

Roll Number: \_\_\_\_\_

**Thapar University, Patiala**Department of Electronics and Communication Engineering  
END SEMESTER EXAMINATION

B. E. (Second Year): Semester-III (2017/18) (ECE/ENC)	Course Code: UEC404
11 <sup>th</sup> December, 2017	Course Name: Signals and Systems
Time: 3 Hours, M. Marks: 100	Monday, 9.00 – 12.00 Hrs.
	Name of Faculty: US, SP, MK, NS, SK

**Note: Attempt all questions****Assume missing data, if any, suitably**

Q.1 (a) Determine and plot the even and odd components of a signal (10)

$$x(t) = \begin{cases} 2e^{-2t}, & t > 0 \\ 0, & t < 0 \end{cases}$$

Q.1 (b) Consider the system with input  $x(t)$  and output  $y(t)$  given by (4+6=10)

$$y(t) = \sum_{n=0}^3 x(t)\delta(t - nT)$$

- (i) Is this system linear?
- (ii) Suppose that input to the system is  $x(t) = \cos(2\pi t)$ . Sketch and label the output  $y(t)$  for each of the following values of  $T$ : 1 and 0.5

Q.2 (a) The input and the output of a causal LTI system are related by (10)

$$\text{differential equation: } \frac{d^2y(t)}{dt^2} + 6\frac{dy(t)}{dt} + 8y(t) = 2x(t)$$

- i) Find the impulse response of the system.
- ii) What is the response of this system if  $x(t) = te^{-2t}u(t)$ ?

Q.2 (b) Find the inverse Laplace transform of (10)

$$X(s) = \frac{-5s - 7}{(s + 1)(s - 1)(s + 2)}$$

if the ROC is

- i)  $\Re\{s\} > 1$
- ii)  $\Re\{s\} < -2$
- iii)  $-1 < \Re\{s\} < 1$
- iv)  $-2 < \Re\{s\} < -1$

Q.3 (a) Determine the z-transform of (8)

$$x(n) = \left(\frac{1}{2}\right)^n u(n) + 2^n u(-n - 1)$$

and depict the ROC and the locations of poles and zeros in the z-plane.

Q.3 (b) Given the following five facts about a discrete-time signal  $x(n)$  with z-transform  $X(z)$  (12)

- i)  $x(n)$  is real and right-sided

- ii)  $X(z)$  has exactly two poles.
- iii)  $X(z)$  has two zeros at the origin
- iv)  $X(z)$  has a pole at  $z = (1/2)^{e^{j\pi/3}}$
- v)  $X(1) = 8/3$

Determine  $X(z)$  and specify its ROC

- Q.4 (a) With the help of discrete Fourier transform (DFT) and inverse DFT, (10) determine the sequence corresponding to the circular convolution of  $x_1(n)$  and  $x_2(n)$ . The sequences  $x_1(n)$  and  $x_2(n)$  are defined as follows:

$$x_1(n) = \{2, 1, 2, 1\} \text{ and } x_2(n) = \{1, 2, 3, 4\}$$

- Q. 4(b) Consider  $x(n) = \{\alpha_0, \alpha_1, \alpha_2, \alpha_3\}$  where  $\alpha_i; i=0,1,2,3$  are real numbers. (10)  
If  $\text{DFT}[x(2n)] = \{4, -2\}$  and  $\text{DFT}[x(2n+1)] = \{6, -2\}$ , then determine the sequence  $x(n)$ .

- Q.5 (a) Two manufacturing plants produce similar parts. Plant 1 produces 1000 parts, 100 of which are defective. Plant 2 produces 2000 parts, 150 of which are defective. A part is selected at random and found to be defective. What is the probability that it came from plant 1? (05)
- Q.5 (b) Consider a random process  $X(t)$  defined by  $X(t) = A \cos(\omega t + \theta)$ , (05)  $-\infty < t < \infty$ , where  $A$  and  $\omega$  are constant and  $\theta$  is a uniform random variable over  $(-\pi, \pi)$ . Show that  $X(t)$  is wide sense stationary process.

- Q. 5 (c) Let  $X$  be a continuous random variable with pdf (10)

$$f_X(x) = \begin{cases} kx & 0 < x < 1 \\ 0 & \text{othersise} \end{cases}$$

where  $k$  is a constant.

- (i) Determine the value of  $k$  and sketch  $f_X(x)$
- (ii) Find and sketch the corresponding CDF  $F_X(x)$
- (iii) Find  $P\left(\frac{1}{4} < X \leq 2\right)$ .

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The answer sheets will be shown on 20-12-17 in room no E101 at 10 a.m.