

Thapar Institute of Engineering & Technology – Patiala

Dr. Vishal Gupta
Assistant Professor
MED-TIET- Patiala

Thapar Institute of Engineering & Technology
(Deemed to be University)
Bhadson Road, Patiala, Punjab, Pin-147004
Contact No. : +91-175-2393201
Email : info@thapar.edu

Contact Details
Cabin H Block, first floor
9729002917
vishal.gupta@thapar.edu
<http://www.drvisalgupta.co.in>



THAPAR INSTITUTE
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Mechanics of Machines

UME 306

Module - 1

Lecture - 4

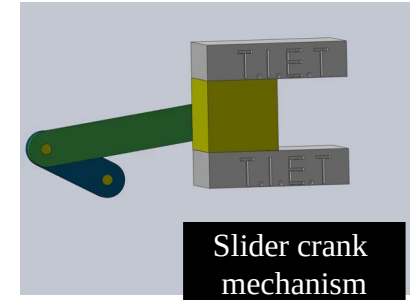
Instructional objective



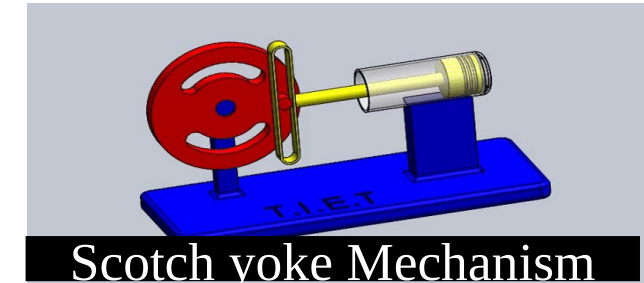
- Kinematic fundamentals
- Types of joint in a chain
- Classification of kinematic pair
- Concept of mobility
- Criterion to plane mechanisms

Kinematic Fundamentals

A Kinematic chain: An assemblage of links and joints, interconnected in a way to provide a controlled output motion in response to a supplied input motion.



Mechanism: When one of the links of a kinematic chain is fixed, the chain is known as mechanism.



Simple Mechanism: A mechanism with four links.

Compound Mechanism: mechanism with more than four links.

Machine : A combination of resistant bodies arranged to compel the mechanical forces of nature to do work accompanied by determinate motion.

Types of joints in a chain

1. *Binary joint.*

$$j + 0.5h = 1 \cdot 5l - 2$$

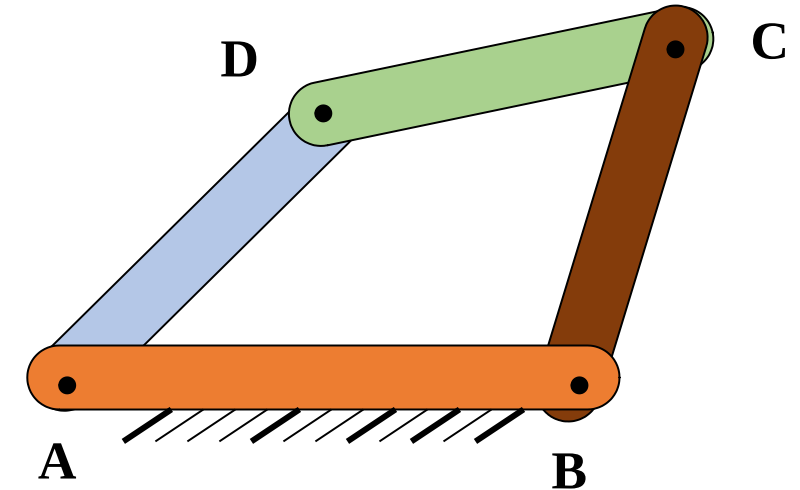
Where:

