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I Mehansko nihanje in valovenje

Enostavna nihala

Enadoa dusenega nihanja

Utez ne vijach: vaneti

y=0.

Fg = [

o mgo

navzdo!

y=yo.

Fy = [

o mgo

navzdo!

Fy = [

o mgo

navzdo!

fg = 10 mgo

vaneti Ny

yo < o

yo < o

$$\vec{a} = 0 \iff \vec{F} = m\vec{a} = 0$$

$$\vec{F}_{g} + \vec{F}_{v} = 0$$

$$\hat{F}_{y} = -ky\hat{e}_{y}$$

$$\hat{F}_{u} = -ky\hat{e}$$

y' = (y-y0) = y y')=y' Ddo:mo: y'+(5y+ω²y'=0 je homogena =

y != y-%

$$y' + (3y') + \omega_{o}^{2}y = 0$$
Nastonek: $y' = Ae^{xt}$

$$y' = \lambda y$$

$$y' = \lambda y$$

$$(\lambda^{2} + (3x) + \omega_{o}^{2}) Ae^{xt} = \lambda^{2} + (3x) + \omega_{o}^{2} = 0$$

[1] = m \$0 6 A+0

$$\ddot{y}^{2} = \lambda^{2} y$$

$$(\lambda^{2} + \beta \lambda + \omega_{o}^{2}) A e^{\lambda t} = 0 \quad \text{for } t \neq 0$$

$$\lambda^{2} + \beta \lambda + \omega_{o}^{2} = 0$$

$$+\omega_o^2 = 0$$

$$-4\omega_o^2 = -4\omega^2$$

$$= \omega_o^2 - \left(\frac{5}{2}\right)^2$$

D= 132-4002 =:-402 (w= w2-(B)2) D<0 > uw2>0 : podbitiono dusanje $\sqrt{D} = \sqrt{-4\omega^2} = \sqrt{-1} 2\omega \quad ; \omega = \sqrt{\omega^2}$

 $\Rightarrow \lambda_{1,2} = -\beta \pm \sqrt{D} = -\beta \pm \omega;$

$$D = \beta^{2} - 4\omega^{2} = -4\omega^{2}$$

$$(\omega^{2} = \omega^{2} - (\frac{3}{2})^{2})$$

$$D < 0 \Rightarrow u\omega^{2} > 0 : podki$$

$$\sqrt{D} = \sqrt{-4\omega^{2}} = \sqrt{-4\omega^{2}}$$

$$\Rightarrow \lambda = -3 + 6$$

Y'= A1e>++= A1exp(- = +; w)+)=

= $A_1 \exp(-\frac{18}{2}t) \exp(i\omega t)$

 $y_2' = A_2 \exp \left(\frac{1}{2} + \frac{1}{2} +$

 $y_{1}^{(1)} + (5y_{1}^{(1)} + \omega_{0}^{(2)} y_{1}^{(1)} = 0$ $y_{1}^{(1)} + (5y_{2}^{(1)} + \omega_{0}^{(2)} y_{1}^{(1)} = 0$ $y_{1}^{(1)} + (5y_{2}^{(1)} + \omega_{0}^{(2)} y_{1}^{(1)} = 0$ $y_{2}^{(1)} + (5y_{2}^{(1)} + \omega_{0}^{(2)} y_{1}^{(1)} = 0)$

Eulerjava enacha

(x) + y2) + 13(x, +x2) + Wo(x) - y) = 0

 $\Rightarrow y' = \exp \{-\frac{3}{2}t\}(A_1 \exp(i\omega t) + A_2 \exp\{-i\omega t\})$

[] = S⁻¹

, A, > konskuti

exp { ± iwi3 = cos(wt3 t is:n(wt) =>>)=exp{- (3+)((A+A2)cos(w+)+; (A-X2) sm w+

= e = (B, cos(w+)+Bzs:n(w+)) $Be^{-\frac{C}{2}t}$ sin($w++\delta$) Fazn: zem: k

B>0; 5= fazu: zemik

Be-Elsin when to swish)

= $e^{-\frac{5}{2}-1}$ (Brind cos(w)) +Bcos wt sind)

B= \(\int_{\beta^2+B}^2\)

B1=B5:105 Bz=Bcast

B2 = B2+B3

 $t \wedge n \delta = \frac{B_1}{B_2}$

Primer:

$$S = \frac{1}{2}$$

$$y'(t) = Be^{-\frac{C}{2}t} \sin(\omega t + \frac{1}{2}) = \sin(\omega t) \cos(\frac{1}{2} + \cos(\omega t))$$

$$\sin(\frac{1}{2}t)$$

$$\dot{y}' + (3\dot{y}) + (3\dot{y}) + (3\dot{y}) = 0$$

y=y-yo, odnik dorenovjeke veneti v ravnovesni Lodnik od konca nedorenovje ne veneti

$$\omega_0^2 = \frac{k}{m} (70)$$

$$\beta \ll C \ll 4$$

$$K_{\text{soratmerns}}$$

Nastavel y = Ae >t

$$\Rightarrow \lambda^2 + \beta \lambda + \omega_0^2 = 0$$

$$D = (5^2 - 4)\omega_0^2 = -4\omega^2 \quad \omega_-^2 \omega_0^2 - (\frac{5}{2})^2$$

a)
$$P < 0 \Rightarrow (\omega^2 > 0)$$

 $y' = Be^{-\frac{C}{2}t} \sin(\omega^{\dagger} + \delta)$; $\omega = \sqrt{\omega^2 = \frac{C}{2}} = \sqrt{\omega_0^2 - (\frac{B}{2})^2}$

