Fourierova vista

$$FV(f)(x) = a_0 + \sum_{n=1}^{\infty} (a_n \cos(nx) + b_n \sin(nx))$$

$$\frac{a_0}{2} = n \text{ predavanjih}$$

$$a_0 = \frac{1}{2\pi} \int_{-\pi}^{\pi} f(x) dx$$

$$a_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) dx$$

$$b_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) dx$$

FV(f) konvergira k f, te je f everne $u \times x$, te pa n:, pa honvergira k $\frac{f(x^{-}) + f(x^{+})}{3}$

$$\int x \cos(nx) dx = \frac{x \sin(nx)}{n} + \frac{\cos(nx)}{n^2} + C$$

$$\int x \sin(nx) dx = \frac{x \cos(nx)}{n} + \frac{\sin(nx)}{n^2} + C$$

$$f$$
 sade $\Rightarrow b_n = 0$
 f l:ha $\Rightarrow a_n = 0$

$$\int X^{2} \cos(nx) dx = \frac{x^{2}}{n} \sin(nx) + \frac{2x}{n^{2}} \cos(nx) - \frac{2}{n^{3}} \sin(nx)$$

 $\int x^{2} \sin(nx) dx = \frac{-x^{2}}{n} \cos x + \frac{2x}{n^{2}} \sin(nx) + \frac{2}{n^{3}} \cos(nx)$

(2)

$$f(x) = |X|$$
 rawij v Fouriero vo vr sto m
sestej $1 + \frac{1}{3^2} + \frac{1}{5^2} + \frac{1}{7^2} + ...$

$$Q_0 = \frac{1}{2\Pi} \int_{-\pi}^{\pi} |X| dX = \frac{1}{\pi} \int_{0}^{\pi} X dX = \frac{1}{2\pi} \pi^2 = \frac{\pi}{2}$$

$$Q_{n} = \frac{1}{\pi} \int_{-\pi}^{\pi} |x| \cos(\ln x) dx = \frac{2}{\pi} \int_{-\pi}^{\pi} x \cos(\ln x) dx = \frac{2}{\pi} \int_{-\pi}^{\pi} x \cos(\ln x) dx = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \sin(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n^{2}} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{\cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{x \cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln x)}{n} + \frac{x \cos(\ln x)}{n} \right) = \frac{2}{\pi} \left(\frac{x \cos(\ln$$

$$= \frac{2}{\pi} \left(\frac{(-1)^n}{n^2} - \frac{1}{n^2} \right)$$

$$b_n = \frac{1}{\pi} \int |x| \sin(nx) = 0$$
|:host

$$FV(f)(x) = \sum_{n=0}^{\pi} + \sum_{n=0}^{\infty} \frac{2}{\pi} (\frac{(-1)^n - 1}{h^2}) \cos(nx) =$$

$$= \frac{\pi}{2} + \frac{2}{\pi} \sum_{K=0}^{\infty} \frac{-2}{(2k+1)^2} \cos((2k+1)K)$$

$$FV(f)(o) = \frac{1}{2} + \frac{-4}{11}, \sum_{k=0}^{\infty} \frac{1}{(2k+n)^2} = f(o) = 0$$

$$\sum_{k=0}^{1} \frac{1}{(2k+n)^2} = -\frac{11}{2} \cdot \frac{1}{(-4)} = \frac{11^2}{8}$$

Dodetno

$$\sum = 1 + \frac{1}{2^2} + \frac{1}{3^2} + \dots = ? S + \frac{1}{2^2} + \frac{1}{4^2} + \dots = ?$$

S... 1:4.
S'... ostalo
$$= S + \frac{1}{2^2} \left(1 + \frac{1}{2^2} + \frac{1}{3^2} + \dots \right) =$$

$$= S + \frac{1}{4} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j=1$$

$$S = \frac{3}{4} \sum_{n=1}^{\infty} \frac{\pi^{2}}{6}$$

$$\int OS = \max(cosx, 0)$$

$$S_A = \sum_{n=1}^{\infty} \frac{(-1)^n}{4n^2 - 1}$$

$$S_z = \sum_{n=1}^{\infty} \frac{1}{4n^2 - 1}$$

$$fOS = max(cosx, 0)$$

 $Q_n = \frac{1}{11} \int f(x) \cdot \cos(nx) dx = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}}$

 $= \frac{2}{\pi} \int_{0}^{\pi} f(x) \cos(nx) = \frac{2}{\pi} \int_{0}^{\pi} \cos(x) \cos(nx) + 2 \int_{0}^{\pi} \cos(x) \cos(x) + 2 \int_{0}^{\pi} \cos(x$

