

Department of Chemical Engineering
Thapar Institute of Engineering &
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Course: Material and Energy Balances
UCH301

Course Instructor:
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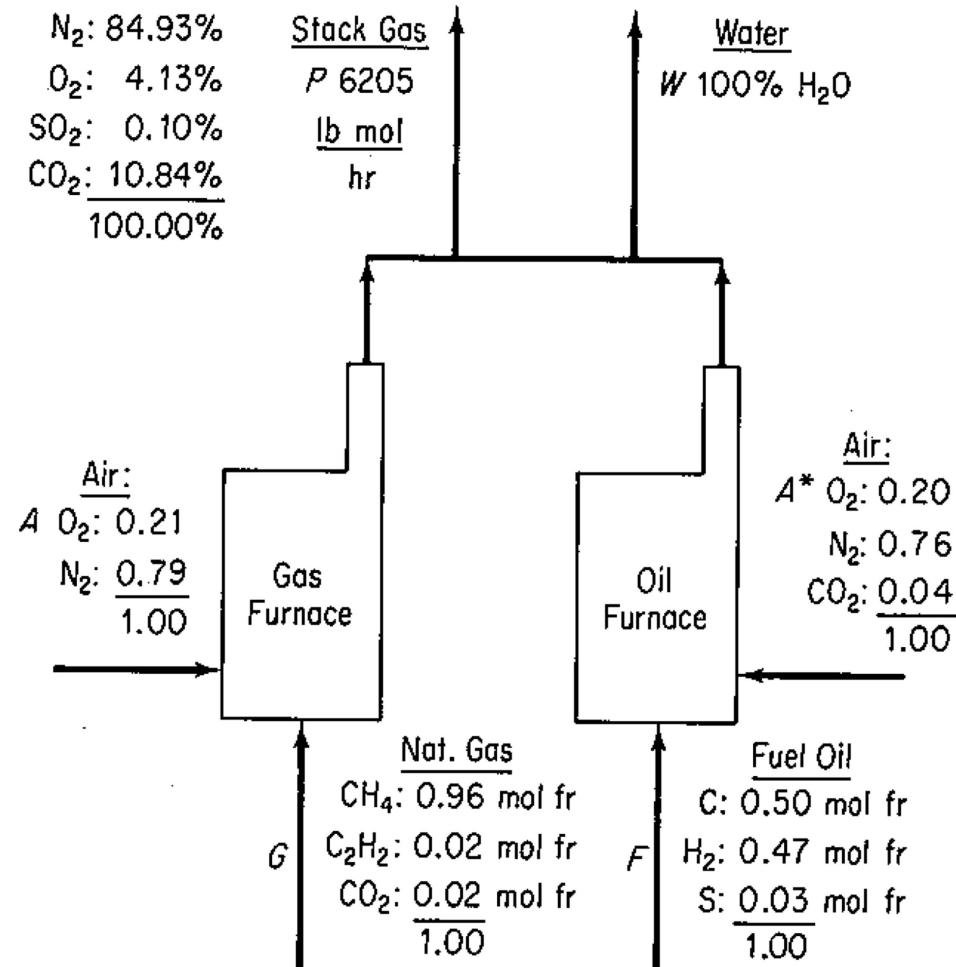


Problem

- A company operates two boilers to generate steam. First boiler uses Fuel Oil (C =50mol%, H₂ = 47 mol%, S = 3 mol%) and the second one uses Natural gas (CH₄ = 96%, C₂H₂ =2%, CO₂=2%). Air (O₂=20%,N₂=76%, CO₂ = 4%) is used in the first boiler and Air (O₂=21% and N₂=79%) is used in the second boiler.
- The orsat analysis of the flue gas from the combined stack of the two boilers is (N₂=84.93%, O₂=4.13%, SO₂ =0.1%, CO₂=10.84%). The stack gas flow is 6205 lbmol/hr. Calculate the molar rates of Natural Gas and Fuel oil.

