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# Mechanics of Machines

## UME 306

### Module - 1

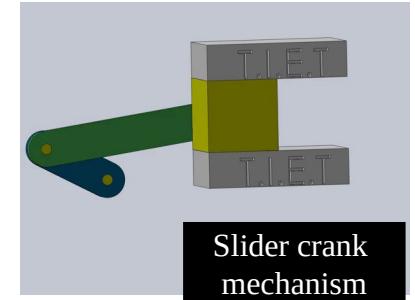
### Lecture - 4

# Instructional objective

- Kinematic fundamentals
- Types of joint in a chain
- Classification of kinematic pair
- Concept of mobility
- Criterion to plane mechanisms

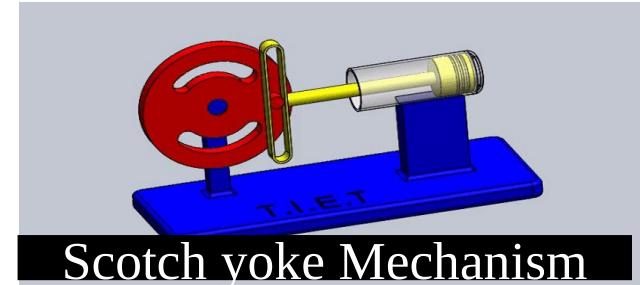
# Kinematic Fundamentals

**A Kinematic chain:** An assemblage of links and joints, interconnected in a way to provide a controlled output motion in response to a supplied input motion.



Slider crank mechanism

**Mechanism:** When one of the links of a kinematic chain is fixed, the chain is known as mechanism.



Scotch yoke Mechanism

**Simple Mechanism:** A mechanism with four links.

**Compound Mechanism:** mechanism with more than four links.

**Machine :** A combination of resistant bodies arranged to compel the mechanical forces of nature to do work accompanied by determinate motion.

# Types of joints in a chain

## 1. *Binary joint.*

$$j + 0.5h = 1 \cdot 5l - 2$$

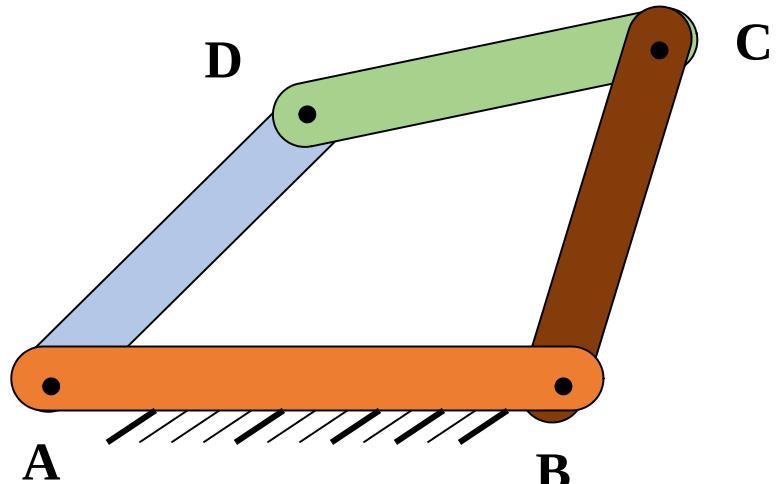
Where:

$j$  = Number of binary joints,

$h$  = Number of higher pairs, and

$l$  = Number of links

**If there is no any higher pair,  $h = 0$**



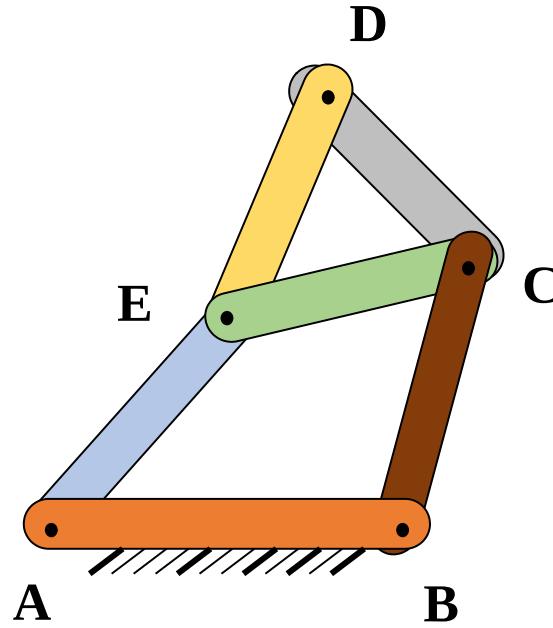
$$j = 4$$

$$h = 0$$

$$l = 4$$

If LHS = RHS , Kinematic chain or constrained chain

## 2. Ternary joint .



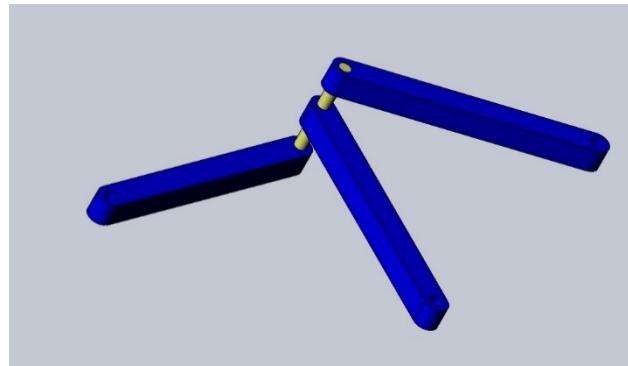
$$1T = 2B$$

$$J = 7$$

$$h = 0$$

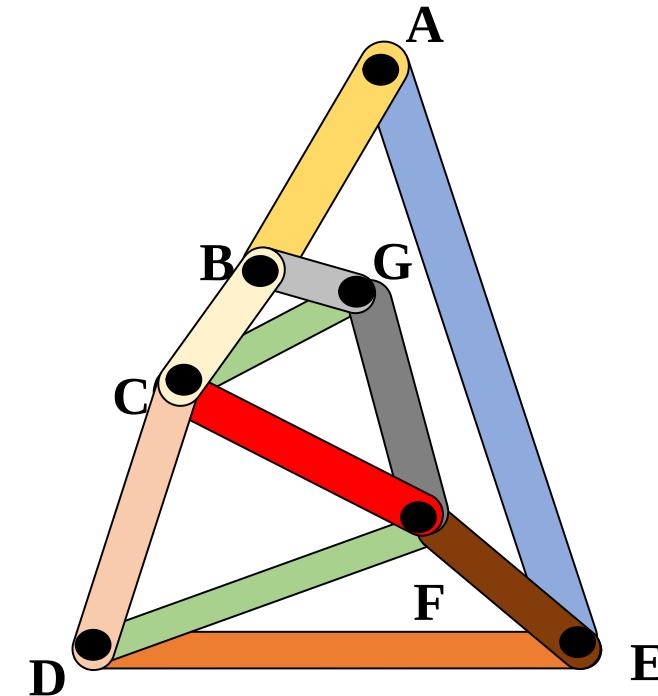
$$L = 6$$

$$\text{LHS} = \text{RHS}$$



$$J + 0.5h = 1 \cdot 5L - 2$$

## 3. Quaternary joint



$$1Q = 3B$$

