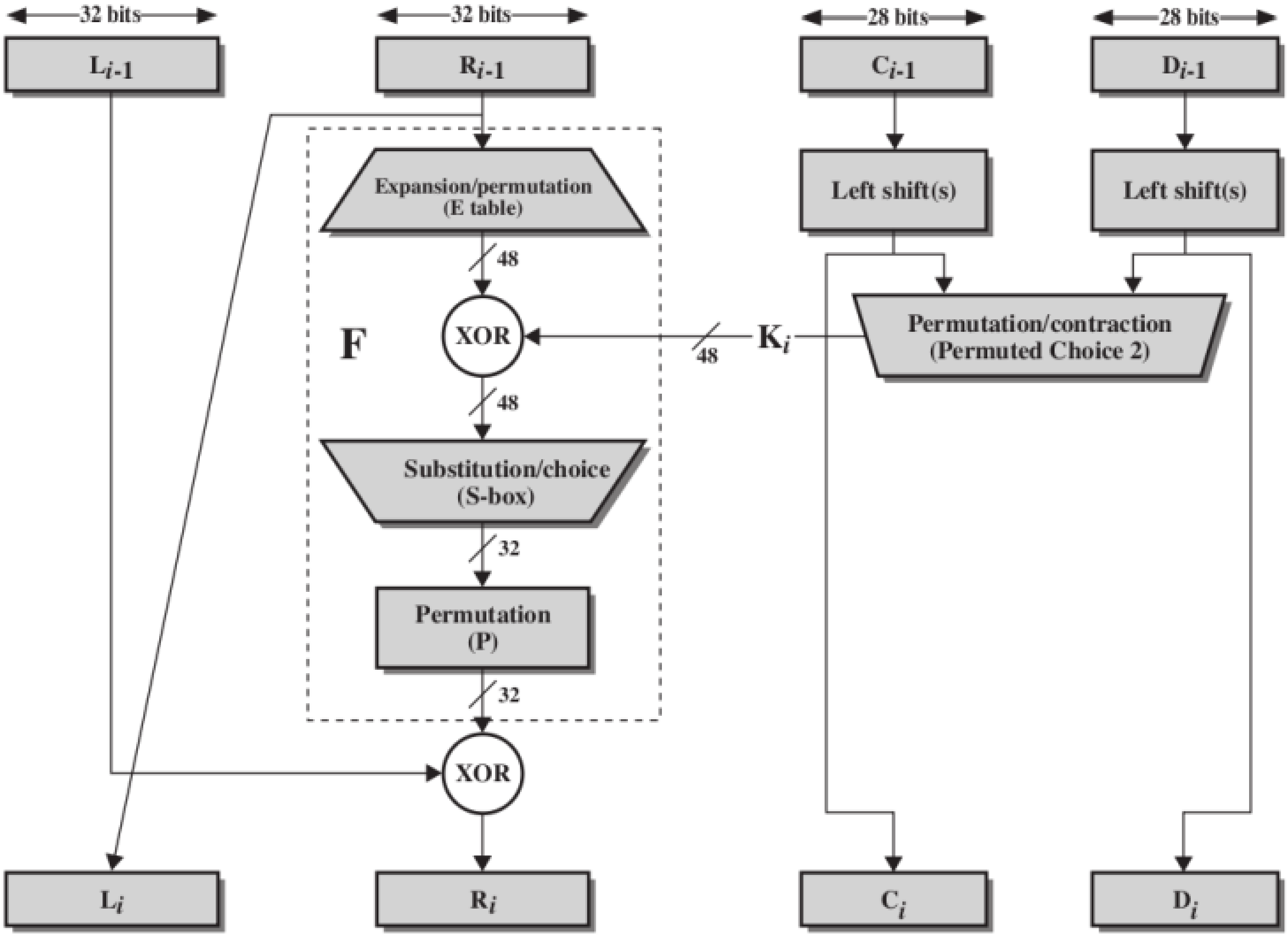
3: Expansion permutation (E)

32	01	02	03	04	05
04	05	06	07	08	09
08	09	10	11	12	13
12	13	14	15	16	17
16	17	18	19	20	21
20	21	22	23	24	25
24	25	26	27	28	29
28	29	31	31	32	01

