



Department of Chemical Engineering
Thapar Institute of Engineering &
Technology, Patiala

Course: Material and Energy Balances
UCH301

Course Instructor:

Dr. R. K. Gupta, Professor, Chemical Engineering

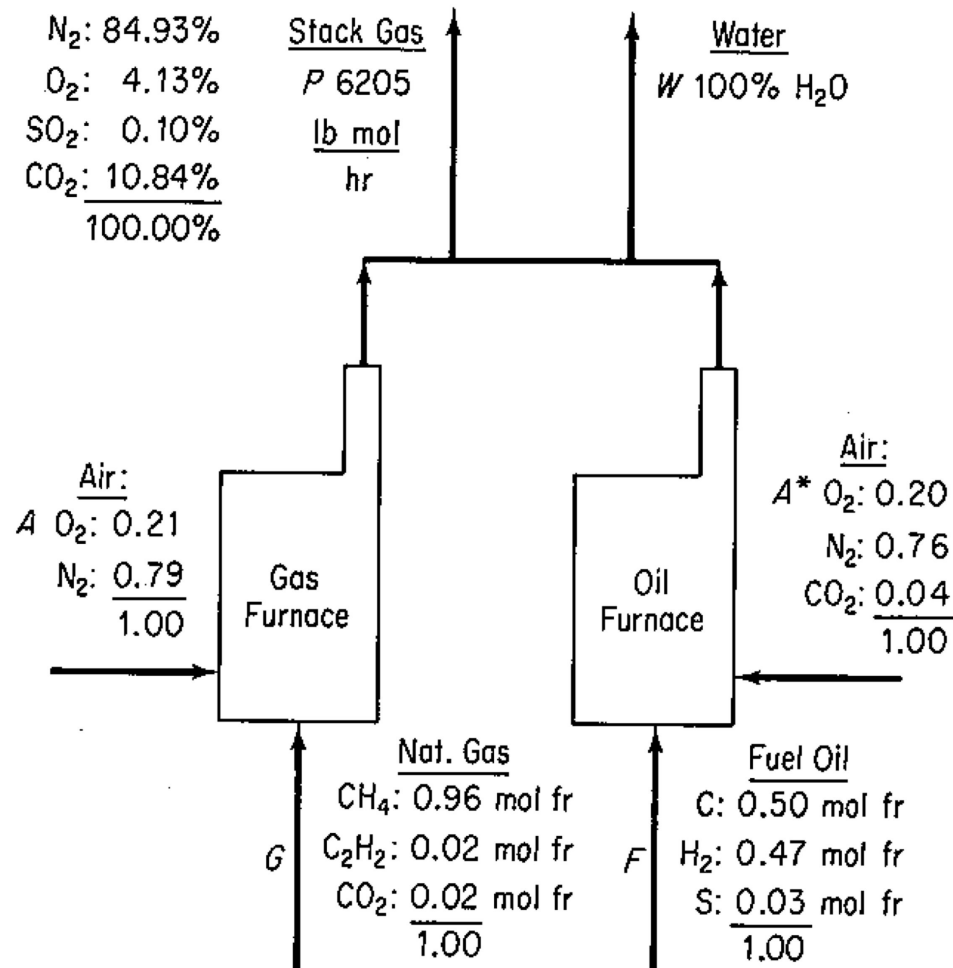


Problem

- A company operates two boilers to generate steam. First boiler uses Fuel Oil (C =50mol%, H₂ = 47 mol%, S = 3 mol%) and the second one uses Natural gas (CH₄ = 96%, C₂H₂=2%, CO₂=2%). Air (O₂=20%,N₂=76%, CO₂ = 4%) is used in the first boiler and Air (O₂=21% and N₂=79%) is used in the second boiler.
- The orsat analysis of the flue gas from the combined stack of the two boilers is (N₂=84.93%, O₂=4.13%, SO₂=0.1%, CO₂=10.84%). The stack gas flow is 6205 lbmol/hr. Calculate the molar rates of Natural Gas and Fuel oil.

