

Computational and Numerical Methods

Group 16

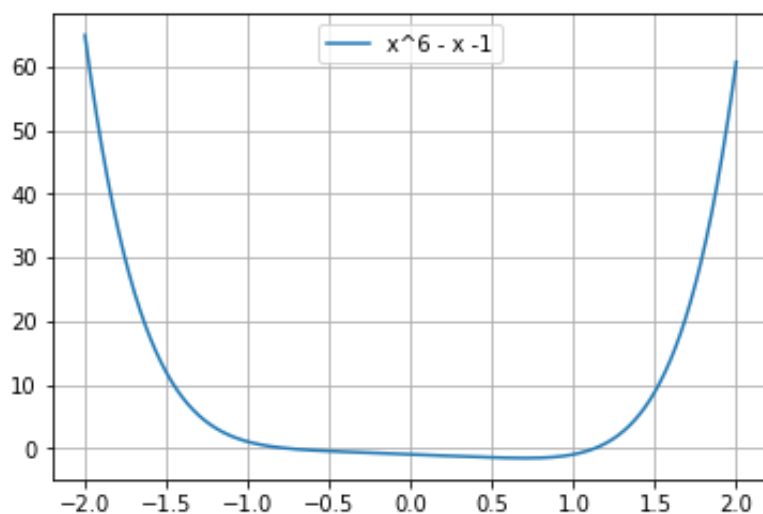
Set 5 (20-08-2018): The Secant Method

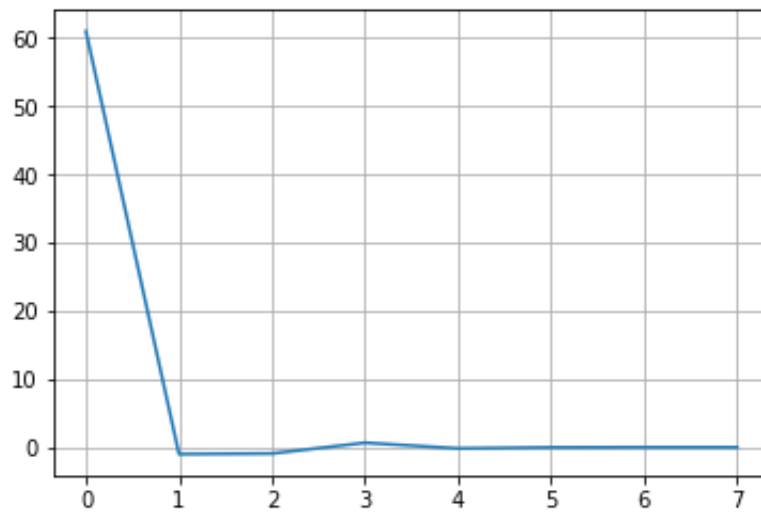
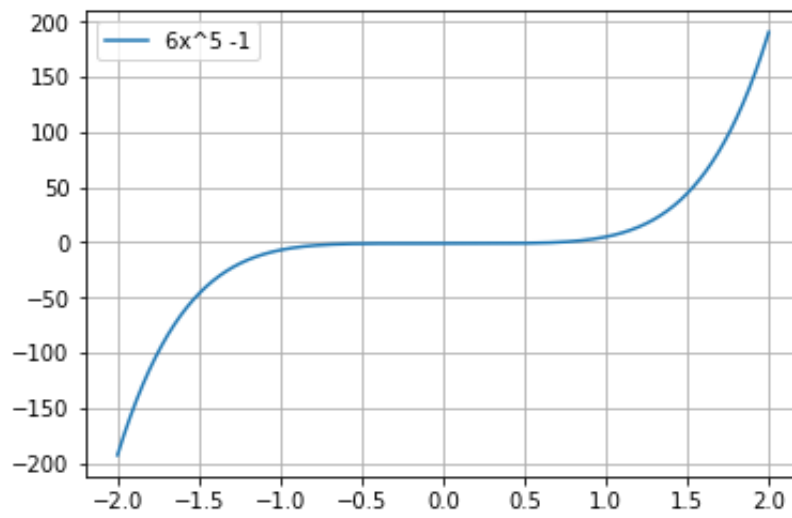
Vidhin Parmar 201601003

Parth Shah 201601086

Write a code, applying the algorithm of the secant method to determine both the real roots of $f(x) = x^6 - x - 1 = 0$.

Opposite Side



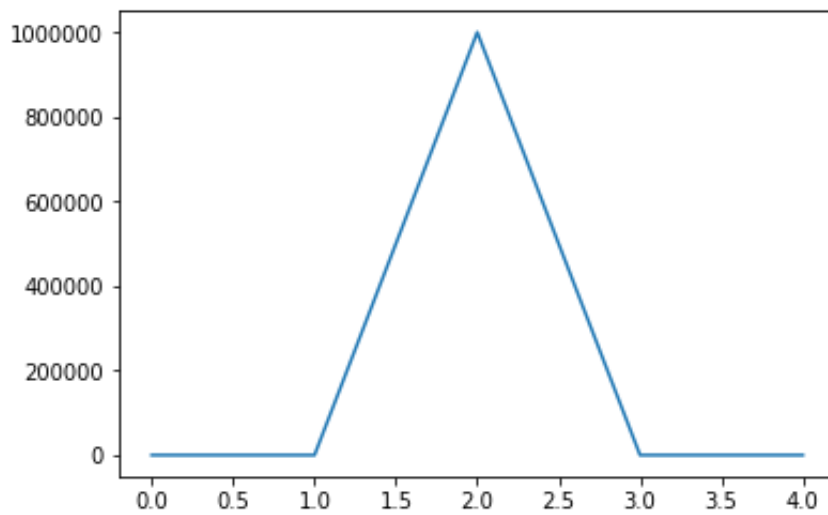


Steps taken to converge in Bisection Method are 14
 Steps taken to converge in Newton Raphson are 6
 Steps taken to converge in Secant Method are 8

Out[3]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|---|---------|--------------|-----------------|-----------|
| 0 | 0 | 2 | 61 | 0 | 0 |
| 1 | 1 | 1 | -1 | -1 | 1.01613 |
| 2 | 2 | 1.01613 | -0.915368 | 0.016129 | 1.19058 |
| 3 | 3 | 1.19058 | 0.657466 | 0.174449 | 1.11766 |
| 4 | 4 | 1.11766 | -0.168491 | -0.0729219 | 1.13253 |
| 5 | 5 | 1.13253 | -0.0224373 | 0.0148757 | 1.13482 |
| 6 | 6 | 1.13482 | 0.000953564 | 0.00228526 | 1.13472 |
| 7 | 7 | 1.13472 | -5.06617e-06 | -9.31621e-05 | 1.13472 |

Same Side



Steps taken to converge in Bisection Method are 14

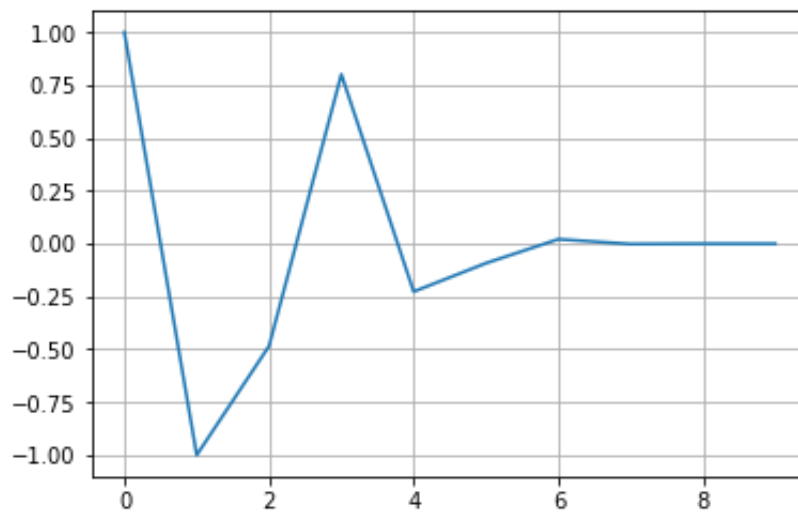
Steps taken to converge in Newton Raphson are 6

Steps taken to converge in Secant Method are 5

Out[4]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|-----|-----------|---------------|-------------------|-------------|
| 0 | 0.0 | 0.100000 | -1.099999e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | -1.000000e+00 | 0.900000 | 10.000090 |
| 2 | 2.0 | 10.000090 | 1.000043e+06 | 9.000090 | 1.000009 |
| 3 | 3.0 | 1.000009 | -9.999550e-01 | -9.000081 | 1.000018 |
| 4 | 4.0 | 1.000018 | -9.999100e-01 | 0.000009 | 1.199984 |