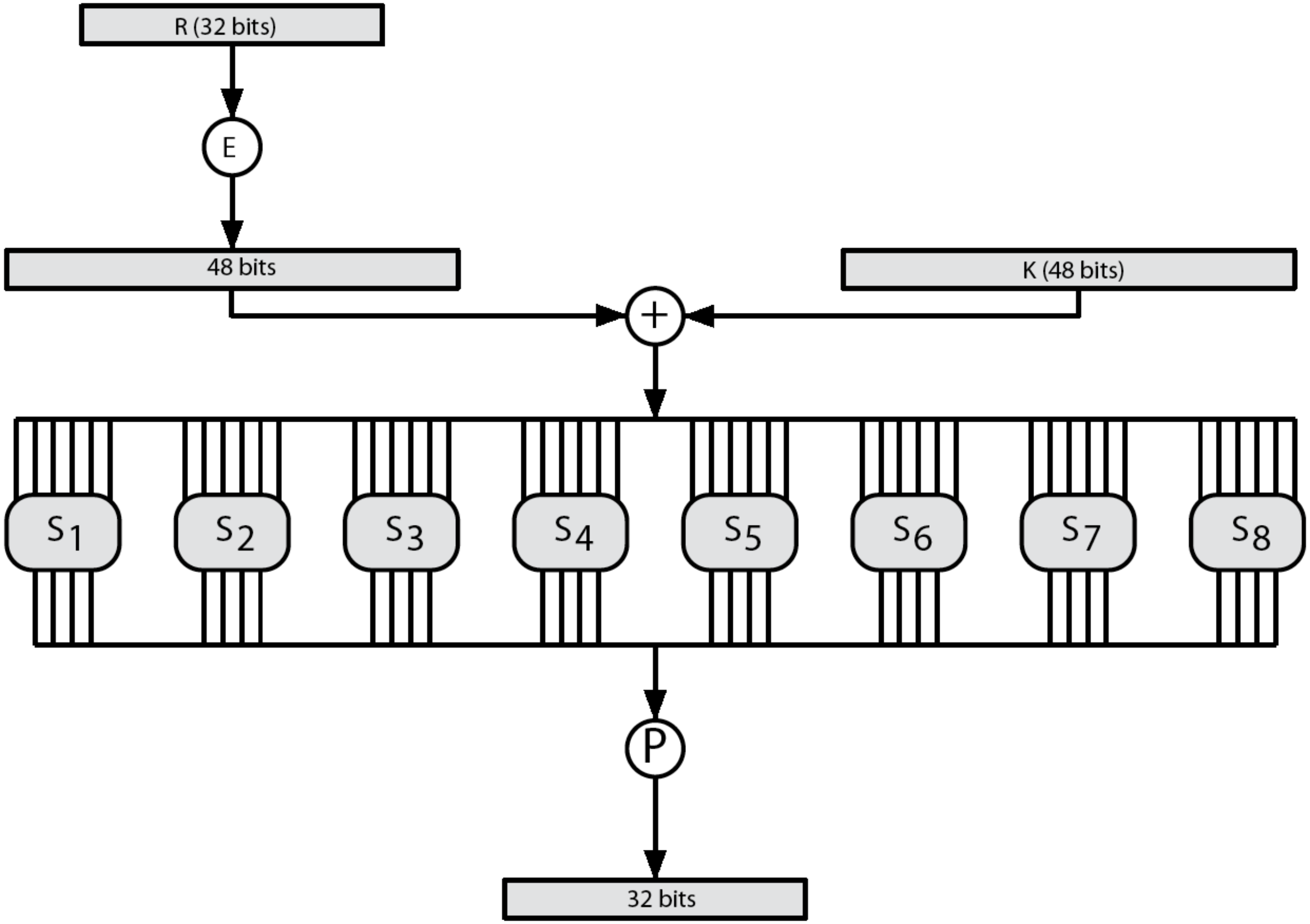
4 : Permutation Function (P)

16	7	20	21	29	12	28	17
1	15	23	26	5	18	31	10
2	8	24	14	32	27	3	9
19	13	30	6	22	11	4	25

