

Array

Address computation

1D array – address calculation

- Let A be a one dimensional array.
- Formula to compute the address of the I^{th} element of an array ($A[I]$) is:

$$\text{Address of } A[I] = B + W * (I - LB)$$

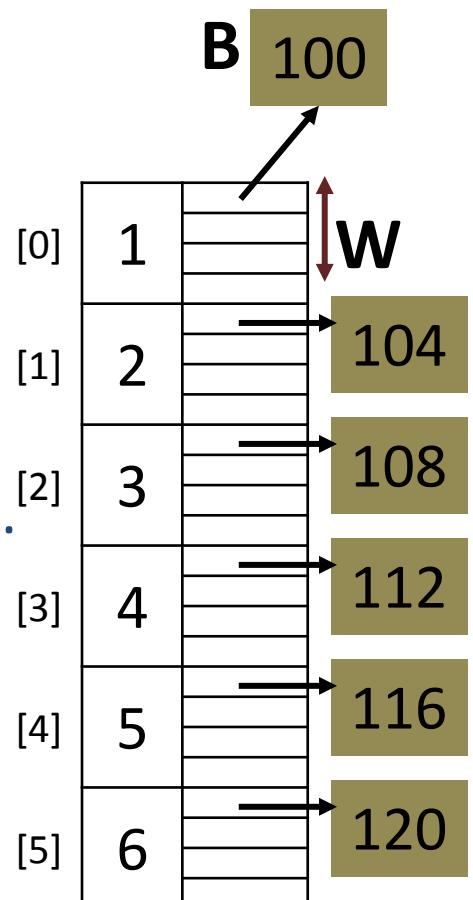
where,

B = Base address/address of first element, i.e. $A[LB]$.

W = Number of bytes used to store a single array element.

I = Subscript of element whose address is to be found.

LB = Lower limit / Lower Bound of subscript, if not specified assume 0 (zero).



Example

- Similarly, for a character array where a single character uses 1 byte of storage.
- If the base address is 1200 then,

$$\text{Address of } A[I] = B + W * (I - LB)$$

$$\text{Address of } A[0] = 1200 + 1 * (0 - 0) = 1200$$

$$\text{Address of } A[1] = 1200 + 1 * (1 - 0) = 1201$$

...

$$\text{Address of } A[10] = 1200 + 1 * (10 - 0) = 1210$$

Example

- If $LB = 5$, $\text{Loc}(A[LB]) = 1200$, and $W = 4$.
- Find $\text{Loc}(A[8])$.

$$\text{Address of } A[I] = B + W * (I - LB)$$

$$\begin{aligned}\text{Loc}(A[8]) &= \text{Loc}(A[5]) + 4 * (8 - 5) \\&= 1200 + 4 * 3 \\&= 1200 + 12 \\&= 1212\end{aligned}$$

Example

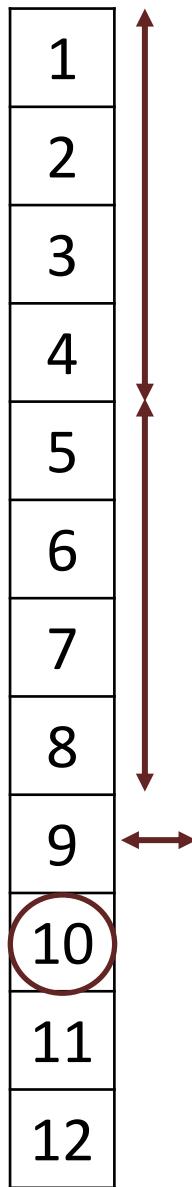
- Base address of an array **B[1300.....1900]** is **1020** and size of each element is 2 bytes in the memory. Find the address of **B[1700]**.

$$\text{Address of } A[I] = B + W * (I - LB)$$

- Given: **B = 1020, LB = 1300, W = 2, I = 1700**

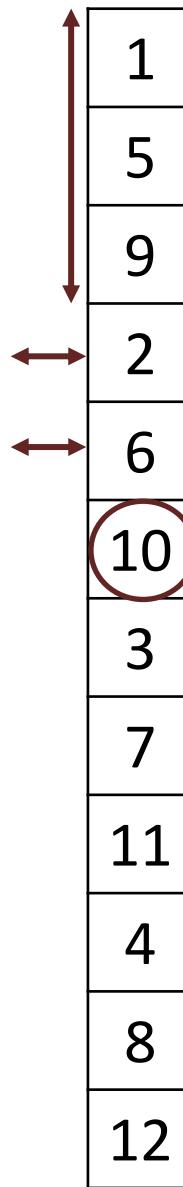
$$\begin{aligned}\text{Address of } B[1700] &= 1020 + 2 * (1700 - 1300) \\ &= 1020 + 2 * 400 \\ &= 1020 + 800 \\ &= 1820\end{aligned}$$

Row-major



| | [0] | [1] | [2] | [3] |
|-----|-----|-----|-----|-----|
| [0] | 1 | 2 | 3 | 4 |
| [1] | 5 | 6 | 7 | 8 |
| [2] | 9 | 10 | 11 | 12 |

Column-major



2D array – address calculation

- If **A** be a two dimensional array with **M** rows and **N** columns. We can compute the address of an element at **Ith** row and **Jth** column of an array (**A[I][J]**).

B = Base address/address of first element, i.e. $A[LBR][LBC]$

I = Row subscript of element whose address is to be found

J = Column subscript of element whose address is to be found

W = Number of bytes used to store a single array element

LBR = Lower limit of row/start row index of matrix, if not given
assume 0

LBC = Lower limit of column/start column index of matrix, if not
given assume 0

N = Number of column of the given matrix

M = Number of row of the given matrix

Contd...

- Row Major

Address of $A[I][J] = B + W * (N * (I - LBR) + (J - LBC))$

- Column Major

Address of $A [I][J] = B + W * ((I - LBR) + M * (J - LBC))$

- Note: **$A[LBR \dots UBR, LBC \dots UBC]$**

$$M = (UBR - LBR) + 1$$

$$N = (UBC - LBC) + 1$$

Example

- Suppose elements of array $A[4][5]$ occupies 4 bytes, and the address of the first element is 49. Find the address of the element $A(4,3)$ when the storage is row major.

$$\text{Address of } A[I][J] = B + W * (N * (I - LBR) + (J - LBC))$$

- Given: $B = 49$, $W = 4$, $M = 4$, $N = 5$, $I = 4$, $J = 3$, $LBR = 0$, $LBC = 0$.

$$\begin{aligned}\text{Address of } A[4][3] &= 49 + 4 * (5 * (4 - 0) + (3 - 0)) \\&= 49 + 4 * (23) \\&= 49 + 92 \\&= 141\end{aligned}$$

Example

- An array $X [-15..10, 15..40]$ requires **one** byte of storage. If beginning location is **1500** determine the location of $X [15][20]$ in column major.

$$\text{Address of } A[I][J] = B + W * [(I - Lr) + M * (J - Lc)]$$

- Number of rows (M) = $(UBR - LBR) + 1 = [10 - (-15)] + 1 = 26$
- Given: $B = 1500, W = 1, I = 15, J = 20, LBR = -15, LCR = 15, M = 26$

$$\begin{aligned}\text{Address of } X[15][20] &= 1500 + 1 * [(15 - (-15)) + 26 * (20 - 15)] \\ &= 1500 + 1 * [30 + 26 * 5] \\ &= 1500 + 1 * [160] \\ &= 1660\end{aligned}$$