Opposite Side



Steps taken to converge in Bisection Method are 14

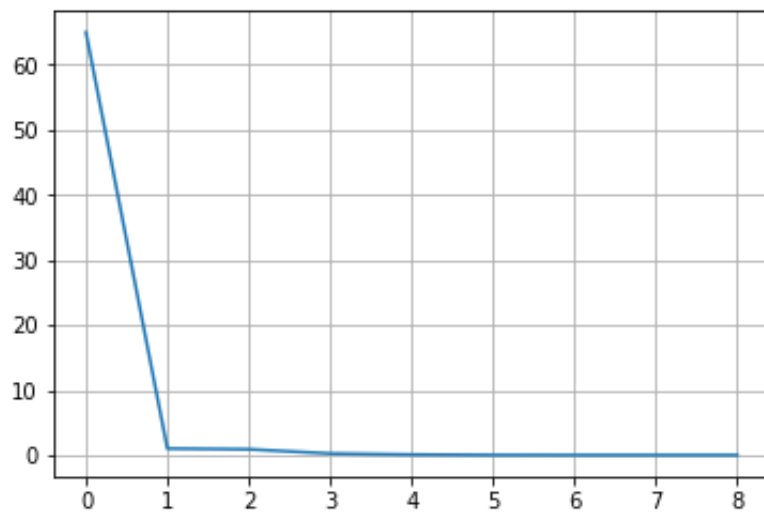
Steps taken to converge in Newton Raphson are 6

Steps taken to converge in Secant Method are 10

Out[5]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|---|-----------|--------------|-----------------|-----------|
| 0 | 0 | -1 | 1 | 0 | 0 |
| 1 | 1 | 0 | -1 | 1 | -0.5 |
| 2 | 2 | -0.5 | -0.484375 | -0.5 | -0.969697 |
| 3 | 3 | -0.969697 | 0.801109 | -0.469697 | -0.676984 |
| 4 | 4 | -0.676984 | -0.226751 | 0.292713 | -0.741558 |
| 5 | 5 | -0.741558 | -0.092151 | -0.0645741 | -0.785767 |
| 6 | 6 | -0.785767 | 0.0211428 | -0.0442092 | -0.777517 |
| 7 | 7 | -0.777517 | -0.00155185 | 0.00825029 | -0.778081 |
| 8 | 8 | -0.778081 | -2.41324e-05 | -0.000564151 | -0.77809 |
| 9 | 9 | -0.77809 | 2.80499e-08 | -8.91153e-06 | -0.77809 |

Same Side



Steps taken to converge in Bisection Method are 14

Steps taken to converge in Newton Raphson are 6

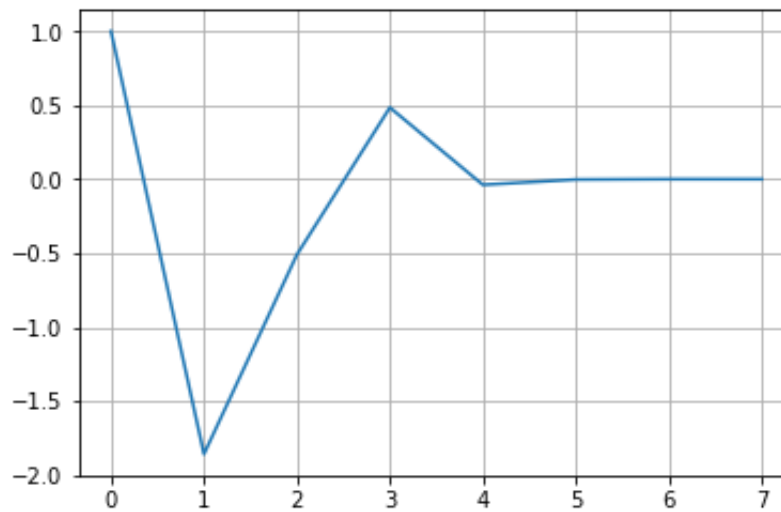
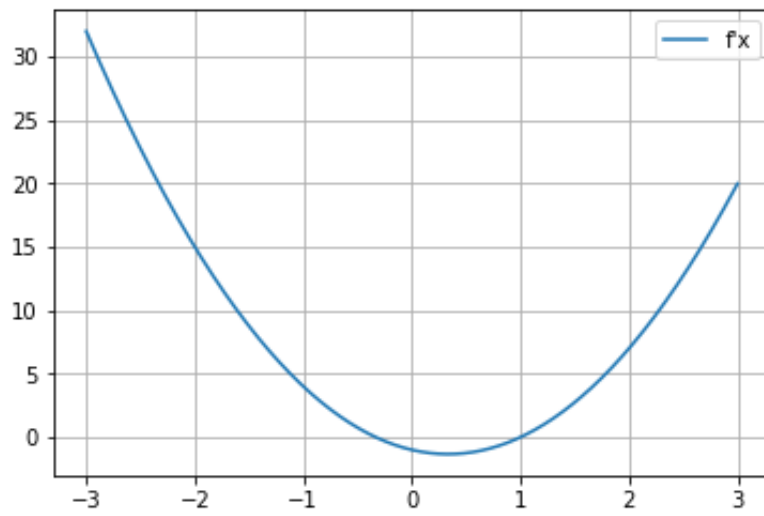
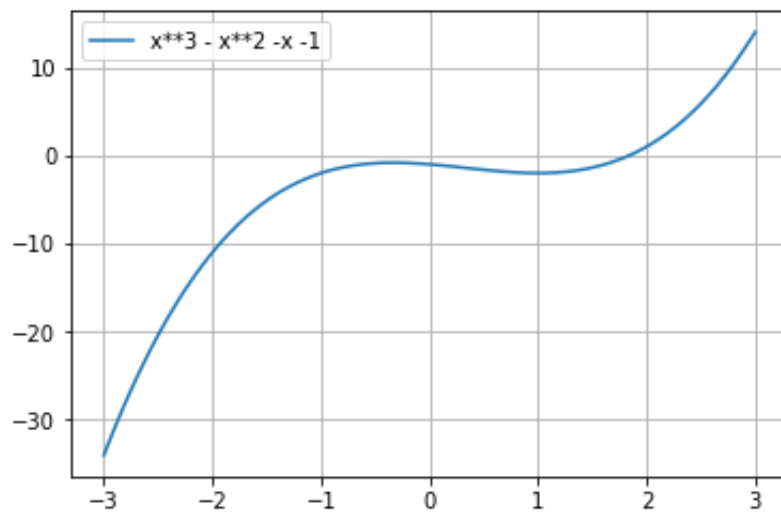
Steps taken to converge in Secant Method are 9

Out[6]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|---|-----------|-------------|-----------------|-----------|
| 0 | 0 | -2 | 65 | 0 | 0 |
| 1 | 1 | -1 | 1 | 1 | -0.984375 |
| 2 | 2 | -0.984375 | 0.894212 | 0.015625 | -0.852299 |
| 3 | 3 | -0.852299 | 0.235612 | 0.132076 | -0.80505 |
| 4 | 4 | -0.80505 | 0.0772799 | 0.0472496 | -0.781988 |
| 5 | 5 | -0.781988 | 0.0106528 | 0.023062 | -0.7783 |
| 6 | 6 | -0.7783 | 0.000571935 | 0.0036873 | -0.778091 |
| 7 | 7 | -0.778091 | 4.51339e-06 | 0.000209198 | -0.77809 |
| 8 | 8 | -0.77809 | 1.92984e-09 | 1.66401e-06 | -0.77809 |

$$A. x^3 - x^2 - x - 1 = 0$$

Opposite Side

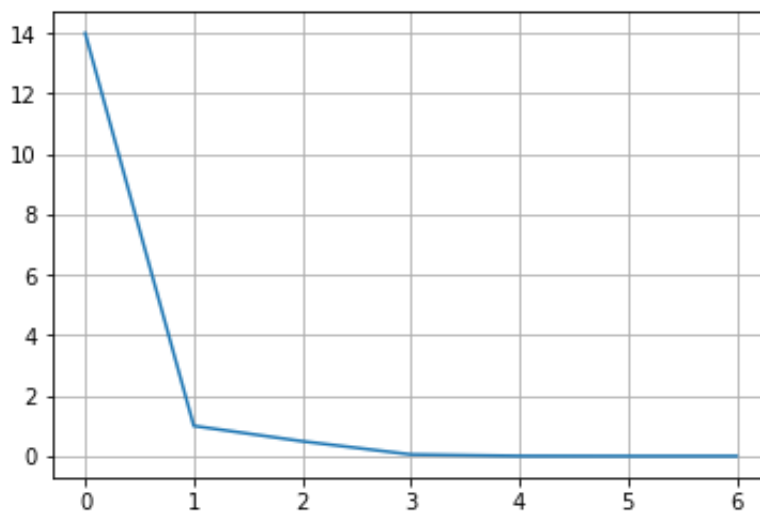


Steps taken to converge in Bisection Method are 14
 Steps taken to converge in Newton Raphson are 7
 Steps taken to converge in Secant Method are 8