Single Round of DES Algorithm



DES Round Structure



Definition of DES S-Boxes

S_1	14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
	0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8
	4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
	15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13
S_2	15	1	8	14	6	11	3	4	9	7	2	13	12	0	5	10
	3	13	4	7	15	2	8	14	12	0	1	10	6	9	11	5
	0	14	7	11	10	4	13	1	5	8	12	6	9	3	2	15
	13	8	10	1	3	15	4	2	11	6	7	12	0	5	14	9
S_3	10	0	9	14	6	3	15	5	1	13	12	7	11	4	2	8
	13	7	0	9	3	4	6	10	2	8	5	14	12	11	15	1
	13	6	4	9	8	15	3	0	11	1	2	12	5	10	14	7
	1	10	13	0	6	9	8	7	4	15	14	3	11	5	2	12
S_4	7	13	14	3	0	6	9	10	1	2	8	5	11	12	4	15
	13	8	11	5	6	15	0	3	4	7	2	12	1	10	14	9
	10	6	9	0	12	11	7	13	15	1	3	14	5	2	8	4
	3	15	0	6	10	1	13	8	9	4	5	11	12	7	2	14

Definition of DES S-Boxes

	2	12	4	1	7	10	11	6	8	5	3	15	13	0	14	9
S_5	14	11	2	12	4	7	13	1	5	0	15	10	3	9	8	6
	4	2	1	11	10	13	7	8	15	9	12	5	6	3	0	14
	11	8	12	7	1	14	2	13	6	15	0	9	10	4	5	3

	12	1	10	15	9	2	6	8	0	13	3	4	14	7	5	11
S_6	10	15	4	2	7	12	9	5	6	1	13	14	0	11	3	8
	9	14	15	5	2	8	12	3	7	0	4	10	1	13	11	6
	4	3	2	12	9	5	15	10	11	14	1	7	6	0	8	13

	4	11	2	14	15	0	8	13	3	12	9	7	5	10	6	1
S_7	13	0	11	7	4	9	1	10	14	3	5	12	2	15	8	6
	1	4	11	13	12	3	7	14	10	15	6	8	0	5	9	2
	6	11	13	8	1	4	10	7	9	5	0	15	14	2	3	12

	13	2	8	4	6	15	11	1	10	9	3	14	5	0	12	7
S_8	1	15	13	8	10	3	7	4	12	5	6	11	0	14	9	2
	7	11	4	1	9	12	14	2	0	6	10	13	15	3	5	8
	2	1	14	7	4	10	8	13	15	12	9	0	3	5	6	11

DES Key Schedule Calculation

(a) Input Key

1	2	3	4	5	6	7	8
9	10	11	12	13	14	15	16
17	18	19	20	21	22	23	24
25	26	27	28	29	30	31	32
33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48
49	50	51	52	53	54	55	56
57	58	59	60	61	62	63	64

(b) Permuted Choice One (PC-1)

57	49	41	33	25	17	9
1	58	50	42	34	26	18
10	2	59	51	43	35	27
19	11	3	60	52	44	36
63	55	47	39	31	23	15
7	62	54	46	38	30	22
14	6	61	53	45	37	29
21	13	5	28	20	12	4

(c) Permuted Choice Two (PC-2)

14	17	11	24	1	5	3	28
15	6	21	10	23	19	12	4
26	8	16	7	27	20	13	2
41	52	31	37	47	55	30	40
51	45	33	48	44	49	39	56
34	53	46	42	50	36	29	32

(d) Schedule of Left Shifts

Round Number	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Bits Rotated	1	1	2	2	2	2	2	2	1	2	2	2	2	2	2	1

Table 3.2

DES Example

(Table can be found on page 75 in textbook)

Round	K_i	L_i	R_i
IP		5a005a00	3cf03c0f
1	1e030f03080d2930	3cf03c0f	bad22845
2	0a31293432242318	bad22845	99e9b723
3	23072318201d0c1d	99e9b723	0bae3b9e
4	05261d3824311a20	0bae3b9e	42415649
5	3325340136002c25	42415649	18b3fa41
6	123a2d0d04262a1c	18b3fa41	9616fe23
7	021f120b1c130611	9616fe23	67117cf2
8	1c10372a2832002b	67117cf2	c11bfc09
9	04292a380c341f03	c11bfc09	887fbc6c
10	2703212607280403	887fbc6c	600f7e8b
11	2826390c31261504	600f7e8b	f596506e
12	12071c241a0a0f08	f596506e	738538b8
13	300935393c0d100b	738538b8	c6a62c4e
14	311e09231321182a	c6a62c4e	56b0bd75
15	283d3e0227072528	56b0bd75	75e8fd8f
16	2921080b13143025	75e8fd8f	25896490
IP^{-1}		da02ce3a	89ecac3b