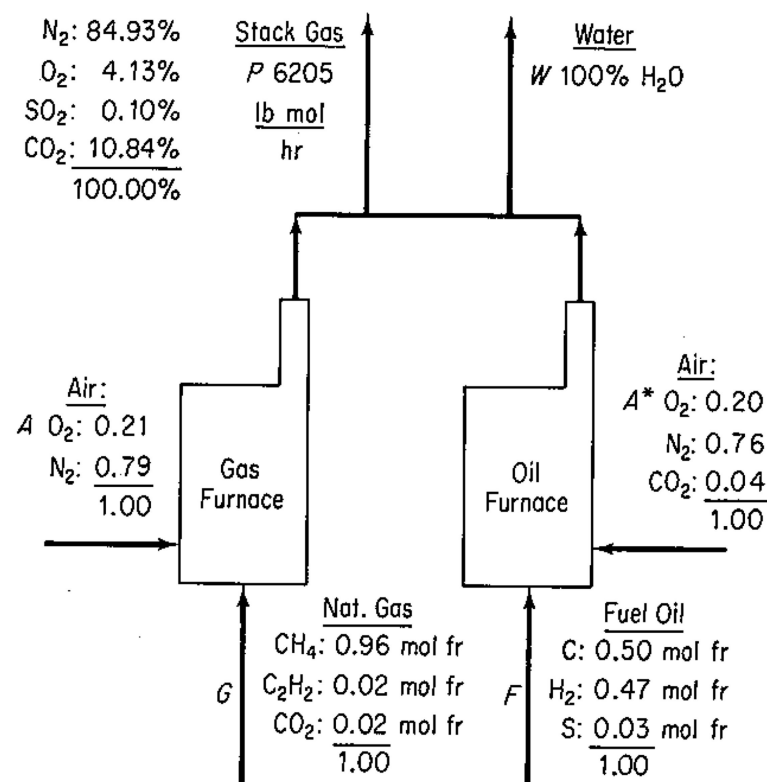


The figure below shows the process arrangement



Solution


- **Basis:** As the amount of stack gas flow is given in the problem statement, we will select this amount as basis of our calculations.
- The composition of all streams are given, but information about the combustion in each boiler is not provided.
- In such case we will need to write elemental species balances, to calculate the flows of the various streams



Writing elemental species balances

- As you can see that sulphur is entering from one stream (Fuel oil) only and leaving from one stream, so, S balance can be solved independently
- **Balance for sulphur:** Sulphur in = Sulphur out