Out[7]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|---|---------|--------------|-------------------|-------------|
| 0 | 0 | 2 | 1 | 0 | 0 |
| 1 | 1 | 1.25 | -1.85938 | -0.75 | 1.7377 |
| 2 | 2 | 1.7377 | -0.510118 | 0.487705 | 1.92209 |
| 3 | 3 | 1.92209 | 0.484525 | 0.184388 | 1.83227 |
| 4 | 4 | 1.83227 | -0.0381561 | -0.0898218 | 1.83883 |
| 5 | 5 | 1.83883 | -0.00250775 | 0.00655706 | 1.83929 |
| 6 | 6 | 1.83929 | 1.46016e-05 | 0.000461269 | 1.83929 |
| 7 | 7 | 1.83929 | -5.53187e-09 | -2.67024e-06 | 1.83929 |

Opposite Side



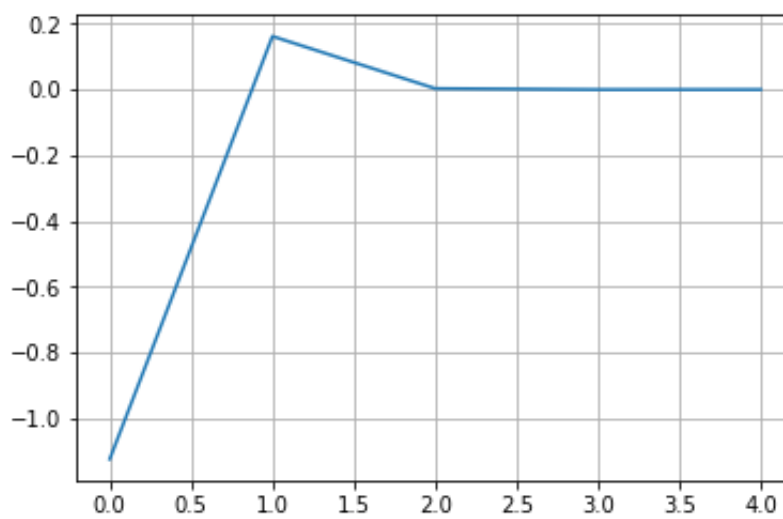
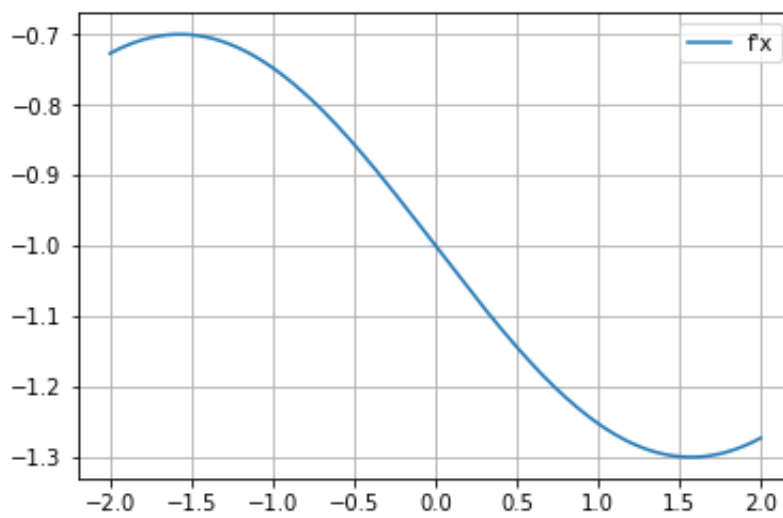
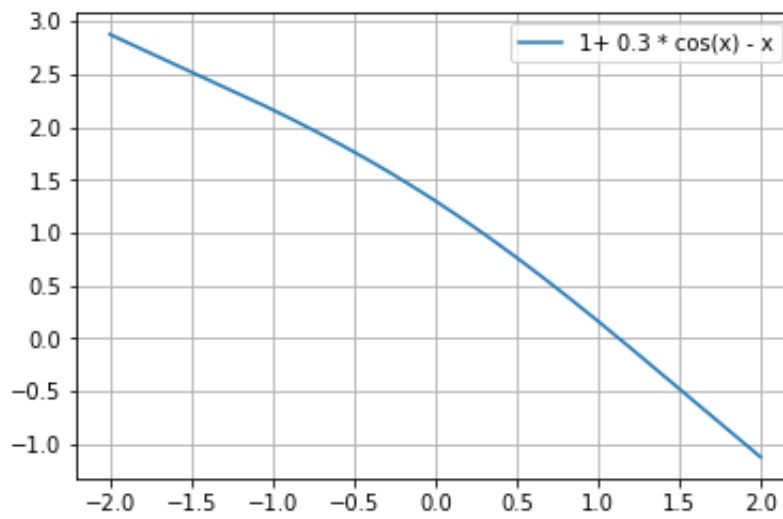
Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 7
Steps taken to converge in Secant Method are 7

Out[8]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|---|---------|-------------|-------------------|-------------|
| 0 | 0 | 3 | 14 | 0 | 0 |
| 1 | 1 | 2 | 1 | -1 | 1.92308 |
| 2 | 2 | 1.92308 | 0.490669 | -0.0769231 | 1.84897 |
| 3 | 3 | 1.84897 | 0.0534081 | -0.0741046 | 1.83992 |
| 4 | 4 | 1.83992 | 0.00347129 | -0.00905131 | 1.83929 |
| 5 | 5 | 1.83929 | 2.75806e-05 | -0.00062919 | 1.83929 |
| 6 | 6 | 1.83929 | 1.44411e-08 | -5.03917e-06 | 1.83929 |

$$B. x = 1 + 0.3\cos x$$

Opposite Side



Steps taken to converge in Bisection Method are 14

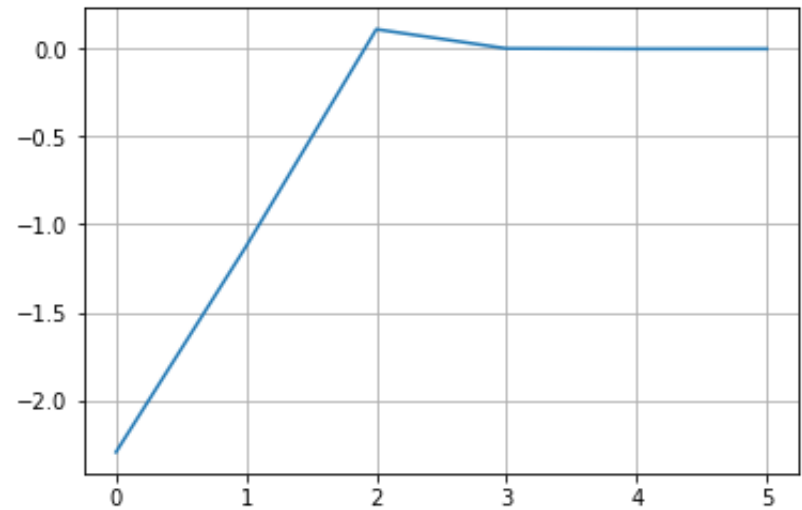
Steps taken to converge in Newton Raphson are 4

Steps taken to converge in Secant Method are 5

Out[9]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 2.000000 | -1.124844e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | 1.620907e-01 | -1.000000 | 1.125951 |
| 2 | 2.0 | 1.125951 | 3.144505e-03 | 0.125951 | 1.128443 |
| 3 | 3.0 | 1.128443 | -2.241347e-05 | 0.002492 | 1.128425 |
| 4 | 4.0 | 1.128425 | 2.806499e-09 | -0.000018 | 1.128425 |