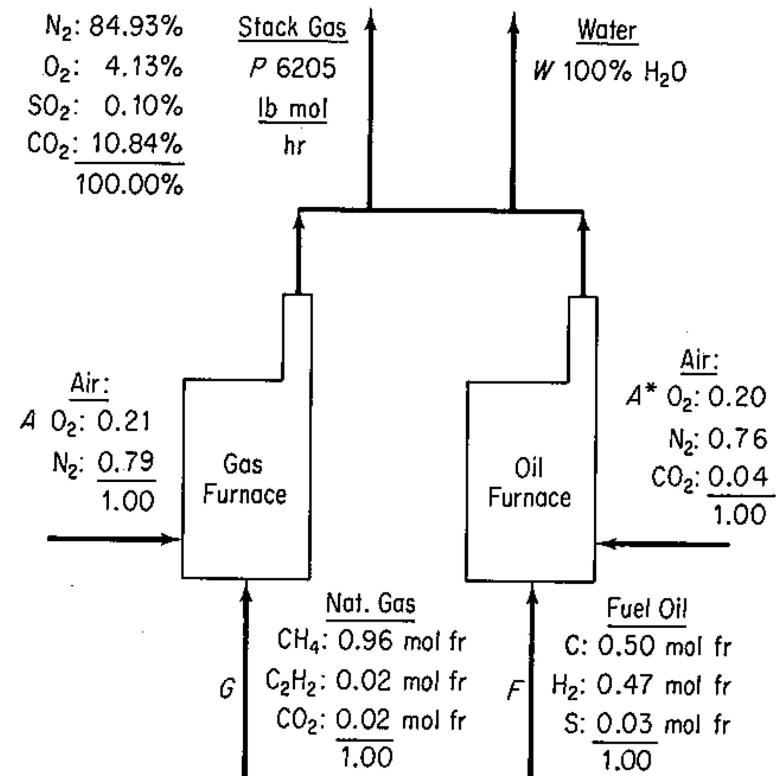


The figure below shows the process arrangement



Solution

- Basis:** As the amount of stack gas flow is given in the problem statement, we will select this amount as basis of our calculations.
- The composition of all streams are given, but information about the combustion in each boiler is not provided.
- In such case we will need to write elemental species balances, to calculate the flows of the various streams



Writing elemental species balances

- As you can see that sulphur is entering from one stream (Fuel oil) only and leaving from one stream, so, S balance can be solved independently
- Balance for sulphur: Sulphur in = Sulphur out

$$\text{S: } F(0.03) = 6205(0.001)$$

$$\rightarrow F = 207 \text{ lbmol/hr}$$

- The remaining balances will have to be solved simultaneously



Elemental species balances

- Balances for H, N₂, and O & C

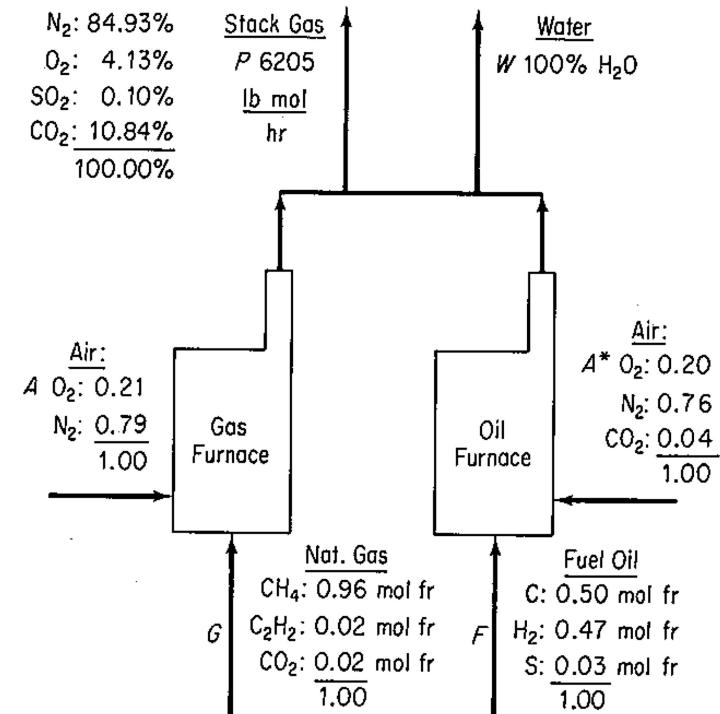
In = Out

$$\text{H: } G(0.96*4+0.02*2) + F(0.47*2) = W*2$$

$$\text{N: } A(0.79*2) + A^*(0.76*2) = 6205 (0.8493*2)$$

$$\text{O: } G(0.02*2) + A(0.21*2) + A^*(0.2*2+0.04*2) = 6205*2(0.0413+0.001+0.1084) + W*1$$

$$\text{C: } G(0.96+2*0.02+0.02) + F(0.5) + A^*(0.04) = 6205(0.1084)$$



ANSWERS

- **FOUR UNKNOWNS A, A*, G, & W CAN BE OBTAINED BY SOLVING THE ABOVE EQUATIONS**
- ✓ Fuel oil (F) = 207 lbmol/hr
- ✓ NG (G) = 498 lbmol/hr
- ✓ $A^* = 1529 \text{ lbmol/hr}$
- ✓ $A = 5200 \text{ lbmol/hr}$
- ✓ $W = 1067.6 \text{ lbmol/hr}$



