

**Department of Chemical Engineering  
Thapar Institute of Engineering &  
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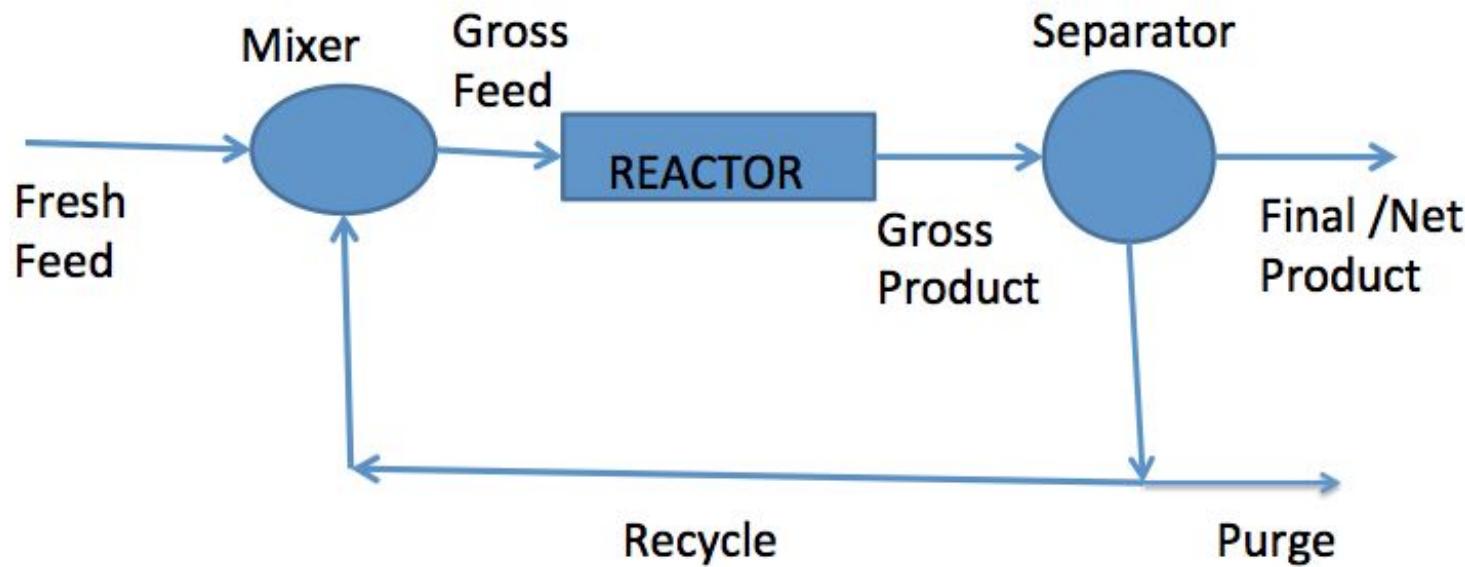
**Course: Material and Energy Balances  
UCH301**

**Course Instructor: Dr. Raj K. Gupta**



# Product separation and recycle

- ✓ In many processes the output from the reactor contains unconverted reactant.
- ✓ This unconverted reactant is required to be separated from the product and sent back to the process to achieve maximum conversion.



- ✓ In a process, where reaction is involved, there are two ways of defining conversion
- ✓ When the reactant passes once through the reactor

**Single pass conversion =**

$(\text{reactant in Gross Feed} - \text{reactant in Gross Product}) / (\text{reactant in Gross Feed})$

- ✓ When reactant is recycled back to the reactor and the conversion is observed at the outlet of the process

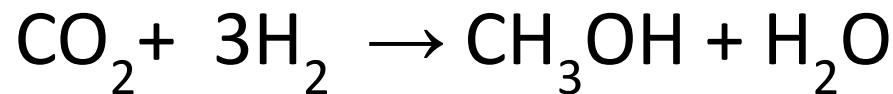
**Overall conversion =**

$(\text{reactant in Fresh Feed} - \text{reactant in Final Product}) / (\text{reactant in Fresh Feed})$