Same Side



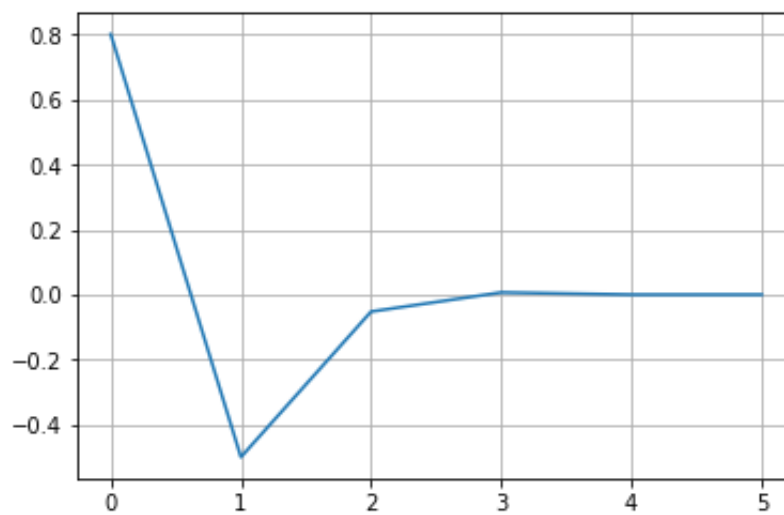
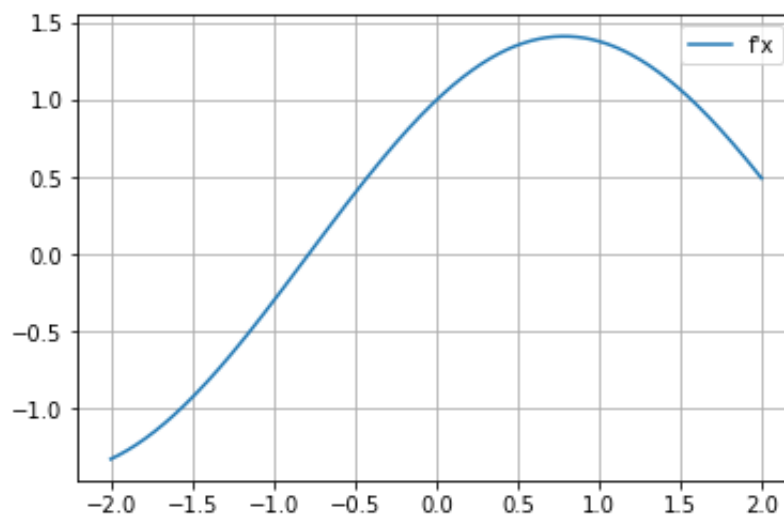
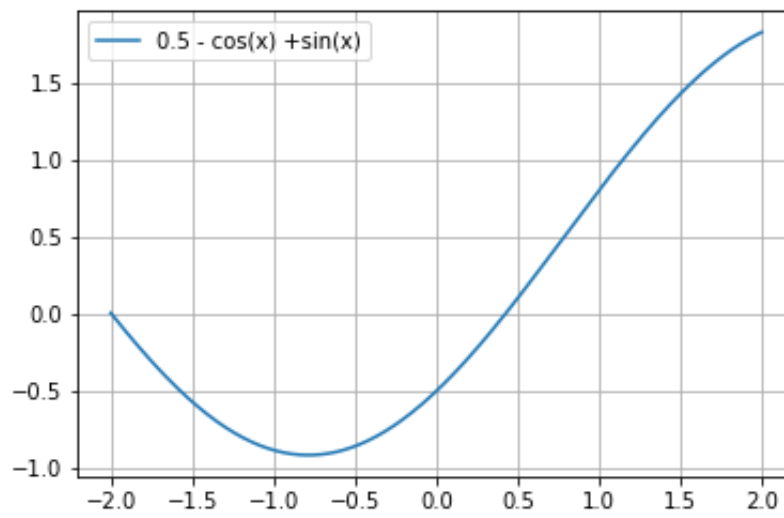
Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 4
Steps taken to converge in Secant Method are 6

Out[10]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 3.000000 | -2.296998e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 2.000000 | -1.124844e+00 | -1.000000 | 1.040361 |
| 2 | 2.0 | 1.040361 | 1.114113e-01 | -0.959639 | 1.126844 |
| 3 | 3.0 | 1.126844 | 2.009717e-03 | 0.086483 | 1.128433 |
| 4 | 4.0 | 1.128433 | -9.545113e-06 | 0.001589 | 1.128425 |
| 5 | 5.0 | 1.128425 | 7.633283e-10 | -0.000008 | 1.128425 |

$C. \cos x = 0.5 + \sin x$

Opposite Side

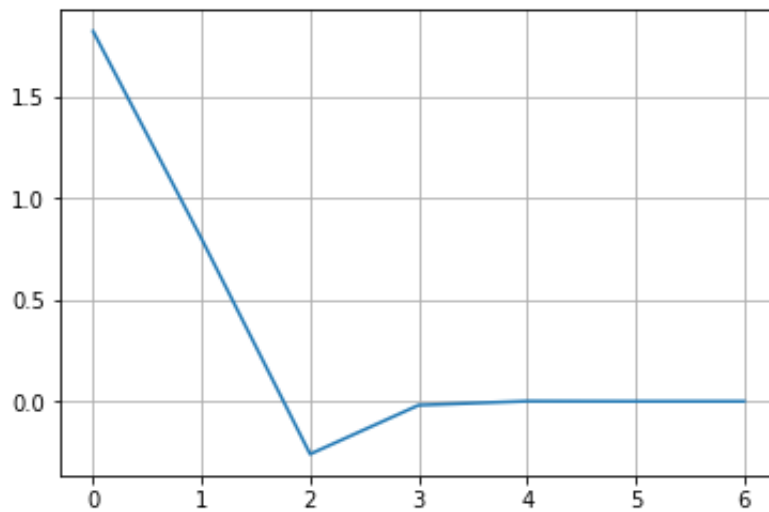


Steps taken to converge in Bisection Method are 14
 Steps taken to converge in Newton Raphson are 5
 Steps taken to converge in Secant Method are 6

Out[11]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 1.000000 | 8.011687e-01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 0.000000 | -5.000000e-01 | -1.000000 | 0.384270 |
| 2 | 2.0 | 0.384270 | -5.218996e-02 | 0.384270 | 0.429055 |
| 3 | 3.0 | 0.429055 | 6.651850e-03 | 0.044785 | 0.423992 |
| 4 | 4.0 | 0.423992 | -5.181144e-05 | -0.005063 | 0.424031 |
| 5 | 5.0 | 0.424031 | -4.892623e-08 | 0.000039 | 0.424031 |

Same Side



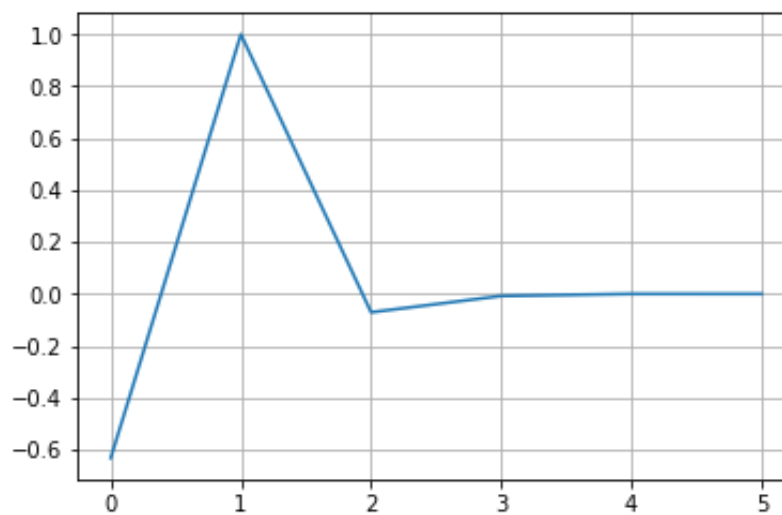
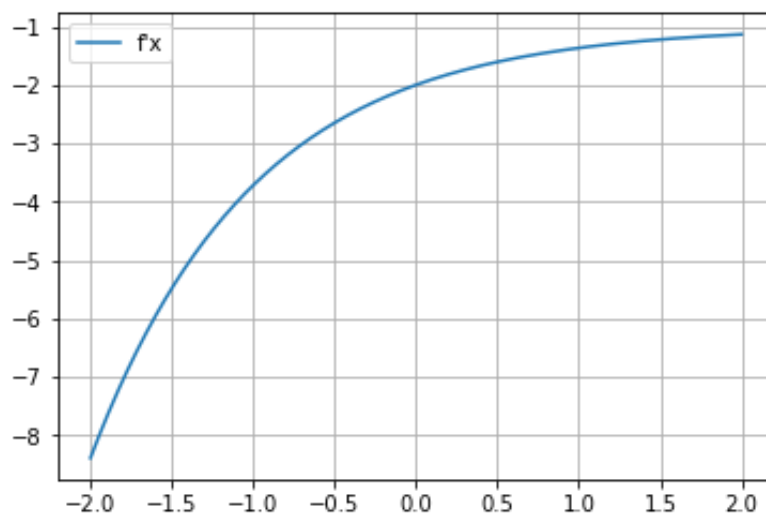
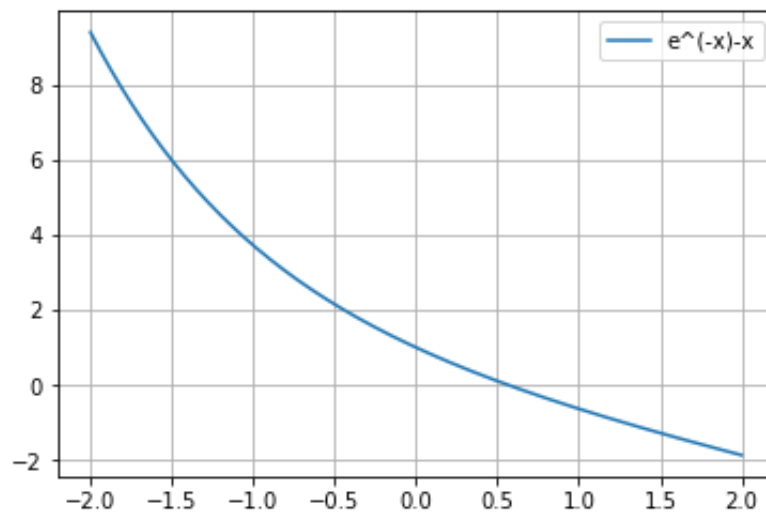
Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 5
Steps taken to converge in Secant Method are 7