$$\text{S:} \quad F(0.03) = 6205(0.001)$$

 $F = 207 \text{ lbmol/hr}$

- The remaining balances will have to be solved simultaneously





Elemental species balances

- Balances for H, N₂, and O & C

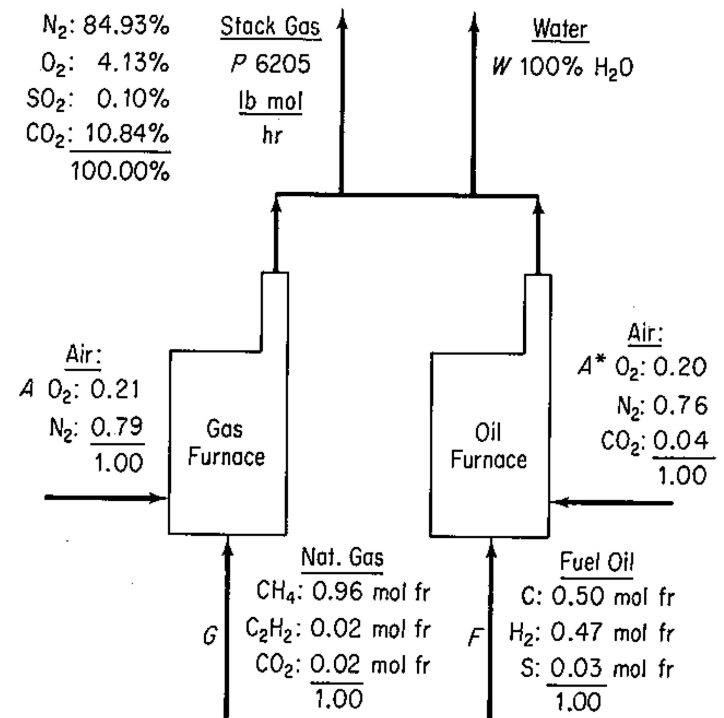
$$\text{In} = \text{Out}$$

$$\text{H: } G(0.96 \cdot 4 + 0.02 \cdot 2) + F(0.47 \cdot 2) = W \cdot 2$$

$$\text{N: } A(0.79 \cdot 2) + A^*(0.76 \cdot 2) = 6205(0.8493 \cdot 2)$$

$$\text{O: } G(0.02 \cdot 2) + A(0.21 \cdot 2) + A^*(0.2 \cdot 2 + 0.04 \cdot 2) = 6205 \cdot 2(0.0413 + 0.001 + 0.1084) + W \cdot 1$$