Zelo sibko duženje
$$\left(\frac{3}{2}\right)^2 << w_0 \Rightarrow$$

$$t_0 = \frac{21}{\sqrt{w_0^2}} = 21 \sqrt{\frac{m}{k}}$$

$$ky_0 = -mg_0$$

$$k = -\frac{mg_0}{y_0} \Rightarrow \frac{m}{k} = -\frac{y_0}{g_0}$$

$$\frac{m}{k} = \frac{0.4m}{10 \, \text{m/s}^2} = 0.04 \, \text{s}^2 =$$

Mundani - - Harry

=> % = 271.02s ≥ 1,2s

 $\sqrt{\frac{m}{L}} = 2.10^{-1} = 0.2 \text{ s}$

B in
$$\overline{d}$$
 debine is sately possible $y^2 = Be^{-\frac{B^2}{2}t}$ sin $(wt+\overline{d})$

$$\dot{y}' = -\frac{6}{2}Be^{-\frac{C}{2}t}sim(\omega t + \delta) + \omega Be^{\frac{C}{2}t}cos(\omega t + \delta)$$

$$\dot{y}'(0) = -\frac{6}{2}Bsin\delta + \omega Bcos\delta = \frac{1}{2}Bsin\delta + \frac{1}{2}Bsin\delta$$

$$y'(0) = \frac{1}{2} \frac{15 \sin \theta + 4 \cos \theta}{15 \sin \theta}$$

$$y'(0) = \frac{1}{2} \frac{1}{2} \sin \theta + 4 \cos \theta$$

$$y'(0) = \frac{1}{2} \sin \theta + 4 \cos \theta$$

$$r = \frac{y'(0)}{\dot{y}'(0)} = \frac{\sin \delta}{\omega \cos \delta - \frac{3}{2} \sin \delta} = \frac{\tan \delta}{\omega - \frac{3}{2} \tan \delta}$$

$$\Rightarrow \int = \arctan\left(\frac{rw}{1+\frac{rw}{2}}\right)$$

$$\Rightarrow \delta = \arctan\left(\frac{r\omega}{1+r\omega}\right)$$

$$\Rightarrow B = \frac{y'(c)}{\sin \sigma}$$

$$\dot{y}'(c) = B\omega\sin \sigma$$

$$\dot{y}'(o) = \mathcal{B}\omega \sin \delta$$

$$\Rightarrow \mathcal{B} = \frac{\dot{y}'(o)}{\pm \omega} = \frac{|\dot{y}'(o)|}{\omega}$$

$$W_{k} = \frac{1}{2} k y^{2} = \frac{1}{2} k (y) + y_{0})^{2}$$

$$y' = B \sin(w_0 t + J)$$

 $y' = w_0 B \cos(w_0 t + J)$

$$W_{K} = \frac{1}{2} m \omega_{o}^{2} B^{2} \cos^{2}(\omega_{o} + \delta) =$$

$$W_{pr} = \frac{1}{2} k B^2 \sin^2(w_0 + \tau_0) + \frac{1}{2} k y_0^2 + k y_0 B \sin(w_0 + \tau_0)$$

$$W_{pr} = M_0 \cdot B \sin(w_0 + \tau_0) + M_0 \cdot y_0$$

$$W = \frac{1}{2} k B^{2} (\sin(\omega_{0} + \delta) + \cos^{2}(\omega_{0} +$$

$$\lambda_{4,2} = -\frac{15 \pm \sqrt{D}}{2} = -\frac{3}{2}$$

$$\frac{12}{2} = \frac{1}{2}$$

(DN)

$$y_2$$
 = Bzte $\frac{3}{2}$ jetud resiter

$$\Rightarrow y' = y_1' + y_2' = (B_a + B_f) e^{-\frac{A_a}{2}}$$

20.2



$$F = F_8 + F_0 = ma$$

$$F_8 = -mg_0 \in \mathcal{F}$$

$$F_{g} = -mg_{o}\hat{e}_{r}$$

$$F_{v} = -F_{v}\hat{e}_{r}$$

$$\vec{r} = \hat{f}_{r}\hat{e}_{r}$$

$$\vec{r} = \hat{f}_{r}\hat{e}_{r}$$

$$\vec{r} \times \vec{F} = \hat{f}_{r} \times (-mg_{o}\hat{e}_{r}^{*} - F_{v}\hat{e}_{r}^{*}) =$$

$$ml(I\Phi + g_0 \sin \Phi)e$$

$$-l\Phi = g_0 \sin \Phi$$

$$-\tilde{\Phi} + \frac{g_0}{e} \sin \Phi = 0$$

 $\dot{\overline{\Phi}} + \omega_o^2 \Phi = 0$

F= l.er

$$\mathcal{Z} \stackrel{\bullet}{\mathcal{D}} + \frac{90}{7} \Phi = 0$$

dz... vstrajnedni
moment ze vrtenje
oksog fikane osi

primer: palico
$$Jz = \frac{1}{3}ml^2 \quad J' = \frac{l}{2}$$

$$sm \Phi \approx \Phi$$

$$7 \dot{E} + \omega^2 \dot{I} = 0$$

$$\omega_0^2 = \frac{m3\ell^*}{Jz} = \frac{3m9\ell}{2mm\ell^2} = \frac{3}{2} \frac{9}{2mm\ell^2}$$
N; ho, the lo:
$$Jz = m\ell^2 / l^* = l$$

