

Changing the Order

$$4 + 7 = 7 + 4$$

&

$$3 \times 5 = 5 \times 3$$

Numbers can be added or multiplied in any order.

+

x

Using this property can make calculations easier by changing the order of operations.

$$1. \quad 18 + 5 + 5 + 2 =$$

$$(18 + 2) + (5 + 5) = 20 + 10 = 30$$

$$2. \quad 20 + 35 + 80 + 65 + 7 =$$

$$(35 + 65) + (20 + 80) + 7 =$$

$$3. \quad 2 \times 48 \times 5 =$$

$$(2 \times 5) \times 48 = 10 \times 48 = 480$$

$$4. \quad 25 \times 11 \times 7 \times 4 = (4 \times 25) \times (11 \times 7)$$

$$= 100 \times 77$$

$$= 7700$$

Multiplying & dividing by 4 or 8

This strategy involves repeated doubling & halving.

Examples:

$$76 \times 4$$

$$\text{Double } 70 = 140$$

$$\text{Double } 6 = 12$$

$$140 + 12 = 156$$

$$\text{Double } 156 = 312$$

Or

Double twice.

$$\text{Double } 76 = 152$$

$$\text{Double } 152 = 312$$

$$13 \times 4$$

$$\text{Double } 13 = 26 \quad \times 4 = \text{Double, Double}$$

$$\text{Double } 26 = 52$$

$$12 \times 8$$

$$\text{Double } 12 = 24 \quad \times 8 = \text{Double, Double, Double}$$

$$\text{Double } 24 = 48$$

$$\text{Double } 48 = 96$$

$$144 / 4$$

$$\text{Half } 144 = 72$$

$$\text{Half } 72 = 36 \quad /4 = \text{Half, Half}$$

$$848 / 8$$

$$\text{Half } 848 = 424$$

$$\text{Half } 424 = 212 \quad /8 = \text{Half, Half, Half}$$

$$\text{Half } 212 = 106$$

Multiplying by a multiple of ten

By adding zeroes to the end of a number all the digits in the number shift one place value or more to the left.

$$43 \times 10 = 430$$

$$79 \times 100 = 7\,900$$

$$87 \times 1000 = 87\,000$$

$$100 \times 1000 = 100\,000$$

$$9 \times 70 = 9 \times 7 \times 10 = 630$$

$$40 \times 300 = 4 \times 3 \times 10 \times 100 = 12\,000$$