j = Number of binary joints,

h = Number of higher pairs, and

l = Number of links

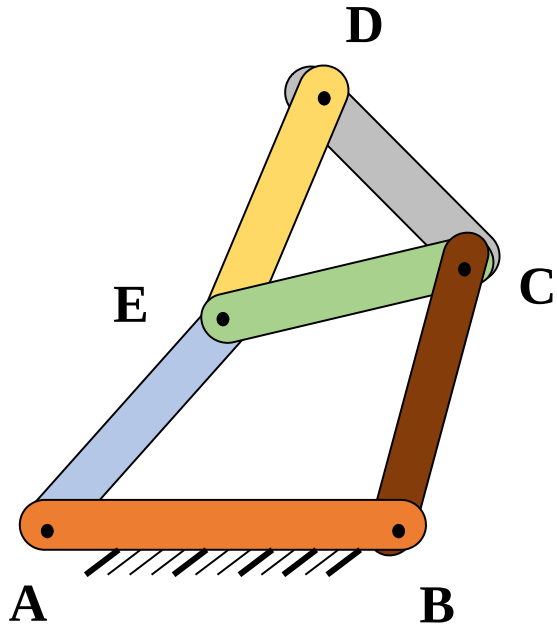
If there is no any higher pair, $h = 0$



$$\begin{aligned} j &= 4 \\ h &= 0 \\ l &= 4 \end{aligned}$$

If LHS = RHS , Kinematic chain or constrained chain chain

2. Ternary joint .



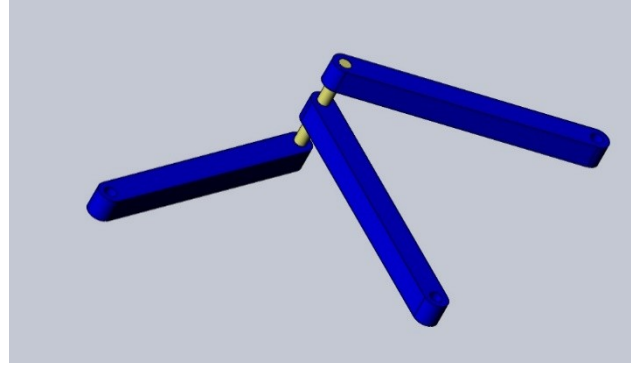
$$1T = 2B$$

$$J = 7$$

$$h = 0$$

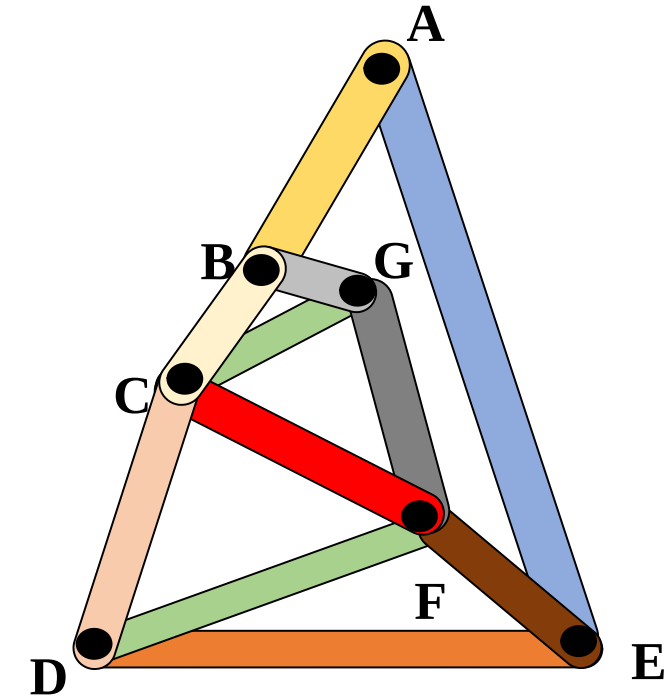
$$L = 6$$

$$\text{LHS} = \text{RHS}$$



$$J + 0.5h = 1 \cdot 5L - 2$$