$$J = 15$$

$$h = 0$$

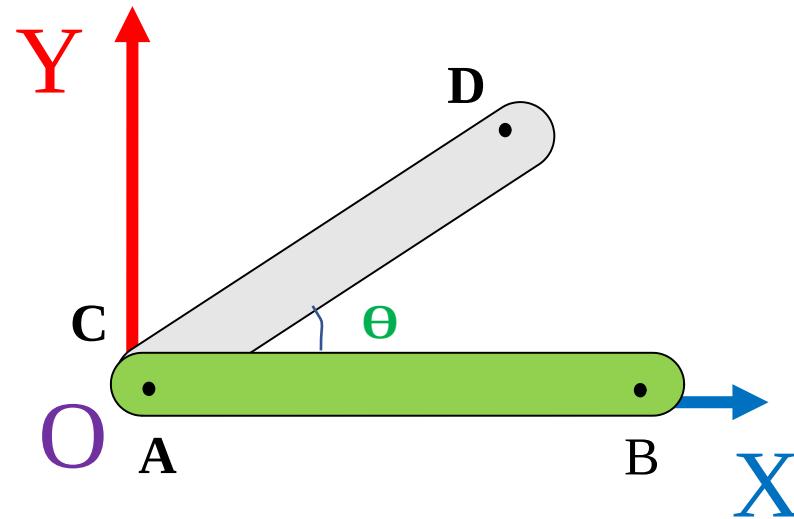
$$L = 11$$

$$\text{L.H.S.} > \text{R.H.S.}$$

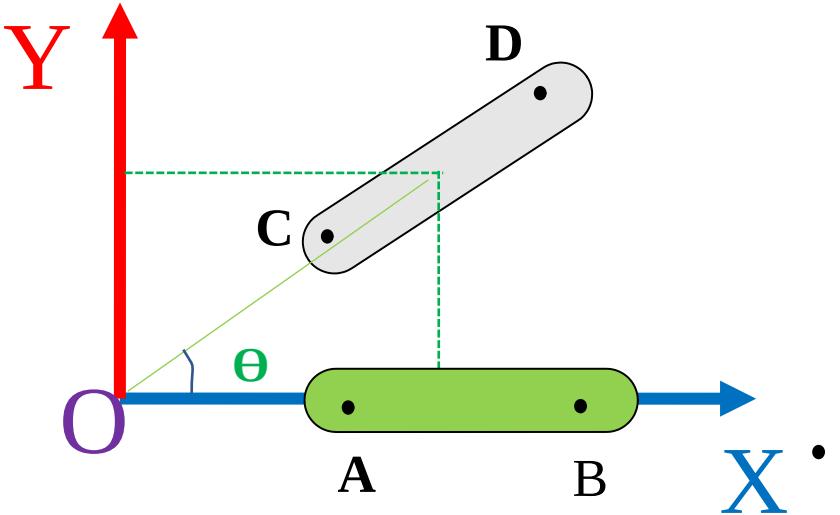
Note : In general, when  $I$  number of links are joined at the same connection, the joint is equivalent to  $(I - 1)$  binary joints.

# Number of Degrees of Freedom for Plane Mechanisms (Mobility)

Link CD, 3 DOF



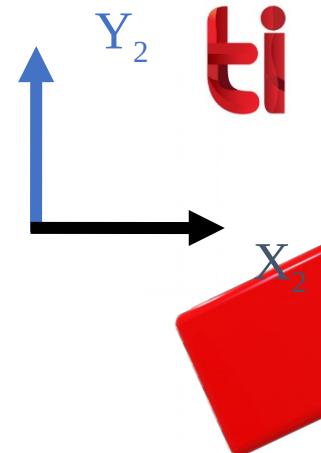
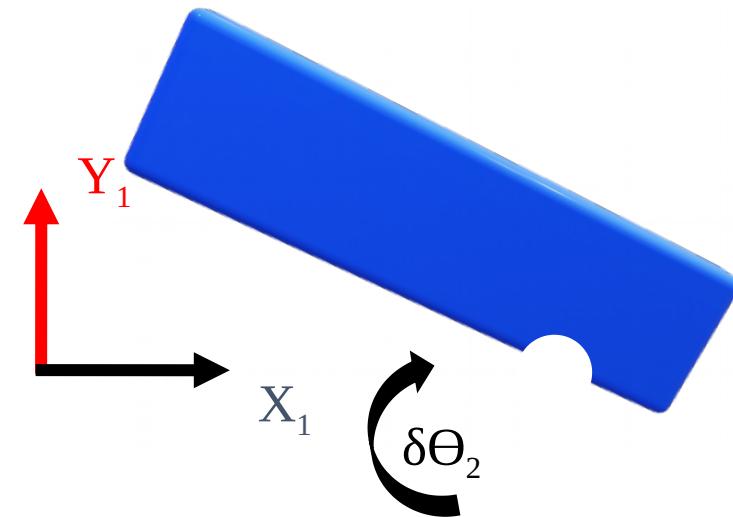
Restricted to 1 DOF



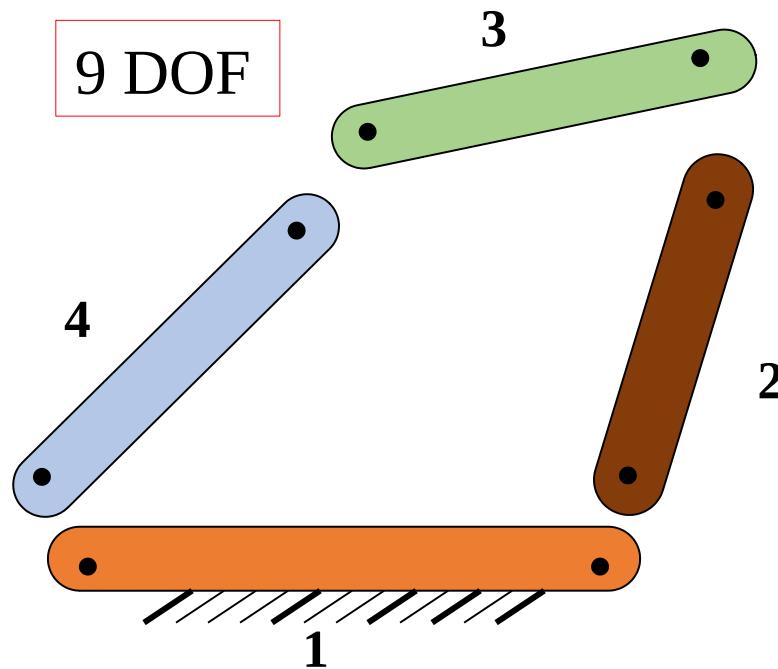
Conti...