Note: DES subkeys are shown as eight 6-bit values in hex format

DES Example

Round	K_i	L_i	R_i
IP		5a005a00	3cf03c0f
1	1e030f03080d2930	3cf03c0f	bad22845
2	0a31293432242318	bad22845	99e9b723
3	23072318201d0c1d	99e9b723	0bae3b9e
4	05261d3824311a20	0bae3b9e	42415649
5	3325340136002c25	42415649	18b3fa41
6	123a2d0d04262a1c	18b3fa41	9616fe23
7	021f120b1c130611	9616fe23	67117cf2
8	1c10372a2832002b	67117cf2	c11bfc09
9	04292a380c341f03	c11bfc09	887fbc6c
10	2703212607280403	887fbc6c	600f7e8b
11	2826390c31261504	600f7e8b	f596506e
12	12071c241a0a0f08	f596506e	738538b8
13	300935393c0d100b	738538b8	c6a62c4e
14	311e09231321182a	c6a62c4e	56b0bd75
15	283d3e0227072528	56b0bd75	75e8fd8f
16	2921080b13143025	75e8fd8f	25896490
IP^{-1}		da02ce3a	89ecac3b

Avalanche Effect

- Aim: small change in key (or plaintext) produces large change in ciphertext
- Avalanche effect is present in DES (good for security)
- Following examples show the number of bits that change in output when two different inputs are used, differing by 1 bit
  - Plaintext 1: 02468aceeca86420
  - Plaintext 2: 12468aceeca86420
  - Ciphertext difference: 32 bits
  - Key 1: 0f1571c947d9e859
  - Key 2: 1f1571c947d9e859
  - Ciphertext difference: 30

Round		δ	Round		δ
	02468aceeca86420 12468aceeca86420	1	9	c11bfc09887fbc6c 99f911532eed7d94	32
1	3cf03c0fbad22845 3cf03c0fbad32845	1	10	887fbc6c600f7e8b 2eed7d94d0f23094	34
2	bad2284599e9b723 bad3284539a9b7a3	5	11	600f7e8bf596506e d0f23094455da9c4	37
3	99e9b7230bae3b9e 39a9b7a3171cb8b3	18	12	f596506e738538b8 455da9c47f6e3cf3	31
4	0bae3b9e42415649 171cb8b3ccaca55e	34	13	738538b8c6a62c4e 7f6e3cf34bc1a8d9	29
5	4241564918b3fa41 ccaca55ed16c3653	37	14	c6a62c4e56b0bd75 4bc1a8d91e07d409	33
6	18b3fa419616fe23 d16c3653cf402c68	33	15	56b0bd7575e8fd8f 1e07d4091ce2e6dc	31
7	9616fe2367117cf2 cf402c682b2cefbc	32	16	75e8fd8f25896490 1ce2e6dc365e5f59	32
8	67117cf2c11bfc09 2b2cefbc99f91153	33	IP–1	da02ce3a89ecac3b 057cde97d7683f2a	32

Table 3.3 Avalanche Effect in DES: Change in Plaintext

Round		δ
	02468aceeca86420 02468aceeca86420	0
1	3cf03c0fbad22845 3cf03c0f9ad628c5	3
2	bad2284599e9b723 9ad628c59939136b	11
3	99e9b7230bae3b9e 9939136b768067b7	25
4	0bae3b9e42415649 768067b75a8807c5	29
5	4241564918b3fa41 5a8807c5488dbe94	26
6	18b3fa419616fe23 488dbe94aba7fe53	26
7	9616fe2367117cf2 aba7fe53177d21e4	27
8	67117cf2c11bfc09 177d21e4548f1de4	32

Round		δ
9	c11bfc09887fbc6c 548f1de471f64dfd	34
10	887fbc6c600f7e8b 71f64dfd4279876c	36
11	600f7e8bf596506e 4279876c399fdc0d	32
12	f596506e738538b8 399fdc0d6d208dbb	28
13	738538b8c6a62c4e 6d208dbbb9bdeeaa	33
14	c6a62c4e56b0bd75 b9bdeeaad2c3a56f	30
15	56b0bd7575e8fd8f d2c3a56f2765c1fb	33
16	75e8fd8f25896490 2765c1fb01263dc4	30
IP^{-1}	da02ce3a89ecac3b ee92b50606b62b0b	30