$$\text{C: } G(0.96 + 2 \cdot 0.02 + 0.02) + F(0.5) + A^*(0.04) = 6205(0.1084)$$



ANSWERS

- **FOUR UNKNOWNNS A, A*, G, & W CAN BE OBTAINED BY SOLVING THE ABOVE EQUATIONS**

✓ Fuel oil (F) = 207 lbmol/hr

✓ NG (G) = 498 lbmol/hr

✓ $A^* = 1529$ lbmol/hr

✓ $A = 5200$ lbmol/hr

✓ $W = 1067.6$ lbmol/hr



Combustion of Liquid Fuel



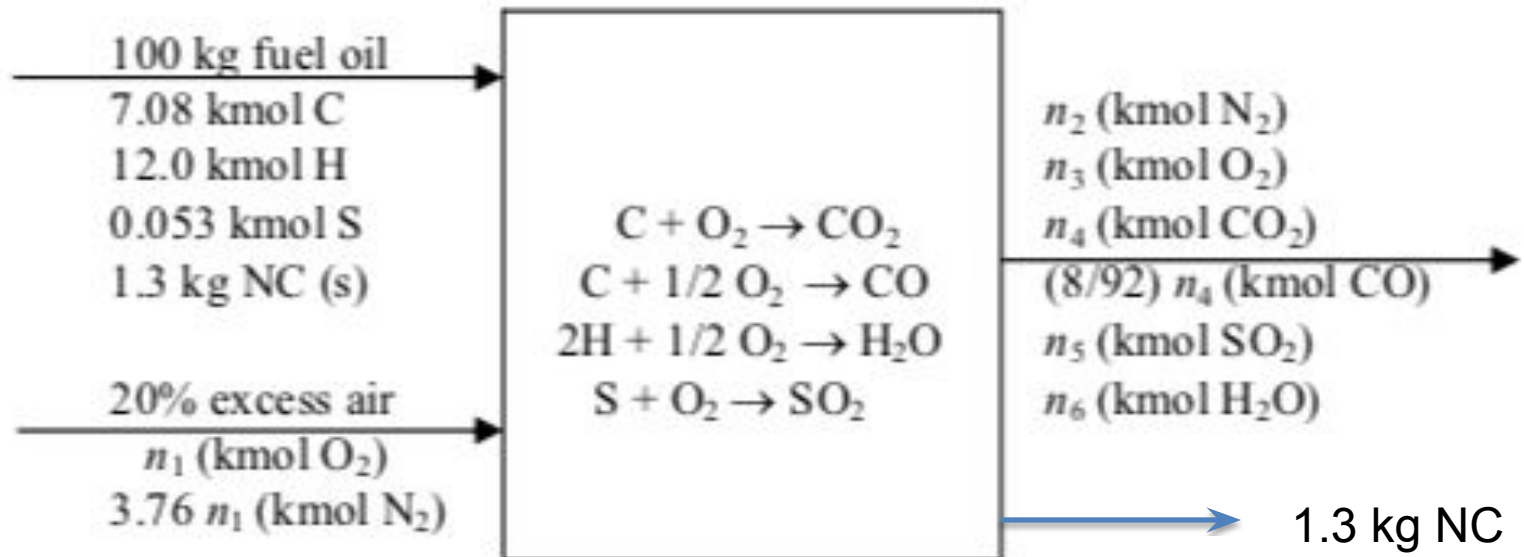
Exercise

- A **fuel oil** is analyzed and found to contain **85.0 wt% carbon**, **12.0% elemental hydrogen (H)**, **1.7% sulfur**, and the remainder noncombustible matter. The oil is burned with **20% excess air**, based on complete combustion of the carbon to CO_2 , the hydrogen to H_2O , and the sulfur to SO_2 . The oil is burned completely, but 8% of the carbon forms CO . Calculate the molar composition of the stack gas.



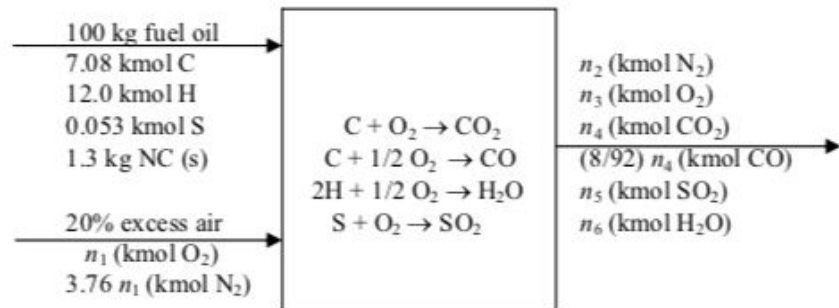
Solution

- Basis: 100 kg fuel oil



- If n_1 are moles of O_2 , then moles of N_2
 $= 0.79/0.21 = 3.76 n_1$

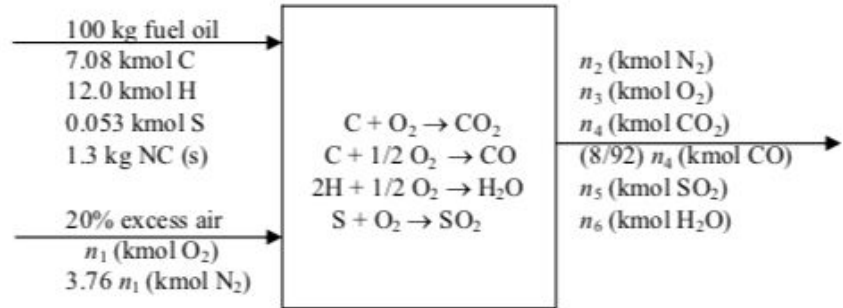




Before applying balance we will convert the mass units to mole units

- Moles of C in fuel = $100 \times 0.85 / 12 = 7.08 \text{ kmol C}$
- Moles of H in fuel = $100 \times 0.12 / 1 = 12 \text{ kmol H}$
- Moles of S in fuel = $100 \times 0.017 / 32 = 0.053 \text{ kmol S}$
- ✓ Non combustible material in fuel is 1.3 kg, we can not convert this amount into moles as mol.wt. is not known so we will leave this amount in kg.
- ✓ Also, since the non combustible material will come out as such so keeping this amount in kg is ok.