3. Quaternary joint



$$1Q = 3B$$

$$J = 15$$

$$h = 0$$

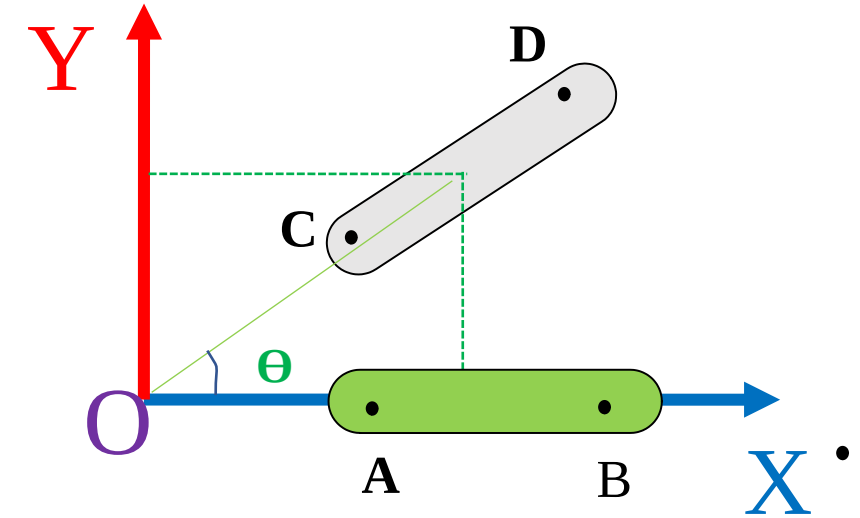
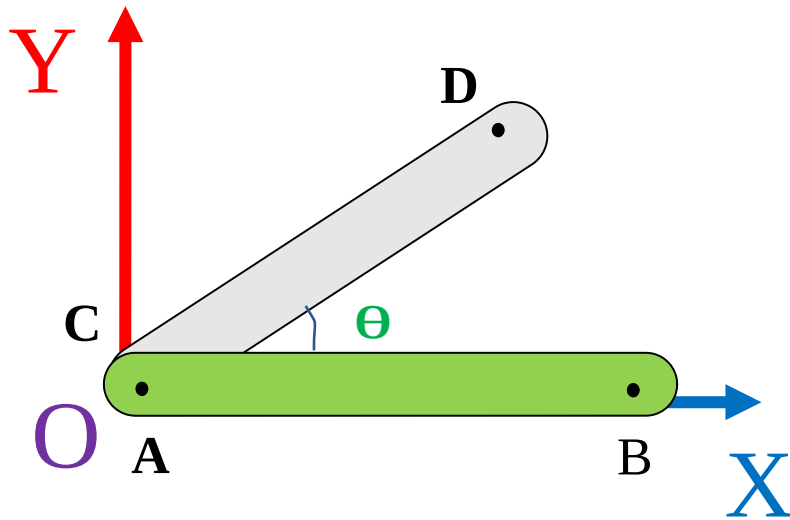
$$L = 11$$

$$\text{L.H.S.} > \text{R.H.S.}$$

Note : In general, when l number of links are joined at the same connection, the joint is equivalent to $(l - 1)$ binary joints.

Number of Degrees of Freedom for Plane Mechanisms (Mobility)

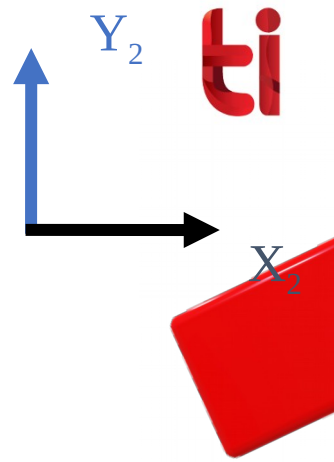
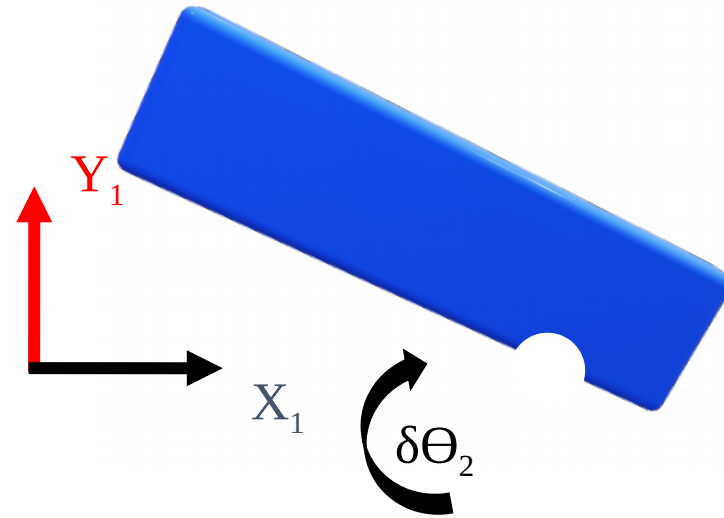
Link CD, 3 DOF