Two unconnected links:  
6 DOF  
(each link has 3 DOF)

$$\delta\Theta_1$$



Conti...



# Criterion to plane mechanisms

## **Kutzbach Criterion to plane mechanisms:**

$$M = 3(L - 1) - 2J - h$$

If there is no any higher pair,  $h = 0$

M = degree of freedom or mobility

L = number of links / lower pair

J = number of full joints

h = number of higher pair

$$M = 3(L - 1) - 2J$$

## **Gruebler's Criterion to plane mechanisms:**

- This criterion is used to find out whether an assembly of links with 1 d.o.f.
- Lower pairs is a constrained mechanism or not.

So here ,  $M = 1$

$$3L - 2J - 4 = 0$$

## **Special Note :**

### **1. If $\text{DOF (M)} = 0$ :**

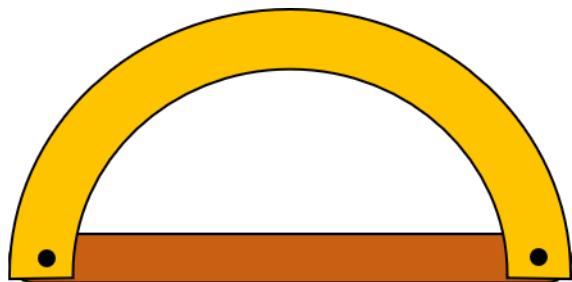
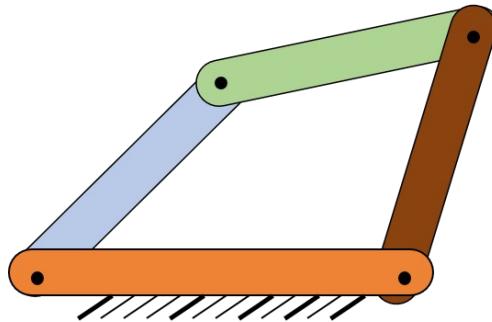
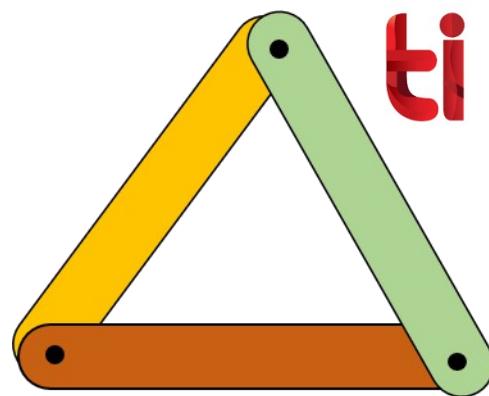
- structure, no relative motion between the link is possible

### **2. If $\text{DOF (M)} = +\text{ve}$**

- $\text{DOF} = 1$  mechanism, then the mechanism can be driven by a single input motion
- $\text{DOF} = 2$  then two separate input motions are necessary to produce constrained motion for the mechanism.

### **3. If $\text{DOF (M)} = -\text{ve}$**

- preloaded structure, there are redundant constraints in the chain and it forms a statically indeterminate structure.
- No motion is possible. Or superstructure



# Reference Books

1. *Uicker, John Joseph, Gordon R. Pennock, and Joseph Edward Shigley. Theory of machines and mechanisms. Vol. 1. New York: Oxford University Press.*
2. *Norton, Robert L. Design of machinery: an introduction to the synthesis and analysis of mechanisms and machines. Boston: McGraw-Hill Higher Education.*
3. *Rattan, Sarjit S. Theory of machines. Tata McGraw-Hill Education.*
4. *Vinogradov, Oleg. Fundamentals of kinematics and dynamics of machines and mechanisms. CRC press.*
5. *Simón Mata, Antonio, et al. Fundamentals of machine theory and mechanisms. Springer.*

Thanks for watching *this* video