 $u_0 := \frac{m}{m l^2} = \frac{30}{p}$

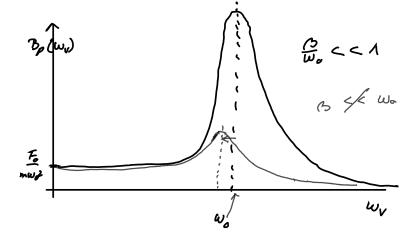
21.2 Nism & shkele

F= Fo Sin (
$$\omega_{v}$$
+) $\omega_{v} = 2\pi V_{v}$
 $\ddot{y} + (p\dot{y}) + \omega^{2}\dot{y} = \frac{F_{0}}{m} \sin(\omega_{v}+)$
 $\omega_{0}^{2} = \frac{k}{m}$ $C_{0} = \frac{C}{m}$
 $y^{2} = y - y_{0}$
 $y = 0 \text{ obtain.}$
 $y = y_{0} + y_{0}^{2} = 0 \text{ obtain.}$
 $y = y_{0} + y_{0}^{2} = 0 \text{ obtain.}$
 $y = x_{0} + y_{0}^{2} = 0 \text{ obtain.}$
 $y = B \sin(\omega t - S_{p})$
 $B_{p} \left\{ (\omega_{0}^{2} - \omega_{v}^{2}) \left[\cos S_{p} \sin(\omega_{v} t) - \sin S_{p} \sin(\omega_{v} t) \right] \right\}$
 $= \frac{F_{0}}{m} \sin(\omega t) + 1 \text{ obtains.}$
 $= \frac{F_{0}}{m} \sin(\omega t) + 1 \text{ obtains$

b) $t_2 = \frac{\pi}{2\omega_V} \implies \omega_V t_2 = \frac{\pi}{2} \implies \sin(\omega_V t) = 1$ $\cos(\omega_V t) = 0$ $B_P \frac{5}{2} (\omega_0^2 - \omega_V^2) \cos \delta_P + \omega_V \cos \delta_P \frac{5}{2} = \frac{F_0}{m}$ $B_P \frac{5}{2} \frac{(\omega_0^2 - \omega_V^2)^2 + \omega_V^2 \beta^2}{\sqrt{(\omega_0^2 - \omega_V^2)^2 + \omega_V^2 \beta^2}} \frac{1}{\sqrt{2}} = \frac{F_0}{m}$ $\Rightarrow B_P = \frac{F_0}{m} \cdot \frac{1}{\sqrt{(\omega_0^2 - \omega_V^2)^2 + \omega_V^2 \beta^2}}$ $\omega_V \implies 0 \implies B_P \implies \frac{F_0}{m} \cdot \frac{1}{\omega_0^2} = \frac{F_0 \cdot m}{m!k} = \frac{F_0}{k}$

 $\omega_{\nu} \longrightarrow \infty \Rightarrow \mathcal{B}_{\rho} \longrightarrow 0$ $\mathcal{B}_{\rho}(\omega_{\nu}) = \max$

Kdaj doseter makeimem? Torg holaje v resonanci? Ke je menavalec nejmanjs; $(w_{\nu}^{2} - w_{\nu}^{2})^{2} + (b_{\nu}^{2})^{2}$ je najmenjer) $\frac{d}{dw}\left(\left(\omega_0^2 - \omega_v^2\right)^2 + \beta \omega_v^2\right) = 0$ 2 (wo2 - wv) (-2wv) + 2wv/52 =0 -2(w,2-w)+B2=0 $\omega_{\nu}^{2} = \omega_{o}^{2} - \frac{G^{2}}{2}$ $\omega_{\nu} = + \sqrt{\omega_o^2 - \frac{B^2}{2}} = \omega_o \sqrt{1 - \frac{B^2}{2\omega_o^2}}$



Sklapljeno mhanje · (s -> 0 dusanje postjema grati 0 · Za zacetek: Simetrion; primer k3=k4 [m] 0, 7 ×2 02 "z drug vametjo, k.j; bomorch! tetja vzmet Frank ... Sile y we went ne pru; vozicek to je v raun avesni legi $\overline{F}_{n \to n, r} = -k_1 O \ell_{n, r} \hat{e}_x$ } + = 0 == 1,r = + k20/2,rêx Fz->2,r = -kz 0 lz,r êx F3 -> 4, r = + K1 & l3, rex Fron = Front - Kaxic Fz-1= == == - k(x1-x2) &x Fz->2 = F2->2, + k2 (×1-×2) êx F3-72 = F3-72,4-K1 x2 êx Find + Fina = mxiêx F1-11,1 - k1x1 &x + F2-51, - k(x1-x2) ex = = mxiêr $m\dot{x}_1 + k_1 \times 1 + k_2(x_1 - x_2) = 0$ ×1+ W1 ×1+W2 (×1-×2)=0 $\omega_1 = \frac{\kappa_1}{m} \qquad \omega_2^2 = \frac{k_2}{m}$ Zelo podeon x2 + w2x2 - w2 (x1-x2) = $X_{\alpha} = X_{\alpha} + X_{2}$ $X_{b} = X_{n} - X_{2}$ $X_{b} = X_{n} - X_{2}$ $X_{b} = X_{n} - X_{2}$ $X_{b} = X_{n} - X_{2}$ XL= Xe-Xb se Sejeno madi x1+ x2 + W1 x1 + W1 x2 = 0 $(x_1+x_2) + \omega_1^2(x_1+x_2) = 0$ × +ω 2× = 0 $\omega_b = \sqrt{\omega_{\lambda}^2 + 2\omega_z^2}$ Xb + Wb Xb = 0 $X_a = B_a sin(\omega_a t + J_a)$ Xb = Ba sin (wot + J.) => x1= Ba sin(wat + Ja) + Bb sin (wat + Jb 72- Bisin(wat+ Ja) - Bz sin (wat + Jb) B, B2, 5, 56 =? Ze = = n; p= q= ;: X1 (+=a) x1, (+=a) x2 (+=0) k2 (+=0) iz tes izuno