Restricted to 1 DOF

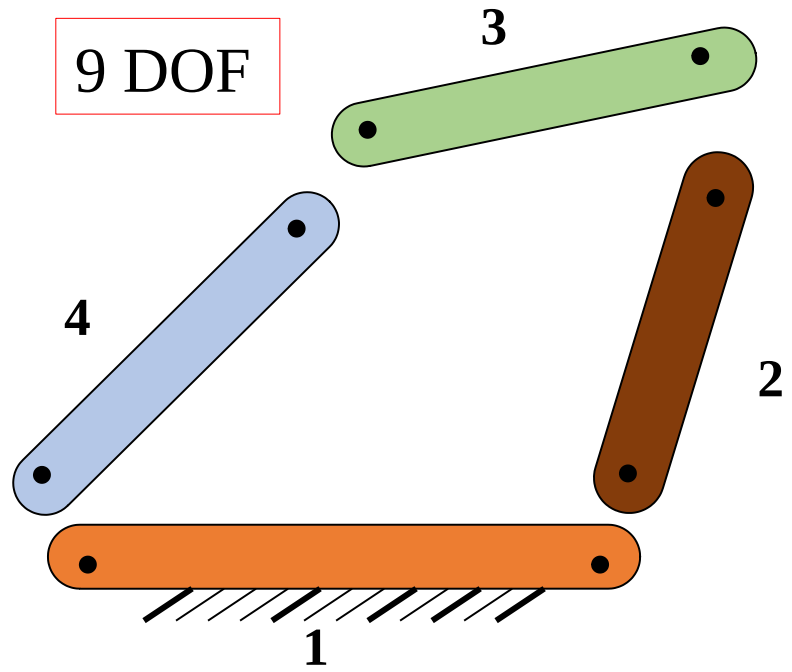
Conti...

Two unconnected links:
6 DOF
(each link has 3 DOF)



Conti...

9 DOF



Criterion to plane mechanisms

Kutzbach Criterion to plane mechanisms:

$$M = 3(L - 1) - 2J - h$$

M = degree of freedom or mobility

L = number of links / lower pair

J = number of full joints

h = number of higher pair

If there is no any higher pair, $h = 0$

$$M = 3(L - 1) - 2J$$

Gruebler's Criterion to plane mechanisms:

- This criterion is used to find out whether an assembly of links with 1 d.o.f.
- Lower pairs is a constrained mechanism or not.

So here , $M = 1$

$$3L - 2J - 4 = 0$$

Special Note :

1. If DOF (M) = 0 :

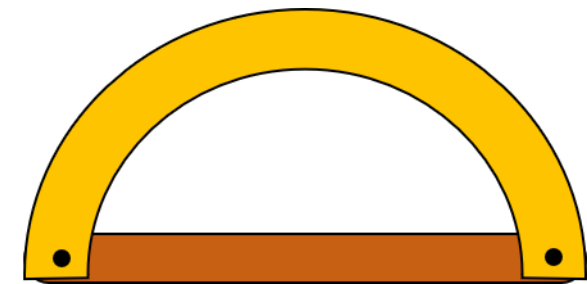
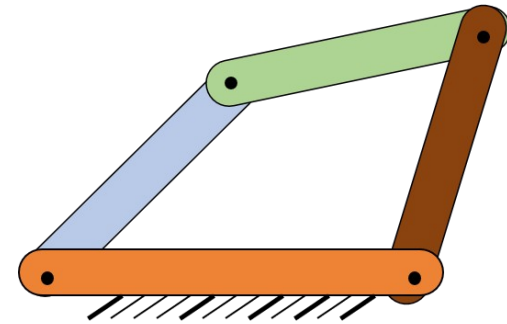
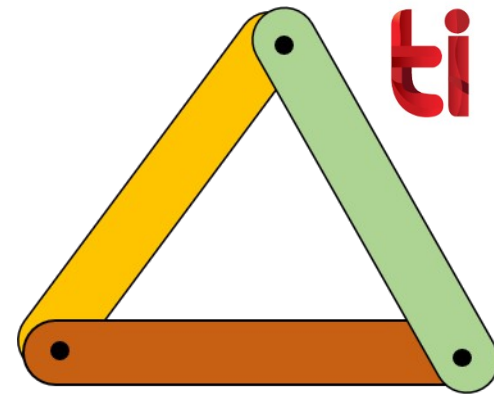
- structure, no relative motion between the link is possible

2. If DOF (M) = +ve

- DOF = 1 mechanism, then the mechanism can be driven by a single input motion
- DOF = 2 then two separate input motions are necessary to produce constrained motion for the mechanism.

3. If DOF (M) = -ve

- preloaded structure, there are redundant constraints in the chain and it forms a statically indeterminate structure.
- No motion is possible. Or superstructure



1. *Uicker, John Joseph, Gordon R. Pennock, and Joseph Edward Shigley. Theory of machines and mechanisms. Vol. 1. New York: Oxford University Press.*
2. *Norton, Robert L. Design of machinery: an introduction to the synthesis and analysis of mechanisms and machines. Boston: McGraw-Hill Higher Education.*
3. *Rattan, Sarjit S. Theory of machines. Tata McGraw-Hill Education.*
4. *Vinogradov, Oleg. Fundamentals of kinematics and dynamics of machines and mechanisms. CRC press.*
5. *Simón Mata, Antonio, et al. Fundamentals of machine theory and mechanisms. Springer.*

Thanks for watching *this* video