Out[12]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 2.000000 | 1.825444e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | 8.011687e-01 | -1.000000 | 0.217819 |
| 2 | 2.0 | 0.217819 | -2.602702e-01 | -0.782181 | 0.409614 |
| 3 | 3.0 | 0.409614 | -1.901947e-02 | 0.191795 | 0.424734 |
| 4 | 4.0 | 0.424734 | 9.305833e-04 | 0.015121 | 0.424029 |
| 5 | 5.0 | 0.424029 | -2.572486e-06 | -0.000705 | 0.424031 |
| 6 | 6.0 | 0.424031 | -3.416855e-10 | 0.000002 | 0.424031 |

$$D. x = e^{-x}$$

Opposite Side



Steps taken to converge in Bisection Method are 14

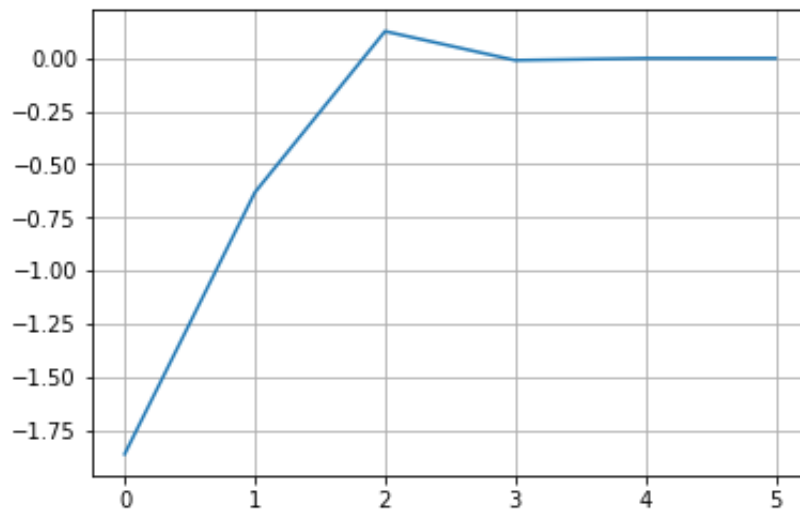
Steps taken to converge in Newton Raphson are 5

Steps taken to converge in Secant Method are 6

Out[13]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 1.000000 | -6.321206e-01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 0.000000 | 1.000000e+00 | -1.000000 | 0.612700 |
| 2 | 2.0 | 0.612700 | -7.081395e-02 | 0.612700 | 0.572181 |
| 3 | 3.0 | 0.572181 | -7.888273e-03 | -0.040518 | 0.567102 |
| 4 | 4.0 | 0.567102 | 6.458283e-05 | -0.005079 | 0.567143 |
| 5 | 5.0 | 0.567143 | -5.883093e-08 | 0.000041 | 0.567143 |

Same Side



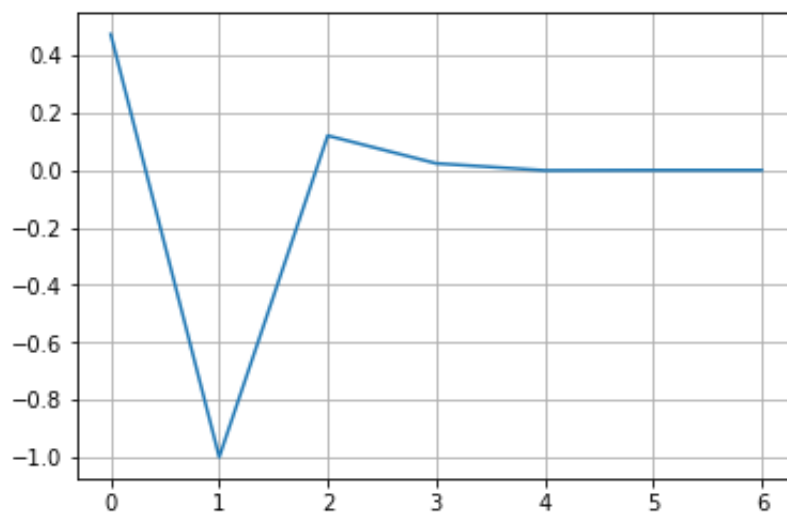
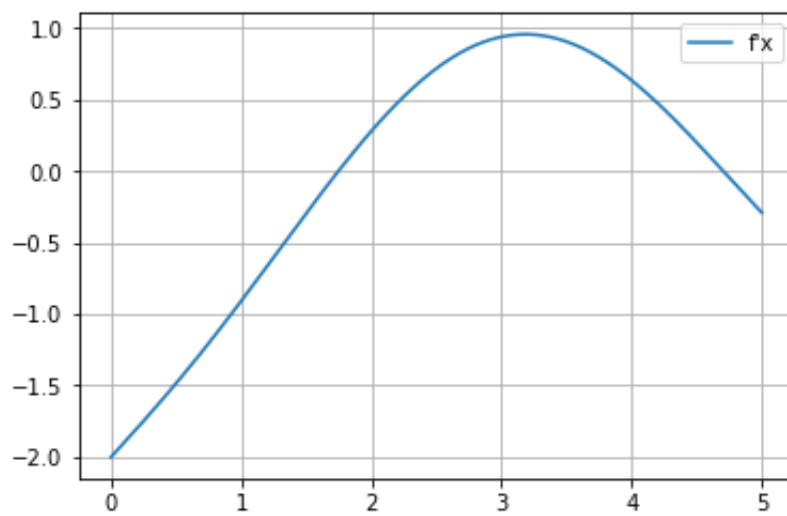
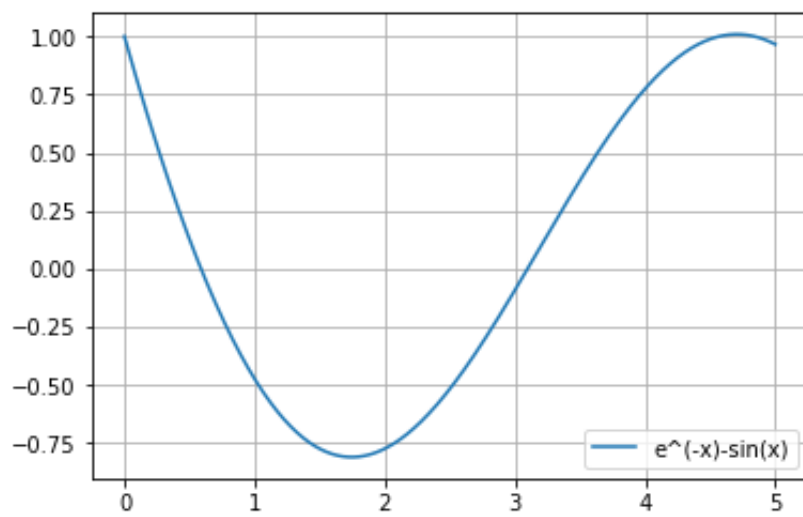
Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 6
Steps taken to converge in Secant Method are 6

Out[14]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 2.000000 | -1.864665e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | -6.321206e-01 | -1.000000 | 0.487142 |
| 2 | 2.0 | 0.487142 | 1.272383e-01 | -0.512858 | 0.573076 |
| 3 | 3.0 | 0.573076 | -9.287930e-03 | 0.085935 | 0.567230 |
| 4 | 4.0 | 0.567230 | -1.361124e-04 | -0.005846 | 0.567143 |
| 5 | 5.0 | 0.567143 | 1.459943e-07 | -0.000087 | 0.567143 |

E. The two smallest positive roots of $e^{-x} = \sin x$

Opposite Side

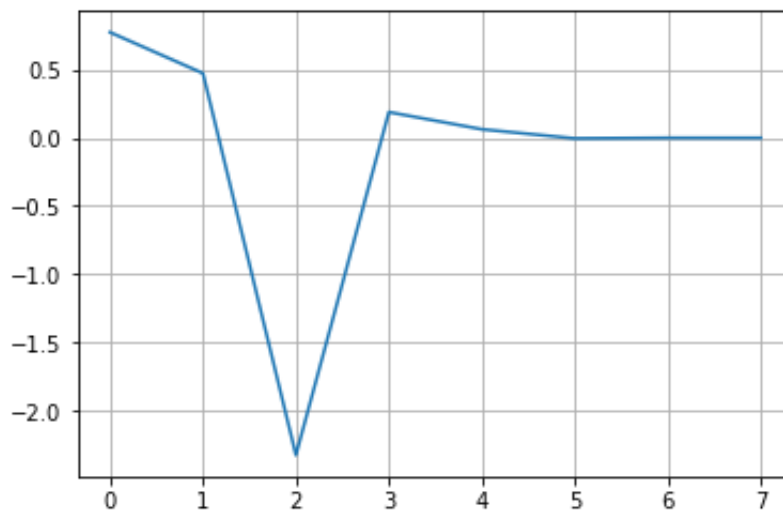


Steps taken to converge in Bisection Method are 14
 Steps taken to converge in Newton Raphson are 5
 Steps taken to converge in Secant Method are 7