## Problem

$\text{CO}_2$  reacts with  $\text{H}_2$  to produce methanol as per the reaction:



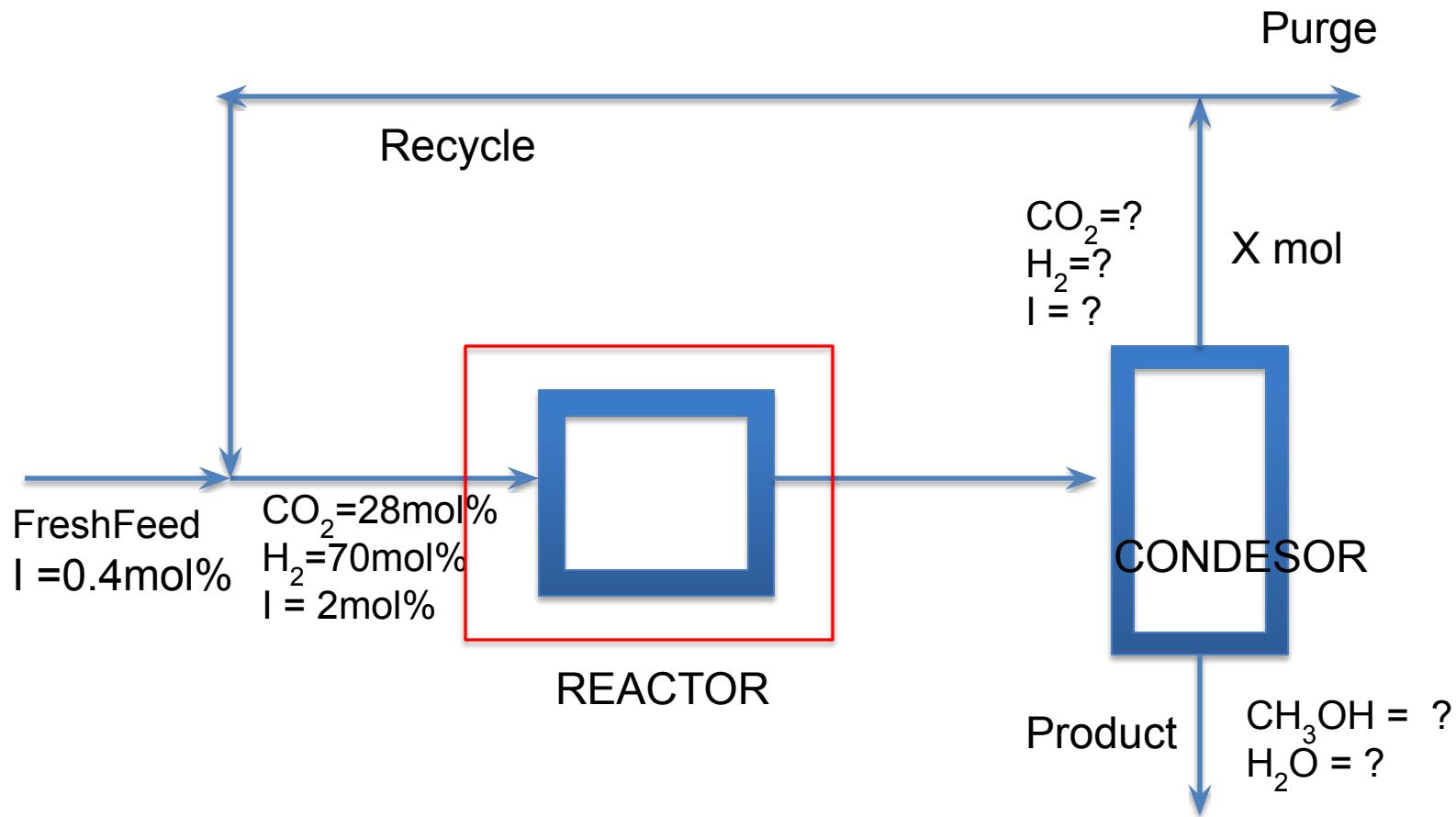
The fresh feed to the process contains hydrogen, carbon dioxide, and 0.4 mol% inert (I). The reactor effluent passes through a condenser that removes all of the methanol and water formed and none of the reactants and inert. The later substances are recycled to the reactor. To avoid the buildup of the inert in the reactor, a purge stream is withdrawn from the recycle stream.