Table 3.4 Avalanche Effect in DES: Change in Key

Table 3.5

Average Time Required for Exhaustive Key Search

Key size (bits)	Cipher	Number of Alternative Keys	Time Required at 10^{9} decryptions/s	Time Required at 10^{13} decryptions/s
56	DES	$2^{56} \approx 7.2 \times 10^{16}$	2^{55} ns = 1.125 years	1 hour
128	AES	$2^{128} \approx 3.4 \times 10^{38}$	2^{127} ns = 5.3×10^{21} years	5.3×10^{17} years
168	Triple DES	$2^{168} \approx 3.7 \times 10^{50}$	2^{167} ns = 5.8×10^{33} years	5.8×10^{29} years
192	AES	$2^{192} \approx 6.3 \times 10^{57}$	2^{191} ns = 9.8×10^{40} years	9.8×10^{36} years
256	AES	$2^{256} \approx 1.2 \times 10^{77}$	2^{255} ns = 1.8×10^{60} years	1.8×10^{56} years
26 characters (permutation)	Monoalphabetic	$26! = 4 \times 10^{26}$	2×10^{26} ns = 6.3×10^{9} years	6.3×10^{6} years

Key size

- Although 64 bit initial key, only 56 bits used in encryption (other 8 for parity check)
- $2^{56} = 7.2 \times 10^{16}$
  - 1977: estimated cost $US20m to build machine to break in 10 hours
  - 1998: EFF built machine for $US250k to break in 3 days
  - Today: 56 bits considered too short to withstand brute force attack
- 3DES uses 128-bit keys

Attacks on DES

- **Timing Attacks**
  - Information gained about key/plaintext by observing how long implementation takes to decrypt
  - No known useful attacks on DES
- **Differential Cryptanalysis**
  - Observe how pairs of plaintext blocks evolve
  - Break DES in 247 encryptions (compared to 255); but require 247 chosen plaintexts
- **Linear Cryptanalysis**
  - Find linear approximations of the transformations
  - Break DES using 243 known plaintexts

DES Algorithm Design

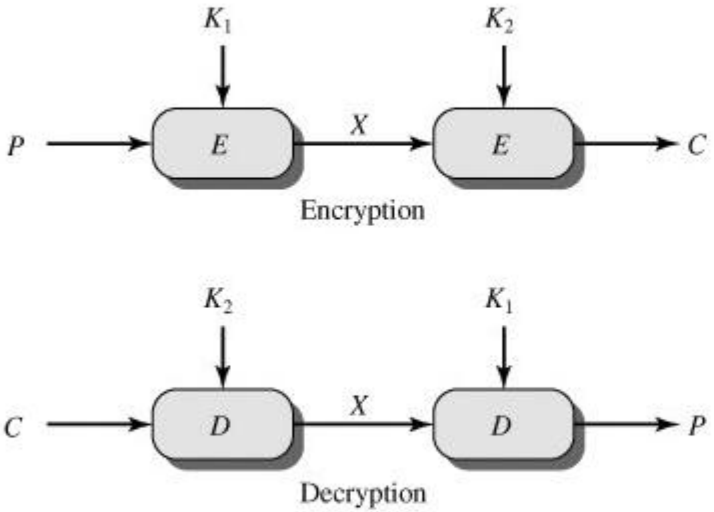
- DES was designed in private; questions about the motivation of the design
  - S-Boxes provide non-linearity: important part of DES, generally considered to be secure
  - S-Boxes provide increased confusion
  - Permutation P chosen to increase diffusion

Multiple Encryption with DES

- DES is vulnerable to brute force attack
- Alternative block cipher that makes use of DES software/equipment/knowledge: encrypt multiple times with different keys
- Options:
  - 1. Double DES: not much better than single DES
  - 2. Triple DES (3DES) with 2 keys: brute force 2^{112}
  - 3. Triple DES with 3 keys: brute force 2^{168}

Double Encryption

- For DES, 2 56-bit keys, meaning 112-bit key length
- Requires 2^{111} operations for brute force?
- Meet-in-the-middle attack makes it easier



(a) Double encryption

Summary

- have considered:
  - block vs stream ciphers
  - Feistel cipher design & structure
  - DES
    - details
    - strength
  - Double DES
  - Triple DES