Out[15]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|-----|----------|---------------|-------------------|-------------|
| 0 | 0.0 | 1.000000 | 4.735915e-01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 0.000000 | -1.000000e+00 | -1.000000 | 0.678614 |
| 2 | 2.0 | 0.678614 | 1.203952e-01 | 0.678614 | 0.605692 |
| 3 | 3.0 | 0.605692 | 2.363407e-02 | -0.072922 | 0.587880 |
| 4 | 4.0 | 0.587880 | -9.050872e-04 | -0.017811 | 0.588537 |
| 5 | 5.0 | 0.588537 | 6.264769e-06 | 0.000657 | 0.588533 |
| 6 | 6.0 | 0.588533 | 1.635542e-09 | -0.000005 | 0.588533 |

Same Side



Steps taken to converge in Bisection Method are 14

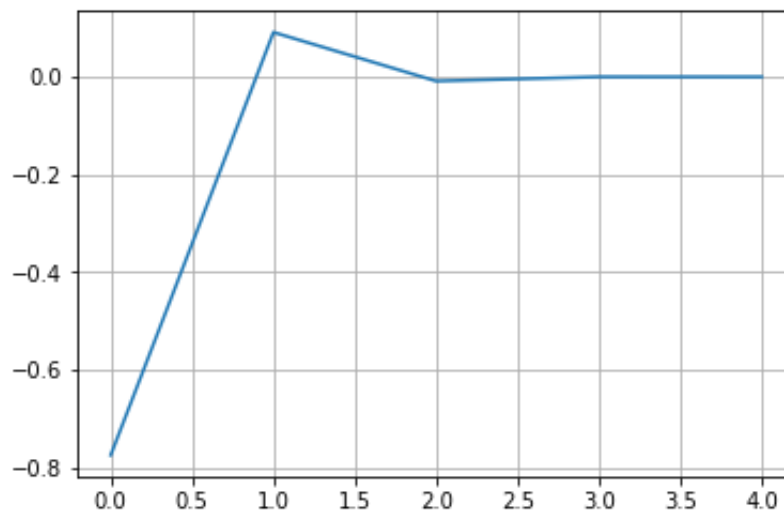
Steps taken to converge in Newton Raphson are 5

Steps taken to converge in Secant Method are 8

Out[16]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|-----|-----------|---------------|-------------------|-------------|
| 0 | 0.0 | 2.000000 | 7.739621e-01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | 4.735915e-01 | -1.000000 | -0.576691 |
| 2 | 2.0 | -0.576691 | -2.325391e+00 | -1.576691 | 0.733222 |
| 3 | 3.0 | 0.733222 | 1.889081e-01 | 1.309913 | 0.634803 |
| 4 | 4.0 | 0.634803 | 6.297963e-02 | -0.098418 | 0.585582 |
| 5 | 5.0 | 0.585582 | -4.096841e-03 | -0.049221 | 0.588589 |
| 6 | 6.0 | 0.588589 | 7.740651e-05 | 0.003006 | 0.588533 |
| 7 | 7.0 | 0.588533 | 9.129174e-08 | -0.000056 | 0.588533 |

Opposite Side



Steps taken to converge in Bisection Method are 14

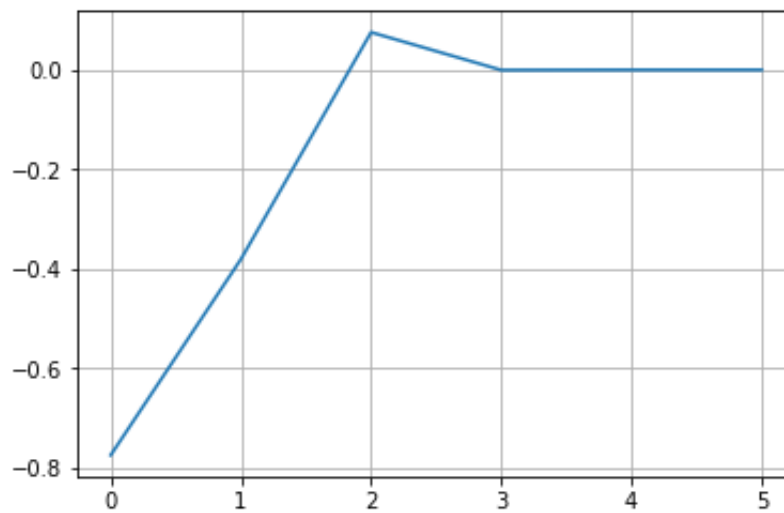
Steps taken to converge in Newton Raphson are 5

Steps taken to converge in Secant Method are 5

Out[17]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|----------|---------------|-----------------|-----------|
| 0 | 0.0 | 4.000000 | -7.751181e-01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 3.000000 | 9.133294e-02 | -1.000000 | 3.105410 |
| 2 | 2.0 | 3.105410 | -8.631751e-03 | 0.105410 | 3.096308 |
| 3 | 3.0 | 3.096308 | 5.295739e-05 | -0.009102 | 3.096364 |
| 4 | 4.0 | 3.096364 | 2.191577e-08 | 0.000056 | 3.096364 |

Same Side



Steps taken to converge in Bisection Method are 14

Steps taken to converge in Newton Raphson are 5

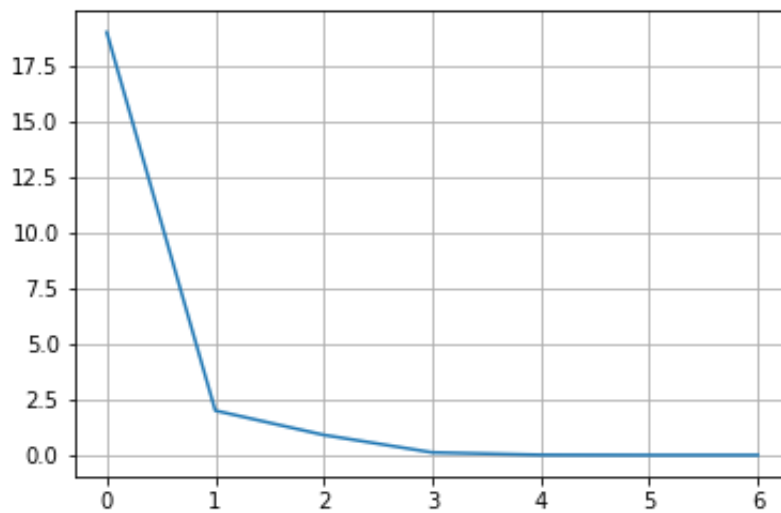
Steps taken to converge in Secant Method are 6

Out[18]:

| | n | x_(n) | f(x_n) | x_(n) - x_(n-1) | x_(n+1) |
|---|-----|----------|---------------|-----------------|----------|
| 0 | 0.0 | 4.000000 | -7.751181e-01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 3.500000 | -3.809806e-01 | -0.500000 | 3.016691 |
| 2 | 2.0 | 3.016691 | 7.561441e-02 | -0.483309 | 3.096729 |
| 3 | 3.0 | 3.096729 | -3.483647e-04 | 0.080038 | 3.096362 |
| 4 | 4.0 | 3.096362 | 1.725728e-06 | -0.000367 | 3.096364 |
| 5 | 5.0 | 3.096364 | 2.983775e-11 | 0.000002 | 3.096364 |

$$F. x^3 - 2x - 2 = 0$$

Same Side



Steps taken to converge in Bisection Method are 14

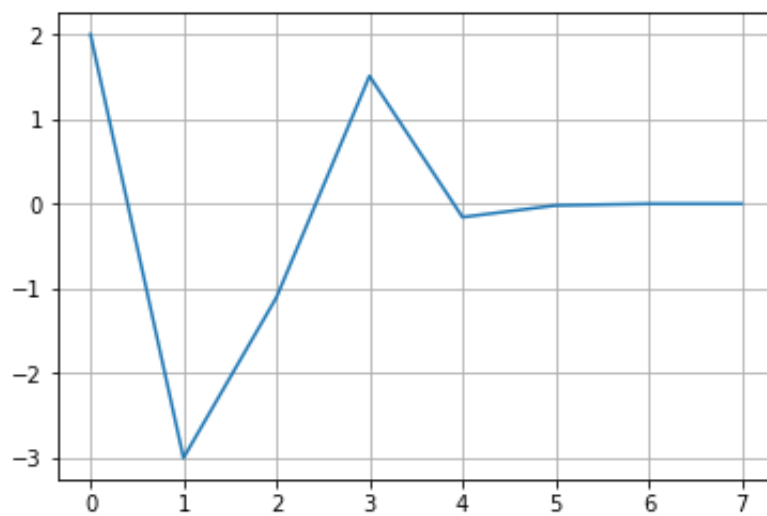
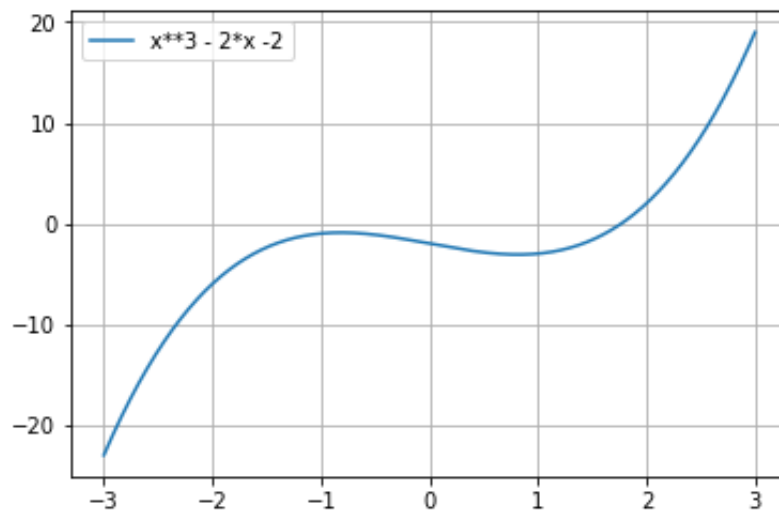
Steps taken to converge in Newton Raphson are 5