The feed to the reactor contains 28 mol% CO<sub>2</sub>, 70 mol% H<sub>2</sub> and 2 mol% inert. The single pass conversion of hydrogen is 60%. Calculate the molar flow rates and molar compositions of the fresh feed, the feed to the reactor, the recycle stream, and the purge stream.



# SOLUTION



What should be the basis ?  
Where to write M.B. first ?



- Basis: 100 mol of feed to reactor

60% single pass H<sub>2</sub> conversion is given

H<sub>2</sub> Balance: H<sub>2</sub> in – H<sub>2</sub> out = H<sub>2</sub> converted

moles of H<sub>2</sub> exiting the reactor = mol H<sub>2</sub> in - mol H<sub>2</sub> converted

$$70 - 70 * 0.6 = 28 \text{ mol}$$

H<sub>2</sub> consumed = 42 mol

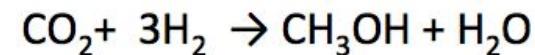
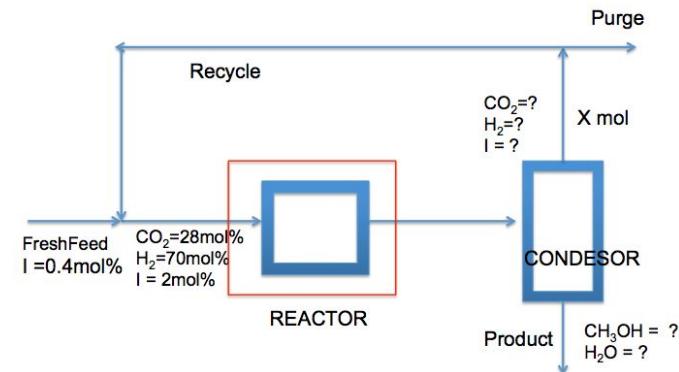
CO<sub>2</sub> Balance: CO<sub>2</sub> out = CO<sub>2</sub> produced

moles of CO<sub>2</sub> exiting the reactor=

$$28 - 42/3 = 14 \text{ mol}$$

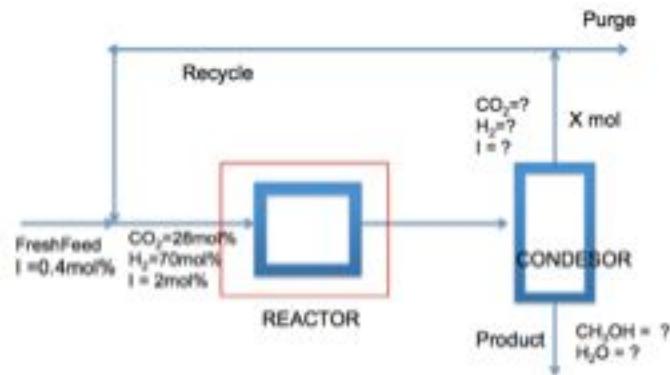
moles of CH<sub>3</sub>OH exiting the reactor=

$$42/3 = 14 \text{ mol}$$



Moles of  $\text{H}_2\text{O}$  exiting the reactor =  $42/3 = 14 \text{ mol}$

M. Balance on condenser:



Total mol balance:

input moles = output moles

(as there is no reaction in the condenser)

$$14 + 28 + 14 + 14 + 2 = \text{Product } (=28) + \text{Purge} + \text{Recycle}$$