Combustion of Liquid Fuel



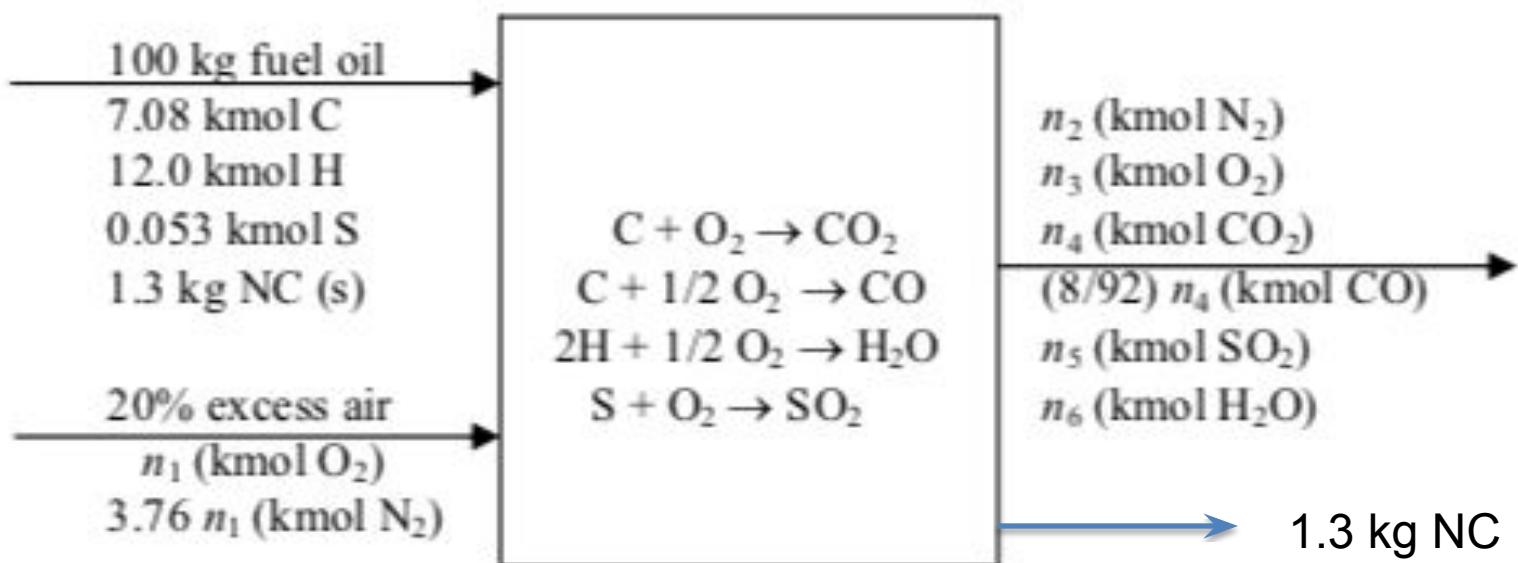
Exercise

- A fuel oil is analyzed and found to contain 85.0 wt% carbon, 12.0% elemental hydrogen (H), 1.7% sulfur, and the remainder noncombustible matter. The oil is burned with 20% excess air, based on complete combustion of the carbon to CO_2 , the hydrogen to H_2O , and the sulfur to SO_2 . The oil is burned completely, but 8% of the carbon forms CO. Calculate the molar composition of the stack gas.