Steps taken to converge in Secant Method are 7

Out[19]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|---|---------|-------------|-----------------|-----------|
| 0 | 0 | 3 | 19 | 0 | 0 |
| 1 | 1 | 2 | 2 | -1 | 1.88235 |
| 2 | 2 | 1.88235 | 0.904946 | -0.117647 | 1.78513 |
| 3 | 3 | 1.78513 | 0.118395 | -0.0972228 | 1.7705 |
| 4 | 4 | 1.7705 | 0.00890179 | -0.0146344 | 1.76931 |
| 5 | 5 | 1.76931 | 0.000100254 | -0.00118977 | 1.76929 |
| 6 | 6 | 1.76929 | 8.65786e-08 | -1.35521e-05 | 1.76929 |

Opposite Side



Steps taken to converge in Bisection Method are 14

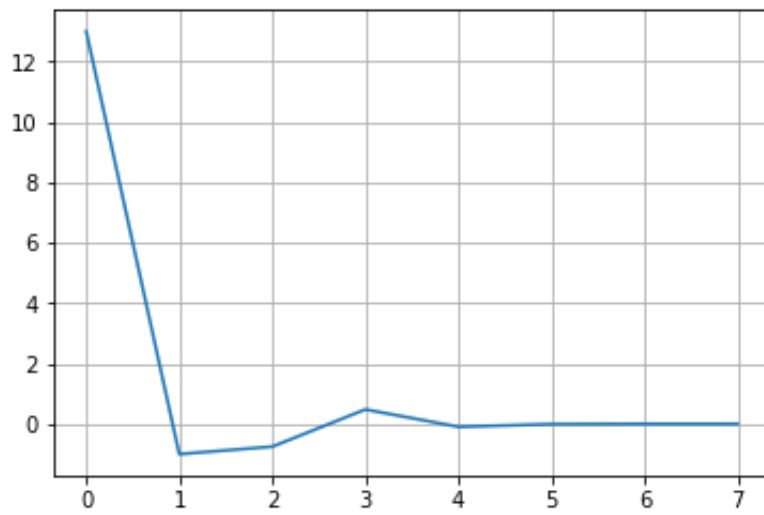
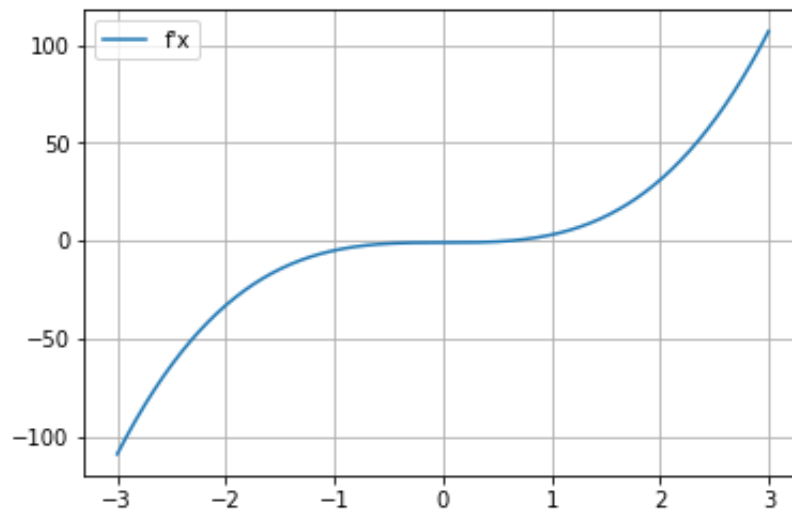
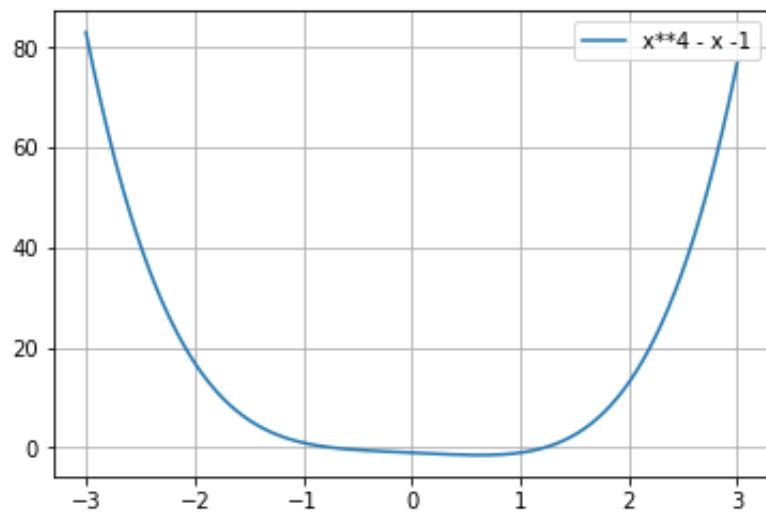
Steps taken to converge in Newton Raphson are 5

Steps taken to converge in Secant Method are 8

Out[20]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|---|---------|-------------|-------------------|-------------|
| 0 | 0 | 2 | 2 | 0 | 0 |
| 1 | 1 | 1 | -3 | -1 | 1.6 |
| 2 | 2 | 1.6 | -1.104 | 0.6 | 1.94937 |
| 3 | 3 | 1.94937 | 1.50892 | 0.349367 | 1.74761 |
| 4 | 4 | 1.74761 | -0.157752 | -0.201754 | 1.76671 |
| 5 | 5 | 1.76671 | -0.0190577 | 0.0190962 | 1.76933 |
| 6 | 6 | 1.76933 | 0.000301132 | 0.00262397 | 1.76929 |
| 7 | 7 | 1.76929 | -5.5937e-07 | -4.08165e-05 | 1.76929 |

Opposite Side



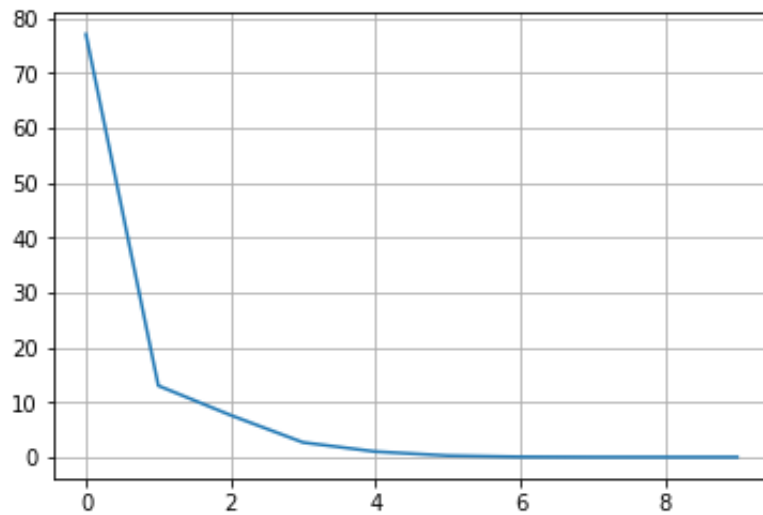
Steps taken to converge in Bisection Method are 14
 Steps taken to converge in Newton Raphson are 8
 Steps taken to converge in Secant Method are 8

Out[21]:

| | n | x_(n) | f(x_n) | x_(n) - x_(n-1) | x_(n+1) |
|---|---|---------|--------------|-----------------|---------|
| 0 | 0 | 2 | 13 | 0 | 0 |
| 1 | 1 | 1 | -1 | -1 | 1.07143 |
| 2 | 2 | 1.07143 | -0.753618 | 0.0714286 | 1.28991 |
| 3 | 3 | 1.28991 | 0.478548 | 0.218482 | 1.20506 |
| 4 | 4 | 1.20506 | -0.0962846 | -0.0848537 | 1.21927 |
| 5 | 5 | 1.21927 | -0.00923606 | 0.014213 | 1.22078 |
| 6 | 6 | 1.22078 | 0.000210003 | 0.00150804 | 1.22074 |
| 7 | 7 | 1.22074 | -4.41665e-07 | -3.35264e-05 | 1.22074 |