 $= \frac{2}{\pi} \int \frac{1}{2} (\cos((n+1)x) + \cos((n-1)x) = n + 1$

 $n = 4k : \frac{1}{\pi_{h+1}} \cdot 1 + \frac{1}{n-1} \cdot 2 \cdot \sqrt{\pi} = \frac{-2}{n^2 - 1} \cdot \frac{1}{\pi} \cdot \frac{-2}{16k^2 - 1} \cdot \frac{1}{\pi}$

 $\alpha_1 = \frac{1}{\pi} \int_{-\pi}^{\pi} \cos^2 x \, dx = \frac{2}{\pi} \int_{-\pi}^{\pi} \frac{1 + \cos^2 x}{2} \, dx = \frac{1}{\pi} + \sin^2 x \int_{-\pi}^{\pi} \frac{1}{2} \, dx$

 $FV(f)(x) = \frac{1}{\pi} + \frac{1}{2} cos(x) + \frac{2}{\pi} \sum_{m=1}^{\infty} \frac{(-1)^{m+1} \cdot 2}{(2m)^{2} \cdot 1} cos(2mx)$

 $5_{1} = \left(\frac{1}{2} - \frac{1}{71}\right) \cdot \frac{7}{2}(-1) = \frac{1}{2} - \frac{7}{4}$

 $f(\frac{\pi}{2}) = 0 = \frac{1}{\pi} + 0 = \frac{2}{\pi} \sum_{m=1}^{\infty} \frac{(-1)^m}{(2m)^2 - 1} \cdot \cos(m\pi) =$

1=f(0)=FV(f)(0)= 1+1-2 = S1=

 $S_{2} = -\frac{1}{\pi} \cdot \frac{\eta}{2} = -\frac{1}{2}$

4k+2 it 4k+3 Sin 3/7 +1/4k+1 Sin 1 ==

1/1 (- 1/2 + 1/4)

 $= \frac{1}{n} \begin{cases} 6 ; n \text{ liho} \\ \frac{(-1)^{m+1}-2}{(2n)^2-1} ; n=2m \end{cases}$

 $\frac{1}{77} \left[\frac{1}{\text{n+1}} \text{ Sir}((n+1) \frac{17}{2}) + \frac{1}{h-1} \text{ Sir}((u-1) \frac{17}{2}) \right]$

$$S_{A} = \sum_{n=1}^{\infty} \frac{(-1)^{n}}{4n^{2}-1}$$

$$S_{2} = \sum_{n=1}^{\infty} \frac{1}{4n^{2}-1}$$

$$Q_{0} = 2\pi \int_{-\pi}^{\pi} f(\omega) = \frac{1}{\pi} \int_{-\pi}^{\pi} \cos(x) = \frac{1}{\pi} \sin(\frac{\pi}{2}) = \frac{1}{\pi}$$

$$FV_{cos}(f)(X) = FV(f)(X)$$

$$v) f_{1}:C^{-1}, \pi] \longrightarrow \mathbb{R} \qquad f_{1}(X) = FV(f_{1})(X)$$

$$FV_{sin}(f)(X) = FV(f_{1})(X)$$

$$FV_{sin}(f)(x) = FV(f_0)(x)$$

$$FV_{sin}(f)(x) = FV(f_0)(x)$$

$$f_{S}(x) = x^{2}$$

$$Q_{0} = \frac{1}{2\pi} \int_{-\infty}^{\infty} x^{2} dx = \frac{\pi^{2}}{3}$$

$$\int x^{2} e^{inx} =$$

$$\int x^{2} e^{inx} =$$

$$u = x^{2} \quad dv = e^{inx} dx$$

$$du = 2x dx \quad V = \frac{1}{in} e^{inx}$$

$$u = x^{2} \quad dw = e^{inx} dx$$

$$du = 2x dx \quad v = \frac{1}{in} e^{inx}$$

$$x^{2} \cdot \frac{e^{inx}}{in} - \int 2x \frac{e^{inx}}{in} dx = \frac{1}{in} dx$$

$$= x^{2} \cdot \frac{e^{inx}}{in} - \int_{2x} \frac{e^{inx}}{jn} dx = e^{-inx}$$

$$= x^{2} \cdot \frac{e^{inx}}{in} - \frac{2}{in} \left(\frac{ixe^{inx}}{n} + \frac{e^{inx}}{n^{2}} \right) + C$$