Pine

$$\begin{array}{lll} \chi_{A}(f=o)=\chi_{O} & (70) & \chi_{I}(f=o)=0 \\ \chi_{I}(f=o)=0 & \chi_{I}(f=o)=0 \\ \chi_{I}=B_{A} & \omega_{A} & \cos(\omega_{A}f+\delta_{A})+B_{I}w_{A} & \cos(\omega_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \omega_{A} & \cos(\omega_{A}f+\delta_{A})+B_{I}w_{A} & \cos(\omega_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \omega_{A} & \cos(\omega_{A}f+\delta_{A})-B_{I}w_{A} & \cos(\omega_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \omega_{A} & \cos(\omega_{A}f+\delta_{A})-B_{I}w_{A} & \cos(\omega_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \sin(\Delta_{A}f+\delta_{A})+B_{I}w_{A} & \cos(\omega_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \sin(\Delta_{A}f+\delta_{A})+B_{I}w_{A} & \cos(\delta_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \omega_{A} & \cos(\delta_{A}f+\delta_{A})+B_{I}w_{A} & \cos(\delta_{A}f+\delta_{A}) \\ \chi_{I}=B_{A} & \omega_{A} & \cos(\delta_{A}f+\delta_{A}$$

$$2B_1 w_a \cos \delta_a = 0 \implies \cos \delta_a = 0$$

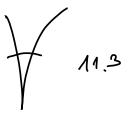
$$\sum_{b_1 = B_2 = \frac{x_0}{2}} = \sum_{b_2 = +\frac{\pi}{2}} \sum_{b_3 = +\frac{\pi}{2}} \sum_{b_4 = +\frac{\pi}{2}} \sum_{b_4$$

7.3
mentalger
adsolver

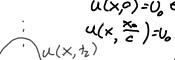
lastre nihanja sestauliences utrela

$$\dot{x}_{1}^{2} + \omega_{1}^{2} x_{1} + \omega_{2}^{2} (x_{1} - x_{2}) = 0$$

$$\dot{x}_{2}^{2} + \omega_{2}^{2} x_{2} - \omega_{2}^{2} (x_{1} - x_{2}) = 0$$



ene timed motions:
$$u(x,t) = f(x-ct)$$



$$\Rightarrow V = \left| \frac{du}{dt} \right| = \left| \frac{\partial u}{\partial t} \right| = \left| \frac{\partial}{\partial t} f(x - ct) \right| = |f|/c$$

∨ ≠c

a)
$$u(x,t) = u(x-ct, o)$$

$$x \rightarrow x' = x-ct$$

$$t \rightarrow t' = o$$

$$u(x',t') = u(x-ct, o) = f(x', ct') = f(x-ct) = f(x,t')$$

$$= u(x,t')$$

ce pernemo u(x, f) ob cesutio 2 4x)

The pername
$$u(x,f)$$
 ob Easy $t = 3 \forall x^{3}$

Potent porum $u(x,t) \ge \forall x \neq 0$
 $u(x,t) = u(0,t-\frac{x}{c})$
 $u(x,t) = -\frac{x}{c}$
 $u(x,t) = u(0,t-\frac{x}{c}) = u(x,t)$
 $u(x,t) = u(0,t-\frac{x}{c}) = u(x,t)$

a potentu(x'=o,t) de t' =poznam u(x,t) ze Vx, Vt

Potujoče sinusno valovanje

$$u(x,t) = f(x-ct)$$

 $u(x=0, t-\frac{x}{c}) = u_0 \sin(-\omega t + \delta);$ $u_0 > 0$
 $u(x,t) = \frac{x}{c}$

$$u(x,t) = u(o,t-\frac{x}{c}) = u_0 \sin(-\omega(t-\frac{x}{c})+\delta) =$$

$$= u_0 \sin(kx-\omega t+\delta) ; k = \frac{\omega}{c} = \frac{2\pi V}{c}$$

$$[k] = \frac{1}{m}$$

8=0
$$\frac{1}{2k} \qquad \frac{31}{k} \times \frac{21}{k}$$

$$u(x, t=0) = u_0 S; n(kx)$$

Valovanje v obe smer;

C= AV

 $\lambda = \frac{2\pi}{k} = \frac{2\pi c}{2\pi V} = \frac{c}{V}$

a) tog vpeta vzmet
$$u(x_1,t) = u(x_2,t) = 0$$

a) tog upeta vzmet

$$u(x_1,t) = u(x_2,t) = 0$$

b) Vzmet (palice) 3 prostima kon

$$u(x_1,t) = u(x_2,t) = 0$$

b) Vznet (police) 3 prostima kon

Model:

 $u(x_2-h,t)$
 h
 $u(x_2,t)$
 h
 h
 h

b) Vznet (palice) 3 prostima koncema,
$$x_1, x_2$$

monnimm Fx2-h >x2=-k, 0 h

0 =×z

 $\frac{m}{lh} \frac{\delta^2 u(x_e t)}{\delta t^2} = -k l \left(\frac{u((x_z) + h)t) - u(x^2, t)}{h} \right)$

X = 1

n-00 € h-0 => hii ->0

 $\frac{\partial x}{\partial r(x,t)} \Big|_{x=0}^{x_{s}-\mu} \frac{\partial x}{\partial r(x,t)} \Big|_{x=0}^{x_{s}}$

 $m_A \ddot{\iota} (x_z,t) = -k l \left(\frac{u(x_z +) - u(x_z - h, t)}{h} \right)$

m, = m lh son vseh wee'

 $x_z = x_z + h$

 $\frac{\partial u(x,t)}{\partial x}\Big| = \frac{\partial u(x,t)}{\partial x}\Big|$

 $0 = x_z - h$

h'-h = u(xz)-u(xzh)

 $= -\frac{k\ell}{h} (u(x_2,t) - u(x_2-h,t))$

tog vpeta vzmet
$$u(x_1,t) = u(x_2,t) = 0$$

$$\frac{\partial \alpha}{\partial x} \Big|_{x=0} = \frac{\partial \alpha}{\partial x} \Big|_{x=L} = 0 \text{ zelft}$$

$$\text{Addinapolae}$$

$$u(x,t) = u_n(x,t) + u_2(x,t)$$

$$u_n = \sin \alpha (kx - \omega t + \delta_n)$$

$$u_2 = u_n(x,t) + \cos \alpha (kx - \omega t + \delta_n)$$

$$U_{n} = Sin \circ (kx - \omega t + \delta_{n})$$

$$U_{2} = U_{0} \sin (kx + \omega t + \delta_{2})$$

$$= 2U_{0} \sin (kx + \delta_{1} + \delta_{2}) \cos(-\omega t + \frac{\partial 1 + \partial_{2}}{2})$$