$$\text{Purge} + \text{Recycle} = X = 44 \text{ mol}$$



- Composition of X:
- $\text{CO}_2 = 14 \text{ mol}$ ;  $\text{H}_2 = 28 \text{ mol}$ ;  $\text{I} = 2 \text{ mol}$

$$\text{CO}_2 = 14/44 = 0.318 \text{ (or } 31.8\%)$$

$$\text{H}_2 = 28/44 = 0.636 \text{ (or } 63.6\%)$$

$$\text{I} = 2/44 = 0.046 \text{ (or } 4.6\%) \}$$

(composition of purge and recycle will be same  
as that of X ??)



Balance on mixing point:

Total mol balance : Fresh Feed + Recycle = 100

Inerts balance: Fresh Feed \* ( 0.004)+ Recycle\* (0.046) = 2.0

Solving these two equations:

Fresh Feed = 61.4 mol; Recycle = 38.6 mol

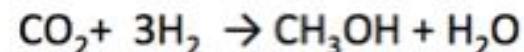
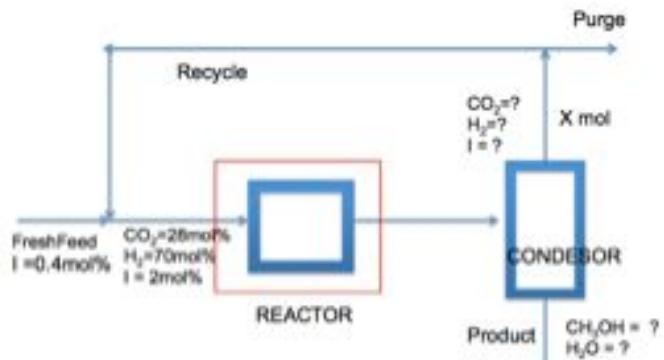
Now, CO<sub>2</sub> balance gives:

$$61.4 * x_{\text{co2,FF}} + 38.6(0.318) = 100 * 0.28$$

$$x_{\text{co2,FF}} = 0.256 \text{ mol CO}_2/\text{mol}$$

And,

$$x_{\text{H2,FF}} = 1 - 0.004 - 0.256 = 0.74 \text{ mol H}_2/\text{m}$$



- Balance on splitting point:

X = Recycle + Purge

$$\text{Purge} = 44 - 38.6 = 5.4 \text{ mol}$$



## Problem

Scale the above process for a methanol production rate of 155 kmol/hr.

Solution

Scaling all streams :

For 100 kmol fed the methanol produced is 14 kmol

A scaling factor of  $155/14 = 11.1$  is required



- Fresh feed Calculated = 61.4 kmol
- Fresh feed scaled up = 681 kmol/h  
( 25.6 mol% CO<sub>2</sub>, 74 mol% H<sub>2</sub>, 0.4 mol% I)
- Feed to reactor Calculated = 100 kmol
- Feed to reactor scaled up = 1110 kmol/h  
( 28 mol% CO<sub>2</sub>, 70 mol% H<sub>2</sub>, 2 mol% I)
- Recycle = 38.6 kmol, Scaled up = 428 kmol/h  
( 31.8 mol% CO<sub>2</sub>, 63.6 mol% H<sub>2</sub>, 4.6 mol% I)
- Purge = 5.4 kmol, Scaled up = 59.9 kmol/h  
( 31.8 mol% CO<sub>2</sub>, 63.6 mol% H<sub>2</sub>, 4.6 mol% I)



# TRY Yourself

- Ammonia is burned to form nitric oxide in the following reaction:



- (i) If ammonia is fed to a continuous reactor at a rate of 100 kmol  $\text{NH}_3/\text{h}$ , what oxygen feed rate (kmol/h) would correspond to 40% excess  $\text{O}_2$ .
- (ii) If 50 kg of ammonia and 100 kg of oxygen are fed to a batch reactor, determine the excess reactant and its percentage excess. Also, find the mass of NO produced (kg) if the reaction proceeds to completion.