$$\frac{(-n^{\frac{1}{2}} + \frac{1}{n^{\frac{2}{3}}})}{n^{\frac{2}{3}}}$$

$$\frac{(-n^{\frac{1}{2}} + \frac{1}{n^{\frac{2}{3}}})}{n^{\frac{2}{3}}}$$

$$\frac{(-n^{\frac{1}{2}} + \frac{1}{n^{\frac{2}{3}}})}{n^{\frac{2}{3}}}$$

$$\frac{(-n^{\frac{1}{2}})}{n^{\frac{2}{3}}}$$

$$= x^{2} \cdot \frac{e^{inx}}{in} - \int_{2x}^{2x} \frac{e^{inx}}{jn} dx =$$

$$= x^{2} \cdot \frac{e^{inx}}{in} - \frac{2}{in} \left(\frac{j \times e^{inx}}{n} + \frac{e^{inx}}{n^{2}} \right) + C$$

$$= e^{inx} \left(\frac{j \times 2}{-n} + \frac{2x}{n^{2}} + \frac{2i}{n^{3}} \right)$$

$$\cos nx + j \sin nx$$

$$= x^{2} \cdot \frac{e^{inx}}{in} - \frac{2}{in} \left(\frac{i \times e^{inx}}{n} + \frac{e^{inx}}{n^{2}} \right) + C$$

$$= e^{inx} \left(\frac{i \times ^{2}}{-n} + \frac{2x}{n^{2}} + \frac{2i}{n^{3}} \right)$$

$$= e^{inx} \left(\frac{i \times ^{2}}{-n} + \frac{2x}{n^{2}} + \frac{2i}{n^{3}} \right)$$

$$= e^{inx} \left(\frac{i \times ^{2}}{-n} + \frac{2x}{n^{2}} + \frac{2i}{n^{3}} \right)$$

$$= \int x^{2} \cos(nx) dx = \frac{x^{2}}{n} \sin(nx) + \frac{2x}{n^{2}} \cos(nx) - \frac{2x}{n^{2}} \cos(nx) - \frac{2x}{n^{2}} \cos(nx) + \frac{2$$

 $\int X^{2} \cos(nx) dx = \frac{x^{2}}{n} \sin(nx) + \frac{2x}{n^{2}} \cos(nx) - \frac{2}{n^{3}} \sin(nx)$ $\int x^{2} \sin(nx) dx = \frac{-x^{2}}{n} \cos x + \frac{2x}{n^{2}} \sin(nx) + \frac{2}{n^{3}} \cos(nx)$ $Q_n = \frac{1}{\pi} \left(\frac{x^2}{h} \sin(nx) + \frac{2x}{h^2} \cos(nx) + \frac{2}{h^3} \sin(nx) \right) =$

$$\int x^{2} \cos(nx) dx = \frac{x^{2}}{n} \sin(nx) + \frac{2x}{h^{2}} \cos(nx) - \frac{x^{2}}{n} \sin(nx) + \frac{2x}{h^{2}} \cos(nx) - \frac{x^{2}}{n} \cos(nx) + \frac{2x}{h^{2}} \sin(nx) + \frac{2x}{h^{3}} \cos(nx) + \frac{2x}{h^{3}}$$

FV cos (A) W = 1 + 5 (-1) 4 ccs (x

b)
$$b_n = \frac{1}{\pi} \int_{S_n}^{\pi} f_n(x) \sin(x) = \frac{z}{\pi} \int_{S_n}^{\pi} f_n(x) \sin(x) dx$$

$$= \frac{7}{7} \left[-\frac{x^2}{h} \cos(6x) + \frac{2}{h^2} \sin 6x + \frac{2}{32} (\cos(6x)) \right]^{\frac{1}{1}}$$

$$= \frac{7}{n} \left(-\frac{n^2}{n} (-n)^n + \frac{2}{n^2} (-n)^n - \frac{2}{n^3} \right)$$

fux) = x(T+x) rezv.jv

6

$$PCM = Sin^{3} \times \text{ rewij } \text{ V FV}$$

Pred premistek:

$$f(x) = Sin \text{ Ux } \text{ Je } \text{ ze } \text{ FV}$$

$$b_{z} = 1, \text{ odd} = so \text{ O}$$

$$f(x) = Sin^{2} \times = \frac{1}{2} \left(\cos(\alpha - \beta) - \cos(\alpha + \beta) \right) = \frac{1}{2} \left(\cos(\alpha - \beta) - \cos(\alpha + \beta) \right) = \frac{1}{2} \left(\cos(\alpha) - \cos(\alpha + \beta) \right) = \frac{1}{2} - \frac{1}{2} \cos(\alpha + \beta) = \frac{1}{2} \left(\cos(\alpha) - \cos(\alpha + \beta) \right) = \frac{1}{2} - \frac{1}{2} \cos(\alpha + \beta)$$

$$\frac{1}{2} \left(\cos(\alpha) - \cos(\alpha + \beta) \right) = \frac{1}{2} \left(\cos(\alpha + \beta) - \cos(\alpha + \beta) \right) = \frac{1}{2} \sin(\alpha + \beta) = \frac{1}{2} \sin(\alpha +$$

ard tractinej tezisõe homogenega
loka astroide
$$\frac{1}{x^3+y^{\frac{2}{3}}=a^{\frac{2}{3}}}$$

 $\int x dm \int x ds$

$$\frac{2}{3} + y^{\frac{2}{3}} = \alpha^{\frac{2}{3}}$$

$$\frac{1}{3} + y^{\frac{2}{3}} = \alpha^{\frac{2}{3}}$$

$$\frac{1$$

$$x = a \cos^{3}t \qquad t \in [0, \frac{\pi}{2}] \quad \text{for in use partition}$$

$$x = a \cos^{3}t \qquad t \in [0, \frac{\pi}{2}] \quad \text{for in use partition}$$

$$y = a \sin^{3}t \qquad \qquad r(t) = (-3a\cos^{2}t \cdot \sin t, 3a\sin^{2}t \cos t)$$

$$|\vec{r}| = 3a \left(\cos^{4}t \cdot 2t \cdot a\right) = 1$$

$$|\vec{r}| = (-3a\cos 4 \cdot \sin t), 3a\sin 4\cos t$$

$$|\vec{r}| = 3a \int \cos^4 t \sin^2 t + \sin^4 t \cos^2 t = \frac{3a \cos t \sin t}{2}$$

$$|\vec{r}| = \frac{1}{2} \cot t \cot t + \frac{1}{2} \cot t + \frac{$$

$$= 3a \cos t \sin t$$

$$\int_{0}^{\pi} |r'(t)| dt = \int_{0}^{\pi} 3a \cos t \sin t dt = 0$$

$$u = \sin t dt$$

$$u = sinfdt$$

$$du = costdt$$

$$= 3a \int u du = \frac{3}{2}a$$

$$\int x ds = \int a\cos^3t \, 3a \cos^3t \sin t \, dt = \frac{3}{2}a$$

 $cost = \alpha \quad du = -sint$ $= 3a^{2} \int u^{4} du = \frac{3}{5}a^{2}$

a cos³t
$$cos3t$$

$$cos$$

7(+)...parmetizacy $ds = |\dot{r}(t)|dt = \sqrt{\dot{x}^2 + \dot{y}^2 + \dot{z}^2} dt$

 $x_{\tau} = \frac{\int x \, dm}{m(\kappa)} = \int_{\kappa} \frac{x \, \rho \, ds}{\int \rho \, ds} = J(\kappa)$

z= asinu

$$\vec{f}(x,y,z) = (y-z, z-x, x-y) \quad \text{velitor sho}$$

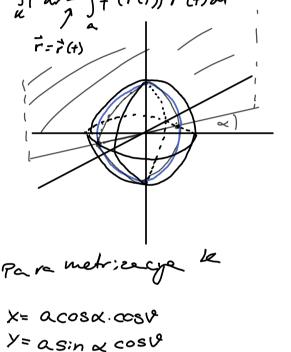
$$\vec{f}(x,y,z) = (y-z, z-x, x-y) \quad \text{velitor sho}$$

$$\vec{f}(\vec{r},y,z) = \vec{f}(\vec{r},y,z) \Rightarrow d\vec{r}$$

$$\vec{f}(\vec{r},y,z) \Rightarrow d\vec{r}$$

$$\vec{f}(\vec{r},y,z) \Rightarrow d\vec{r}$$

$$\vec{f}(\vec{r},y,z) \Rightarrow d\vec{r}$$



Y(V) = (acost cos x, acos v sin x, asm v) $V \in [-\frac{\pi}{2}, \frac{\pi}{2}]$ Y(V) = (asin v cos x, -asin v sin x, acos v)