 $\Rightarrow \frac{\delta_4 + \delta_2}{3} = \frac{\pi}{3}$

 $\frac{du}{dx} = 0 \implies$

 $cos(kx + \frac{\pi}{2}) = -sin(kx)$

 $u(x,1) = 2u_0 cos(kx) cos(-\omega t + \frac{\sigma_1 - \sigma_2}{z})$

-2kuosin(kl)cosl-w1 + $\frac{\delta_1 - \partial z}{z}$) = 0

 $u(x,t) = 2u_0 \cos\left(\frac{n\pi}{L}x\right) \cos\left(-2\pi\nu n + \frac{d-d\tau}{2}\right)$

Dobimo stoječe valovanje. nima več tner:

du =- 2k uo s; n (kx) coscut + 51-52)

KL= 0+11n, nez

 $k = \frac{n\pi}{L} = \frac{\omega}{2\pi} = \frac{2\pi v_n}{2\pi}$

Un= nc new

 $Sin(kx+\frac{1}{2})=cos(kx)$

 $\frac{\partial u}{\partial x} = \frac{\partial u_n}{\partial x} + \frac{\partial u_2}{\partial x} = \frac{k u_0 \cos(kx - wt + d_n)}{+ k u_0 \cos(kx + wt + d_2)}$

= 2k uo cos (kx+ d+d2) cos (-w+ d+ d+ de)

 $\frac{\partial u}{\partial x}$ = 2k vo cos $\left(\frac{\delta_1 + \delta_2}{z}\right)$ cos $\left(-\omega + \frac{\delta_3 - \delta_2}{z}\right)$

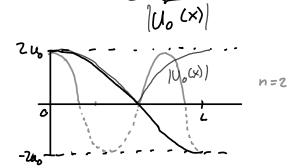
7+



$$n=0 \Rightarrow u(x,t)=2u_0 \cos\left(\frac{\delta_n-\delta_z}{z}\right)$$

$$n=1 \rightarrow V_{n} = \frac{c}{2c}$$

$$u(x,t) = 2u_{0} ccs \left(\frac{\pi}{a} x\right) ccs \left(\frac{\pi c}{c} + \frac{\delta_{n} - \delta_{z}}{2}\right)$$



$$V_{\Lambda} = \frac{c}{2L} = \frac{1}{2L} \sqrt{\frac{E}{3}} \longrightarrow E$$

$$\rho = \frac{m}{V} = \frac{m}{LS}$$

10 Energia valovanja

· potovanje motnyse -> potovanje unergije

· valovanje po vijaon; vzmeti

$$W_{k} = \frac{1}{2} m_{A} \cdot V^{2} = \frac{1}{2} m_{A} \left| \frac{\partial u(x,t)}{\partial t} \right|^{2} = \frac{1}{2} \frac{mh}{k!} \left| \frac{\partial u(x,t)}{\partial t} \right|^{2}$$

$$\Rightarrow \frac{W_R}{h} = \frac{1}{2} \frac{m}{\ell} \left| \frac{\partial u(x,t)^2}{\partial t} \right|^2$$

$$u(x,t) = \frac{1}{2} \left[\frac{\partial u(x,t)}{\partial t} \right]^2$$

$$W_{pr} = \frac{1}{2}k_{1}\left[u(x+h,t) - u(x,t)\right] =$$

$$= \frac{1}{2}\frac{k_{1}!}{h!}\left[u(x+h,t) - u(x,t)\right] =$$

$$= \frac{1}{2} k lh \left(\frac{u(x+h,t) - u(x,t)}{h} \right)^{2} =$$

$$\frac{W_{pr}}{h} = \frac{1}{2} k l \left[\frac{u (x+n,t) - u (x,t)}{h} \right]^{2}$$

$$|\int_{h\to 0}^{h\to 0} \frac{W_{p'}}{h} = \frac{1}{2}kl \left| \frac{\partial u(x,t)}{\partial x} \right|^2 = \frac{1}{2}kl \left| \frac$$

$$-\frac{1}{2}kl\frac{l}{m}\frac{m}{l}\left|\frac{\partial u(x,t)}{\partial x}\right|^{2} =$$

$$=\frac{1}{2}c^{2}\frac{m}{l}\left|\frac{\partial u(x,t)}{\partial x}\right|^{2}$$

$$=\frac{l}{2}kl\frac{l}{m}$$

$$=\frac{l}{2}kl\frac{l}{m}$$

Prothe palica

$$m = \rho v = \rho s. V^{2} \Rightarrow \frac{W_{K}}{h} (x,t) = \frac{ES}{h}$$

$$\frac{1}{Z} \rho S \left| \frac{\partial u}{\partial t} \right|^{2}$$

$$W_{K} = \frac{W_{K}}{\partial V} = \frac{W_{K}}{SQ} = \frac{1}{Z} \rho \left| \frac{\partial u}{\partial t} \right|^{2}$$

$$golota kinetiene energive$$

$$\overline{W} = \frac{1}{2} P \omega^2 U_0^2 \dots porprene gestoteenergije $\omega = 2\pi V$$$

oneraja, hi v casu t prepatuje shoz; S

$$P := \frac{\overline{W}}{t} = \frac{\overline{w} \cdot Sct}{t} = \overline{w} \cdot Sc$$

$$[P] = \frac{J}{m^3} \frac{m^2 \cdot m}{s} = \frac{J}{s} = W \dots \text{ and}$$

$$j_w := \frac{P}{g}$$
 ... jakest energijstege take

$$j_w = \frac{p}{s} = \overline{w}c$$
 $[j_w] = \frac{W}{m^2}$

Primer:

200k v zraku

$$e^2 = \frac{1}{x}p$$

sholjivost

PV= MRT

$$\chi := -\frac{1}{V} \frac{\partial V}{\partial \rho}$$

$$\frac{P^V}{T} = \frac{P^{0}V^{0}}{T_{0}}$$

T=To=konst (izoterman)
$$pV=p.V_0=K$$

$$\Rightarrow V=\frac{K}{p} \Rightarrow \frac{1}{V}=\frac{P}{K}$$

$$\frac{1}{2} V = \frac{K}{p} \Rightarrow \frac{1}{\sqrt{1 - \frac{K}{p}}} = \frac{P}{K}$$

$$\chi = (-\frac{1}{V})(-\frac{K}{p}) = \frac{1}{p}$$

$$\chi = \frac{1}{p} \Rightarrow \frac{1}{K_p}$$

[t]=K

$$\chi = \frac{1}{p} \longrightarrow \frac{1}{K_p}$$

$$K P R T$$

$$\chi = \frac{1}{p} \longrightarrow \frac{1}{K_p}$$

$$c^2 = \frac{K p RT}{pM} = \frac{KRT}{M}$$

$$K = 1, k$$
 The vise disastowne molekule
$$C = \sqrt{\frac{KRT}{H}} = \sqrt{\frac{1, k \cdot 8300 \, J \cdot 300 \, K}{K}} \approx 340$$

$$\Rightarrow c = \sqrt{\frac{\kappa RT}{H}} = \sqrt{\frac{1.4.8300 \text{ J.} 300 \text{ K}}{\kappa}} \approx 340 \text{ m/s}$$

$$\text{Nook} = 1 \text{ kHz} \dots \text{ nese uho jo nejbodj}$$

$$\text{ob autijive a to}$$

$$\text{jo = 10}^{-12} \text{ W} \dots \text{ tolke She jokent jk}$$

$$\text{of toke, de distree}$$

$$\text{Vo = 2}$$

jo= 1 PW20,2.c for 1,2 kg. => u02 = 2jo PRπ Vnax)2 c

c: hitrost woke v snovi (zraku)

V': frewenca, ki jo sto sprejemnih

1=0 odda prvi pisk

tz=to odda drugi pisk

priblizije z vz

t,' = 1

 $V^{2} = V \frac{1 \pm \frac{\sqrt{2}}{c}}{1 \mp \frac{\sqrt{4}}{c}}$

t,=0

た=ナー

(glede na trah)

x=cto-4to = to (C-4)

b) oddejnik miruje (va=0), sprejemnik se

Po zraku proti sprejeminiku potujejo

 $c_{o}t_{o}' + v_{e}t_{o}' = \lambda = \frac{c}{y}$ $t_{o}'(c_{o} + v_{e}) = \frac{c}{y}$

 $\frac{C_0+V_2}{V^1}=\frac{C}{V}$

valori z valorno dolzino >

 $\frac{1}{12} = \gamma^{\prime}$

 $V^1 = V \cdot \frac{C + \sqrt{c}}{c} = V \left(1 + \frac{\sqrt{c}}{c}\right)$

oddejnik se mu priblizuje s hitrostjo Va

a) sprejemnik miruje glede na zrak (Vz=0),

pri km se prematne za to va proti sprojemmiku prvo celo se pemekne za to c proti spejanink

- za približevanje + za oddaljevanje

n: valorne dotine woke v snovi (zraku)

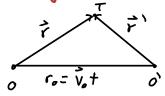
V: frewence oddajn:ka ($t_0 = \frac{1}{V}$

Predpostance:

T1: UpIN okolice upade z razdeljo

lim F=0 dmin=00 K slurpne sile obdice K nejmanjše vezdelje obdice do predmete Primer: Fg.

Galilejeve transformaciji



$$S: \vec{V} = \frac{d\vec{r}}{dt}$$

$$S': \vec{V}' = \frac{d\vec{r}'}{dt} = \frac{d\vec{r}'}{dt} = \frac{d}{dt} \left((-r_o) = \frac{dr}{dt} - \frac{d(v_o + t)}{dt} \right)$$

$$S: \vec{a} = \frac{dv}{dt} = v - v_0$$

$$S: \vec{a}' = \frac{dv}{dt} = \frac{dv}{dt} = \frac{d}{dt} / v_0 + \frac{d}{dt} = \frac{dv}{dt} / v_0 + \frac{d}{dt} = \frac{dv}{dt} = \frac{dv}{dt} / v_0 + \frac{dv}{dt} = \frac{dv}{dt} = \frac{dv}{dt} = \frac{dv}{dt} / v_0 + \frac{dv}{dt} = \frac{dv}{dt} =$$

S': à' =
$$\frac{dv'}{dt'} = \frac{dv}{dt} = \frac{dv}{dt} (v-v_o) = \frac{dv}{dt} - \frac{dv_o}{dt} = \frac{dv_o}{dt}$$

$$\dot{\vec{r}} = x e_{x} + y e_{y} + z e_{z} \left[\frac{\dot{x}}{\dot{x}} \right]$$

$$\dot{\vec{r}}' = x' e_{x}' + y e_{y} + z' e_{z}' = x' e_{x}' + y e_{y}' + z e_{z}' = \left[\frac{\dot{x}}{\dot{x}} \right]'$$

$$x = x - \frac{v_0}{c_0} \quad c_0 \neq = x - p_0 c_0 \neq 0$$

@ Elektrion sila

(Kolombor zekon)

3. Elektricho paje

ディア)....·sile

È ... vektor. el. polja oz jakast. el. polja

2 ... rebo)

Fel, 2 = g. E = Fel 2

 $\vec{E}_{e'(\vec{r}')} = \frac{\vec{F}_{e'\to e}}{g} = \frac{2^{1}(\vec{r}-\vec{r}')}{u\pi\epsilon. |\vec{r}-\vec{r}'|^{2}}$