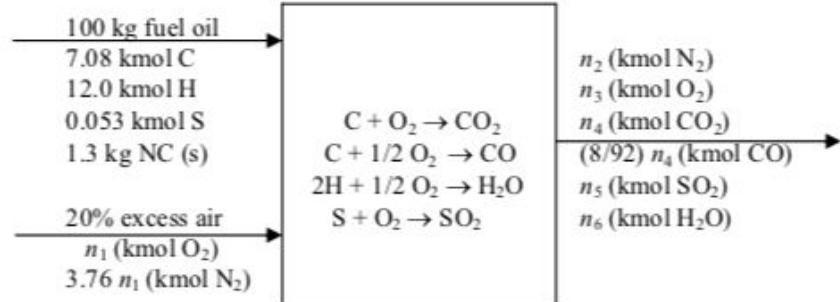
Solution

- Basis: 100 kg fuel oil



- If n_1 are moles of O₂, then moles of N₂
 $= 0.79/0.21 = 3.76 n_1$

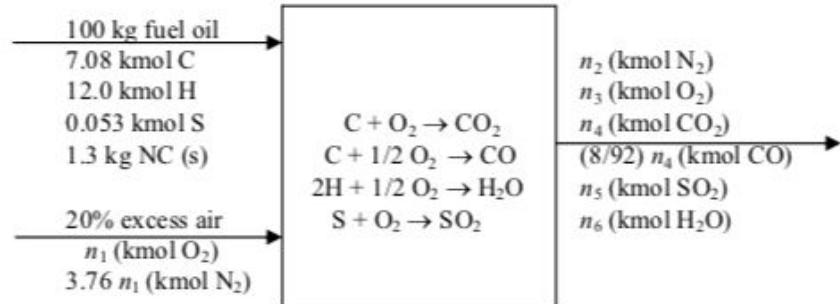




Before applying balance we will convert the mass units to mole units

- Moles of C in fuel = $100 * 0.85 / 12 = 7.08 \text{ kmol C}$
- Moles of H in fuel = $100 * 0.12 / 1 = 12 \text{ kmol H}$
- Moles of S in fuel = $100 * 0.017 / 32 = 0.053 \text{ kmol S}$
- ✓ Non combustible material in fuel is 1.3 kg, we can not convert this amount into moles as mol.wt. is not known so we will leave this amount in kg.
- ✓ Also, since the non combustible material will come out as such so keeping this amount in kg is ok.





Theoretical amount of O₂ required for combustion

mol O₂ required for C = moles of C = 7.08 kmol

mol O₂ required for H = moles of H/4 = 12/4 = 3 kmol

mol O₂ required for S = moles of S = 0.053 mol

Mol O₂ required for combustion = 7.08+3+0.053=10.133 kmol

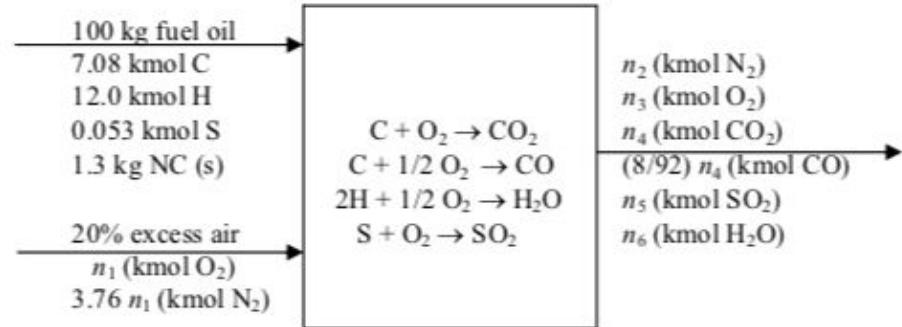
Therefore Air required = 10.133/0.21 =48.25 kmol

Air Supplied = 48.25*1.2 = 57.9 kmol

O₂ supplied = 57.9/0.21 = 12.16 kmol

N₂ supplied = 3.76*12.16 = 45.72 kmol





Here, the relation between amounts of CO and CO₂ formed is given:

- Moles of C burned = 7.08 kmol

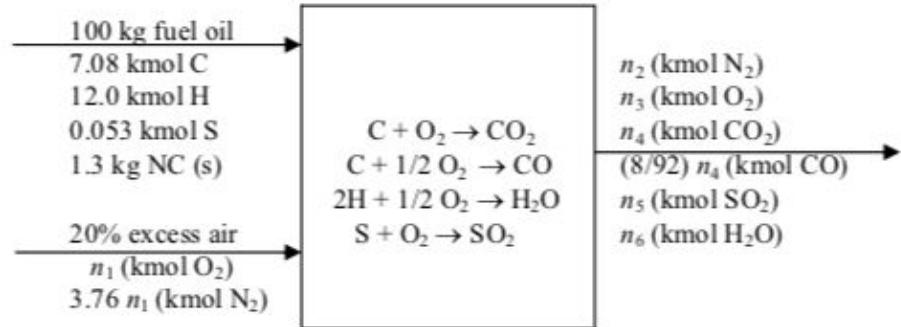
Therefore, $7.08 = n_4 + (8/92)*n_4 \rightarrow n_4 = 6.514$ mol CO₂

Mol of CO formed = $(8/92)*6.514 = 0.566$ mol

The amount of O₂ reacted = O₂ required - (CO formed/2)
 $= 10.133 - 0.566/2 = 9.853$ kmol

O₂ out = O₂ supplied - O₂ reacted = $12.16 - 9.853 = 2.31$ kmol = n_3





SO₂ formed = moles of S burned = 0.053 kmol = n₅

H₂O out = n₆ = moles of H in/2 = 6 kmol

N₂ out = N₂ in = 45.72 kmol = n₂

O₂ out = O₂ supplied-O₂ reacted = 12.16-9.853= 2.31 kmol=n₃

Total moles of flue gas = 45.72+2.31+6.514+CO mol+0.053+6
 = 61.16 kmol

Mol% composition of flue gas:

CO₂ = 10.7%, CO=0.92%, SO₂ =0.087%

H₂O =9.8%, O₂ 3.8%,N₂ = 74.8%