 $\hat{f}(\hat{r}(y)) = \alpha \left(\cos \theta \sin \theta - \sin \theta - \cos \theta \cos \theta \cos \theta\right)$ $\cos \theta \sin \theta - \cos \theta \cos \theta$ $\hat{f} \cdot \hat{r} = \alpha^2 \left(-\cos \theta \cos \theta \cos \theta \sin \theta\right)$

- $S:n^2U sin\alpha + CosU cos a sinU sin\alpha +$ + $Cos^2U sin\alpha - cos^2U cos\alpha)$ =

= $a^2(cos 2U sin\alpha - cos 2U cos\alpha)$

 $= a^{2}(\cos \alpha - \sin \alpha)$ 2π $\int \vec{f} d\vec{r} = \int a^{2}(\cos \alpha - \sin \alpha) d\theta = 0$

2Ta2 (cosx-sina)

t pri orientaji

X= cosu cosp y = cosu sing 9€ [0, 1] $\vec{r}(u, p) = (\cos u \cos p, cosusinp, sinu)$

Pox Pp= (-cos2 vc osp, cos2 vsing, - sinucosucosy - cosusinusiny) =

= - cosu (cosu cosu, - cosusup, sinu-)

Silde J dy facosiocosp+ bcosio sn-csnown

= (-cosucosp, cosusing, _sinucosu) =

 $r_{\alpha} = (-sinulcose, -sinulsine, cosul)$

 $= \iint_{0}^{2} (-a\cos\rho + b\sin\rho)\cos^{2}\theta + \frac{\pi}{2} \cos^{2}\theta d\theta = 0$ $= \iint_{0}^{2} (-a\cos\rho + b\sin\rho) \frac{\pi}{4} - \frac{C}{2} = 0$ $= \iint_{0}^{2} (-a\cos\rho + b\sin\rho) \frac{\pi}{4} - \frac{C}{2} = 0$

 $= \left(-\frac{\pi a}{u} \sin \rho + \frac{\pi}{u} b \cos \rho - \frac{c}{2} \rho \right) \Big| =$

 $= -\frac{\pi}{u} a - \frac{\pi}{u} b - \frac{\pi}{u} c = -\frac{\pi}{u} (a + b + c)$

$$\vec{f}(x,y,z) = (y^2 - z^2, z^2 - x^2, x^2 - y^2)$$

i (x,y,2) = (y2-z2, z2-x2, x2-y2) Izracunaj cirkulacijo f vzdolž preseka roba kocke [0,a]3 in

ravnine
$$x+y+z=\frac{3a}{2}$$

k;vulj= 6 ketnik

cirkulacija ... integral vektorskega polje sklenjene wirule

y=0 Z= 30 -X r(x)=(x,0, 3e-x)

$$\int_{K_{1}}^{\infty} f dx$$

$$K_{1} = (1,0,-1)$$

$$f(r(x) = (0 - (\frac{3}{2} - x)^{2}) \cdot (\frac{3}{2} - x^{2}) - x^{2}, x^{2} = 0$$

$$f \cdot \dot{r} = -(\frac{3}{2} - x)^{2} - x^{2} = -2x^{2} + 3ax - \frac{3}{4}a^{2}$$

$$a = \int ((\frac{3}{2}a - x)^{2} - x^{2}) dx = \frac{1}{3}(\frac{3}{2}a - x)^{3} - \frac{1}{3}x^{3} = \frac{1}{3}(\frac{3}{2}a - x)^{3} - \frac{1}{3}(\frac{3}{2}a - x)^{3} + \frac{1}{3}(\frac{3}{8}a - x)^{3} = 0$$

m, n,p > 0 a, b, c eR $I = \int x^2 dz dy + y^2 dx dz + z^2 dx dy$ $S: \left(\frac{x-a}{m}\right)^2 + \left(\frac{y-b}{n}\right)^2 + \left(\frac{z-c}{p}\right)^2 = 1$ Zunanja stran te plostue F= (x2+ y2+22) I = \int fd8 = \int div fdV gaussov : 2 rek \int D Normala mara b:ti \int \int \text{zunanja} $\int (2x+2y+2z)dV = 2x_{7}+2y_{7}+2z_{7}$ $x_7 = \int_{X} dW = x_7 \cdot V(D) = qV(D)$

enotale hagle B: V(B)= 47, 3= 47

V(D)= m.n.p. 47

V(D)= m.n.p. 47

D dobina ce Brackegnemo cafelder
m vener: x, n,p v drujh duch

Bopiseno:

X=rcosvesip

y=rcosvesinp

z=rsinv

x = mrcospcosu y = nrcasus mp z = prsinu $T = 2 \frac{4}{3} 7 m \cdot n \cdot p \left(a + b + c\right)$

Dop:semo:

$$\vec{f}(\vec{r}) = |\vec{r}|^2 \vec{r} \quad b > 0$$

$$|\vec{r} = cuning \quad pretok \quad \vec{f} \quad shoz$$

$$|\vec{r} = cuning \quad pretok \quad \vec{f} \quad shoz$$

$$|\vec{r} = cuning \quad pretok \quad \vec{f} \quad shoz$$

$$|\vec{r} = cuning \quad pretok \quad \vec{f} \quad shoz$$

$$|\vec{r} = cuning \quad pretok \quad \vec{f} \quad shoz$$

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= 5x45y2+5z2

y=r sing

Sd:v fdW = 5 S(x2+y2+z2) W

 $= 5 \int_{0}^{\infty} dy \int_{0}^{\infty} dx \int_{0}^{\infty} (r^{2} + z^{2}) r dz$

 $= 5 \int_{0}^{2\pi} d\rho \int_{0}^{2\pi} (r^{3}z + \frac{1}{3}z^{3}) \int_{0}^{2\pi} dr$

 $= 107 \int (br^3 + \frac{1}{3}b^3 - \frac{r^5}{2} - \frac{1}{6}r^6) dr =$

 $\left| \sqrt{2} \left(\frac{1}{u} b r^{4} + \frac{1}{3} b^{3} r - \frac{1}{12} r^{6} - \frac{1}{6^{2}} r^{7} \right) \right| =$

= $4C\Pi\left(\frac{1}{4}b^3\cdot4+\frac{1}{3}b^3\sqrt{2}b-\frac{1}{12}\cdot8b^3-\frac{1}{6\cdot7}\cdot8b^3\sqrt{2}b\right)$

= $\int (2x^2 + 2y^2 + 2^3) ds = \int (6x^2 + 6y^2 + 6^3) ds =$

 $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \left(\int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr \right)$ $= 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} (r^{2} + 6^{2}) dr = 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr = 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr = 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr = 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} dr + \frac{\partial^{2}}{\partial r^{2}} dr = 6 \int_{0}^{\infty} d\rho \int_{0}^{\infty} r^{2} d\rho \int_{0}^{\infty} r^$

=> Job Stag = 10 11 63+13764-2763

 $10\pi \left(6^3 + \frac{6^4}{3} - \frac{2}{3} 6^3 - \frac{6^4}{12} \right) =$

1011 (53+ 54)

Sfd8 = Sfds - Sfd8

 $\int_{S} f ds = \int_{S_0} (f \cdot \vec{n}) ds =$

 $= b \left(271b^3 + \int dp \int r^3 dr\right) =$

= 21164 +21163

= 6(21163+ 1 211 4.462)=

b) D= SU So

y=rsing

trannej I=5 xdy-ydx EC & K = R2 sklengere k:vuly; a) hi ne abkrozi izhadisa b) ki dohadi jehadisce Omejima e ne prime: K=dD Z D'odsehme gradkim rasa $\int_{\partial D} P_{dx} + Q_{dy} = \int_{\partial D} (Q_{x} - P_{y}) dxdy$ $\mathcal{P} = \frac{-y}{x^2 + y^2} \qquad \mathcal{Q} = \frac{x}{x^2 + y^2}$ $Q_{x} = \frac{x^{2}+y^{2}-2x^{2}}{(x^{2}+y^{2})^{4}} = \frac{y^{2}-x^{2}}{(x^{2}+y^{2})^{4}}$ $\mathcal{P}_{y} = \frac{-x^{2}+y^{2}}{(x^{2}+y^{2})^{2}}$ $\int_{\mathbb{R}} (Q_{x} - P_{y}) dxdy = \int_{\mathbb{R}} 0 dxdx = 0$ D ne abbraci (0,0) (0,0) & D (x2+x2) #0 K(0, E) D'= D-K(0,e) Uporabino greenovo Amulo net) 80'= 80+ 8 K(O,E)-0= SPax+Qdy+SPdx+Qdx Poor or: entiring light ponared:

k Dierezano dovolj mejhon krcay $\int Q + P_{0} + P_{0} = 0$ $\int Q + P_{0} + P_{0} = 0$ x= Ecosp y= Esing dx=-Esaf $\int_{...}^{2\pi} = \frac{1}{\xi} \int_{-2\pi}^{2} c_{+5;n} c_$ dx = Ecosp