[= 1 = A52 V mm - VAS = N

[E] _ ¥

Y 27.3 odsome zedných no minut

$$2^{\frac{1}{2}} - \frac{1}{2^{\frac{1}{2}}}$$
 $3^{\frac{1}{2}} = 3$
 $3^{\frac{1}{2}} = 3$
 $3^{\frac{1}{2}} = -2$
 $3^{\frac{1}{2}} = -2$
 $3^{\frac{1}{2}} = -2$
 $3^{\frac{1}{2}} = -2$
 $3^{\frac{1}{2}} = -2$

$$\vec{E}(\vec{r}) = \vec{E}_1 + \vec{E}_2$$

$$\vec{E}_1 = \vec{Q}_1 \quad (\vec{r} - \vec{r}_1)$$

$$\vec{E}_{n} = \frac{3^{2}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{n})}{(\vec{r} - \vec{r}_{n})^{3}} = \frac{3\vec{r}}{4\pi\epsilon_{0}} \frac{3\vec{r}}{(\vec{r} - \vec{r}_{n})^{3}}$$

$$\vec{E}_{n} = \frac{3^{2}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{n})}{(\vec{r} - \vec{r}_{n})^{3}} = \frac{3\vec{r}}{4\pi\epsilon_{0}} \frac{3\vec{r}}{(\vec{r} - \vec{r}_{n})^{3}} = \frac{3\vec{r}}{(\vec{r} - \vec{r}_{n})^{3}} = \frac{3\vec{r}}{(\vec{r} - \vec{r}_{n})^{3}} = \frac{3\vec{r$$

$$E_{2} = \frac{3^{\circ}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{1})^{3}}{4\pi\epsilon_{0}} = \frac{3^{\circ}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} = -\frac{3^{\circ}(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} = -\frac{3^{\circ}(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} = -\frac{3^{\circ}(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} = -\frac{3^{\circ}(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} = -\frac{3^{\circ}(\vec{r} - \vec{r}_{2})^{3}}{4\pi\epsilon_{0}} \frac{(\vec{r} - \vec{r}_{2}$$

$$E = \frac{1}{4\pi \epsilon_r^3} \left(3p_e \cdot \hat{e}_r \right) \hat{e}_r - p\hat{e}_r^3$$

$$\hat{e}_r = \frac{\vec{r}}{r} \quad \vec{p}_e := 2\vec{k}$$

$$\hat{e}_r = \hat{r}$$
 $\hat{p}_e := 2\hat{z}$

$$2i \rightarrow 52$$
: $Fd_1 2z = g_1 \vec{E}(\vec{r_2}) = -g \vec{E}$

$$\vec{r_1} - \vec{r_2} = r_d \quad (od near, do poz.)$$

$$\vec{r_1} = 2a = g$$

E ne simetali erakemerne nelik zanke

$$\vec{r} = r\hat{e}_{x}$$

$$\vec{r}' = r^{2}\cos p \, e_{y} + r^{2}\sin p \, e_{z}$$

$$\vec{r}' = r^{2}\sin p \, e_{z}^{2}$$

$$|\vec{r}' - \vec{r}'|^{3} = (r^{3} + r^{4})^{\frac{3}{2}}$$

$$|\vec{r} - \vec{r}|^3 = (r_3 + r_5)^{\frac{3}{2}}$$

$$|\vec{r} - \vec{r}|^3 = (r_3 + r_5)^{\frac{3}{2}}$$

$$|\vec{r} - \vec{r}|^3 = (r_3 + r_5)^{\frac{3}{2}}$$

$$= \frac{p_{g}r'(r\ddot{e}_{x} - rcoste_{y} - rsn_{p}\ddot{e}_{z})dp}{u\pi\varepsilon_{o}(r^{2}+r^{12})^{3}\varepsilon}$$

$$\Rightarrow \vec{E}(\vec{r}) = \int LE_{p} = \frac{p_{g}r'}{u\pi\varepsilon_{o}} \frac{[r\dot{e}_{x}I_{x} - r'\dot{e}_{y}I_{z} - r\dot{e}_{z}^{2}I_{3}]}{(r^{2}+r^{12})^{3}\varepsilon}$$

$$df_{1} = g_{1} r^{2} dp$$

$$df_{2} = g_{2} r^{2} dp$$

$$df_{3} = \frac{dg^{2}}{4\pi e_{0}} \frac{(\vec{r} \cdot \vec{r})}{(\vec{r}^{2} \cdot \vec{r})^{2}} =$$

$$= g_{1} r^{2} (re^{2}_{x} - rcospe_{y} - rsonpe_{z}) dp$$

$$u\pi E_{0} (r^{2} + r^{2})^{3} =$$

$$\Rightarrow \vec{E}(\vec{r}) = \int dE_{p} = \frac{f_{2} r^{2}}{4\pi E_{0}} \frac{[re^{2}_{x}I_{x} - r^{2}e_{y}I_{z} - re^{2}_{z}]}{(r^{2} + r^{2})^{3} =}$$

 $I_{\lambda} = \int d\rho = 21$ $I_{z} = \int_{cop}^{2\pi} d\rho = 0$ $I_3 = \int_{\text{sing}}^{2\pi} d\phi = 0$