Theoretical amount of O_2 required for combustion

mol O_2 required for C = moles of C = 7.08 kmol

mol O_2 required for H = moles of H/4 = $12/4 = 3$ kmol

mol O_2 required for S = moles of S = 0.053 mol

Mol O_2 required for combustion = $7.08 + 3 + 0.053 = 10.133$ kmol

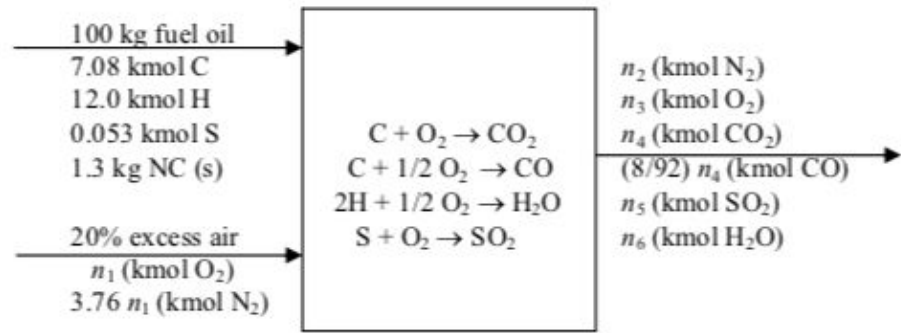
Therefore Air required = $10.133 / 0.21 = 48.25$ kmol

Air Supplied = $48.25 \times 1.2 = 57.9$ kmol

O_2 supplied = $57.9 / 0.21 = 12.16$ kmol

N_2 supplied = $3.76 \times 12.16 = 45.72$ kmol





Here, the relation between amounts of CO and CO₂ formed is given:

- Moles of C burned = 7.08 kmol

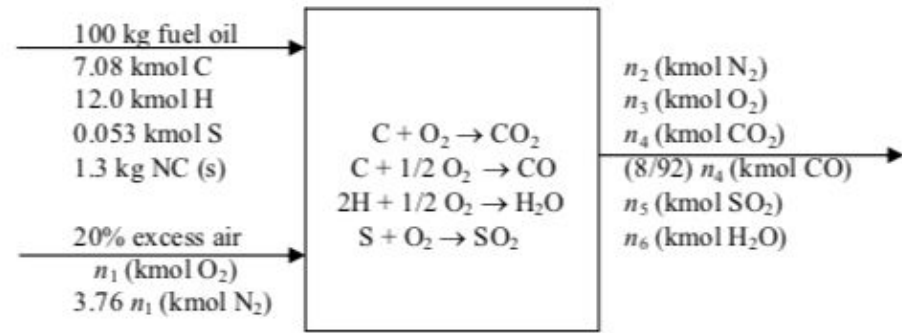
Therefore, $7.08 = n_4 + (8/92) \cdot n_4 \Rightarrow n_4 = 6.514 \text{ mol CO}_2$

Mol of CO formed = $(8/92) \cdot 6.514 = 0.566 \text{ mol}$

The amount of O₂ reacted = O₂ required - (CO formed/2)
 $= 10.133 - 0.566/2 = 9.853 \text{ kmol}$

O₂ out = O₂ supplied - O₂ reacted = $12.16 - 9.853 = 2.31 \text{ kmol} = n_3$





SO_2 formed = moles of S burned = 0.053 kmol = n_5

H_2O out = n_6 = moles of H in/2 = 6 kmol

N_2 out = N_2 in = 45.72 kmol = n_2

O_2 out = O_2 supplied - O_2 reacted = $12.16 - 9.853 = 2.31$ kmol = n_3

Total moles of flue gas = $45.72 + 2.31 + 6.514 + CO \text{ mol} + 0.053 + 6$
= 61.16 kmol

Mol% composition of flue gas:

$CO_2 = 10.7\%$, $CO = 0.92\%$, $SO_2 = 0.087\%$

$H_2O = 9.8\%$, $O_2 = 3.8\%$, $N_2 = 74.8\%$