Ne viden netable oznake so the mage se pravile
$$S = \Pi R^2$$

$$S = \frac{3}{11} = \frac{3}{11}$$

$$18' = 2\Pi r' 2r'$$
(povisine zunke)

$$P_{s'} = -\frac{ds'}{ds'} \Rightarrow dg' = P_{s'} ds' = \frac{2}{\Pi R^2} 2\Pi r' dr' = \frac{3}{R^2}$$

$$= \frac{3}{R^2} 2r' dr' = \frac{2}{R^2} \frac{2$$

$$\frac{3^{2}r^{2}Ar}{24 \epsilon_{0} (r^{2}+r^{12})^{\frac{3}{2}} e^{2x}} \stackrel{?}{\epsilon_{0}} \times \stackrel{?}{\epsilon_{0}} \stackrel{?}{\epsilon_{0}} = \frac{3^{2}r^{2}}{24 \epsilon_{0} R^{2}} \stackrel{?}{\epsilon_{0}} \times \stackrel{?}{\underline{I}}$$

$$\stackrel{?}{\underline{I}} = \int \frac{r^{2}Ar}{24 \epsilon_{0} R^{2}} e^{2x} \stackrel{?}{\underline{I}} = \frac{4}{r^{2}}$$

$$\frac{3^{1}r^{2}dr}{2\pi E_{0}(r^{2}+r^{12})^{\frac{3}{2}}} \hat{e}_{x}$$

$$\hat{E}(\hat{r}) = \frac{3^{1}r}{2\pi E_{0}R^{2}} \hat{e}_{x} \hat{I}$$

$$\hat{I} = \int_{0}^{R} \frac{r^{2}dr^{2}}{(r^{2}+r^{2})^{\frac{3}{2}}} = \frac{1}{r}(1)$$

$$\vec{E}(\vec{r}) = \frac{3^{1}r}{2\pi E R^{2}} \hat{e}_{x} \vec{I}$$

$$\vec{E}(\vec{r}) = \frac{3^{1}r}{2\pi E R^{2}} \hat{e}_{x} \vec{I}$$

$$\vec{E}(\vec{r}) = \frac{2^{1}}{\pi r^{2}} \frac{1}{3E_{0}} \cdot (1 - \frac{1}{\sqrt{4}})$$

$$\vec{E}(\vec{r}) = \frac{2^{1}}{\pi r^{2}} \frac{1}{3E_{0}} \cdot (1 - \frac{1}{\sqrt{4}})$$

$$\vec{E}(\vec{r}) = \frac{3^{1}r}{2\pi E R^{2}} \hat{e}_{x} \vec{I}$$

$$\vec{I} = \int_{a}^{a} \frac{r^{2}dr^{2}}{(r^{2}+r^{2})^{\frac{3}{2}}} = \frac{1}{r} (1)$$

$$\vec{E}(\vec{r}) = \frac{2^{1}}{11r^{2}} \frac{1}{3E_{a}} \cdot (1 - \frac{1}{\sqrt{1+R^{2}}})$$

$$= \frac{P_{a}}{2E_{a}} (1 - \sqrt{1+R^{2}})$$

$$\vec{E}(\vec{r}) = \frac{2^{3}r}{2\pi \epsilon R^{2}} \hat{e}_{x} \vec{I}$$

$$\vec{I} = \int_{0}^{R} \frac{r^{3}dr^{3}}{(r^{2}+r^{3})^{\frac{3}{2}}} = \frac{1}{r} (1)$$

$$\vec{E}(\vec{r}) = \frac{2^{3}}{11r^{2}} \frac{1}{3\epsilon_{0}}, (1 - \frac{1}{\sqrt{11}})$$

$$= \frac{\rho_{0}}{2\epsilon_{0}} (1 - \sqrt{11}) \frac{1}{\sqrt{11}}$$

$$\hat{I} = \int_{0}^{R} \frac{r' dr'}{(r^{2} + r'^{2})^{\frac{3}{2}}} = \frac{1}{r} \left(1 - \frac{1}{\sqrt{1 + \frac{R^{2}}{r^{2}}}} \right)$$

$$\hat{E}(\vec{r}) = \frac{2}{\Pi r^{2}} \frac{1}{3E_{0}}, \left(1 - \frac{1}{\sqrt{1 + \frac{R^{2}}{r^{2}}}} \right)$$

$$= \frac{\rho_{0}}{2E_{0}} \left(1 - \frac{1}{\sqrt{1 + \frac{R^{2}}{r^{2}}}} \right)$$

$$= \frac{r}{\sqrt{1 + \frac{R^{2}}{r^{2}}}}$$

$$I = \int_{0}^{\infty} \frac{r'dr'}{(r^{2}+r'^{2})^{\frac{3}{2}}} = \frac{1}{r} \left(1\right)$$

$$\stackrel{\stackrel{?}{=}}{E}(\stackrel{?}{r}) = \frac{2}{\Pi r^{2}} \frac{1}{3\epsilon_{o}} \cdot \left(1 - \frac{1}{\sqrt{1+\epsilon^{2}}}\right)$$

$$= \frac{\rho_{0}}{2\epsilon_{o}} \left(1 - \frac{1}{\sqrt{1+\epsilon^{2}}}\right)$$

$$\stackrel{r}{=} \frac{1}{r} \left(1 - \frac{1}{\sqrt{1+\epsilon^{2}}}\right)$$

$$\stackrel{r}{=} \frac{1}{r} \left(1 - \frac{1}{\sqrt{1+\epsilon^{2}}}\right)$$

是>>1

$$\vec{E}(\vec{r}) = \frac{2}{\Pi r^2} \frac{1}{3E_o} \cdot \left(1 - \frac{1}{\sqrt{1 + \frac{R^2}{r^2}}}\right)$$

$$= \frac{P_0}{2E_o} \left(1 - \frac{1}{\sqrt{1 + \frac{R^2}{r^2}}}\right)$$

$$= \frac{P_0}{R} \left(1 - \frac{1}{\sqrt{1 + \frac{R^2}{r^2}}}\right)$$

$$= \frac{P_0}{R} \left(1 - \frac{1}{\sqrt{1 + \frac{R^2}{r^2}}}\right)$$

$$= \frac{P_0}{R} \left(1 - \frac{1}{\sqrt{1 + \frac{R^2}{r^2}}}\right)$$

 $\vec{E}(r) \approx \frac{\vec{S}}{2E} \left[1 - \vec{F} \right] \approx \frac{\vec{P}_1}{2E}$

$$\frac{1}{+\frac{R^2}{r^2}}$$