G. All real roots of $x^4 - x - 1 = 0$

Same Side



Steps taken to converge in Bisection Method are 14

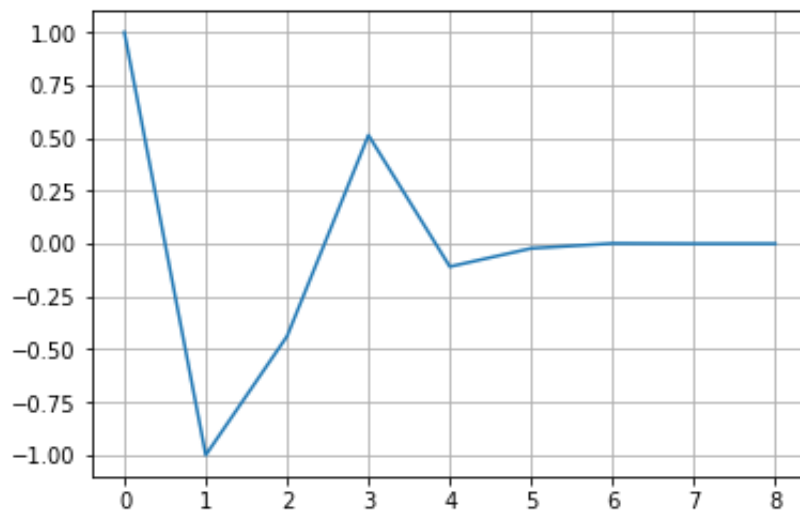
Steps taken to converge in Newton Raphson are 8

Steps taken to converge in Secant Method are 10

Out[22]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|---|---------|-------------|-----------------|-----------|
| 0 | 0 | 3 | 77 | 0 | 0 |
| 1 | 1 | 2 | 13 | -1 | 1.79688 |
| 2 | 2 | 1.79688 | 7.62801 | -0.203125 | 1.50845 |
| 3 | 3 | 1.50845 | 2.66903 | -0.28843 | 1.35321 |
| 4 | 4 | 1.35321 | 0.999965 | -0.155239 | 1.2602 |
| 5 | 5 | 1.2602 | 0.261873 | -0.0930064 | 1.2272 |
| 6 | 6 | 1.2272 | 0.0409049 | -0.0329983 | 1.22109 |
| 7 | 7 | 1.22109 | 0.00219036 | -0.00610855 | 1.22075 |
| 8 | 8 | 1.22075 | 2.00186e-05 | -0.000345605 | 1.22074 |
| 9 | 9 | 1.22074 | 9.94345e-09 | -3.18776e-06 | 1.22074 |

Opposite Side



Steps taken to converge in Bisection Method are 14

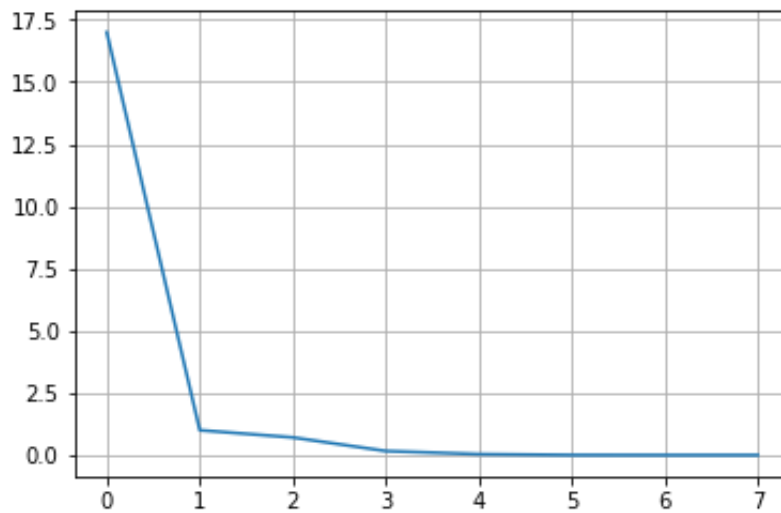
Steps taken to converge in Newton Raphson are 8

Steps taken to converge in Secant Method are 9

Out[23]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|---|-----------|--------------|-----------------|-----------|
| 0 | 0 | -1 | 1 | 0 | 0 |
| 1 | 1 | 0 | -1 | 1 | -0.5 |
| 2 | 2 | -0.5 | -0.4375 | -0.5 | -0.888889 |
| 3 | 3 | -0.888889 | 0.513184 | -0.388889 | -0.678965 |
| 4 | 4 | -0.678965 | -0.108521 | 0.209924 | -0.715608 |
| 5 | 5 | -0.715608 | -0.0221517 | -0.036643 | -0.725006 |
| 6 | 6 | -0.725006 | 0.00129622 | -0.00939808 | -0.724486 |
| 7 | 7 | -0.724486 | -1.44153e-05 | 0.000519533 | -0.724492 |
| 8 | 8 | -0.724492 | -9.25098e-09 | -5.71421e-06 | -0.724492 |

Same Side



Steps taken to converge in Bisection Method are 14

Steps taken to converge in Newton Raphson are 8

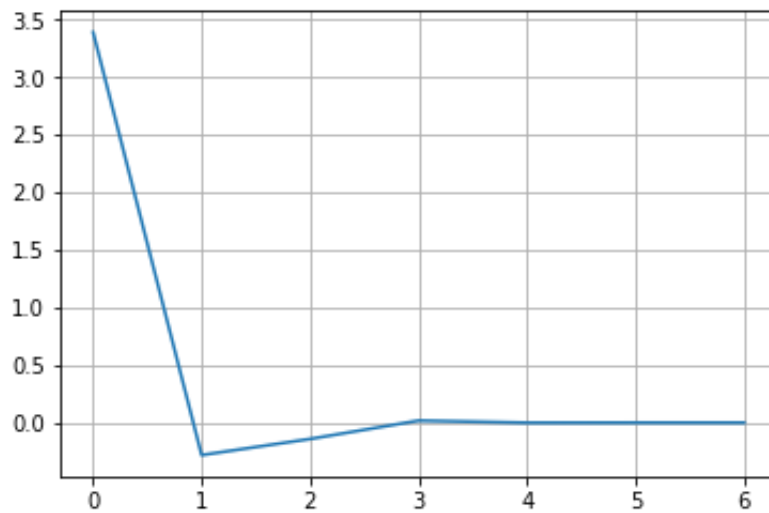
Steps taken to converge in Secant Method are 8

Out[24]:

| | n | x_(n) | f(x_n) | x_(n) - x_(n-1) | x_(n+1) |
|---|---|-----------|-------------|-----------------|-----------|
| 0 | 0 | -2 | 17 | 0 | 0 |
| 1 | 1 | -1 | 1 | 1 | -0.9375 |
| 2 | 2 | -0.9375 | 0.709976 | 0.0625 | -0.7845 |
| 3 | 3 | -0.7845 | 0.163268 | 0.153 | -0.738809 |
| 4 | 4 | -0.738809 | 0.0367487 | 0.0456915 | -0.725537 |
| 5 | 5 | -0.725537 | 0.00263908 | 0.0132715 | -0.724511 |
| 6 | 6 | -0.724511 | 4.68959e-05 | 0.00102683 | -0.724492 |
| 7 | 7 | -0.724492 | 6.12199e-08 | 1.85766e-05 | -0.724492 |

2. Find the largest root of $f(x) = e^x - x - 2 = 0$, with $\epsilon = 0.0001$.

Opposite Side



Steps taken to converge in Bisection Method are 14

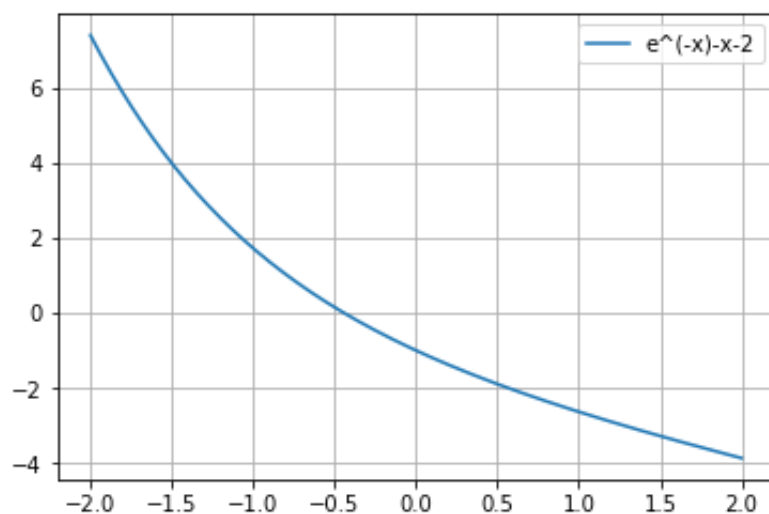
Steps taken to converge in Newton Raphson are 5

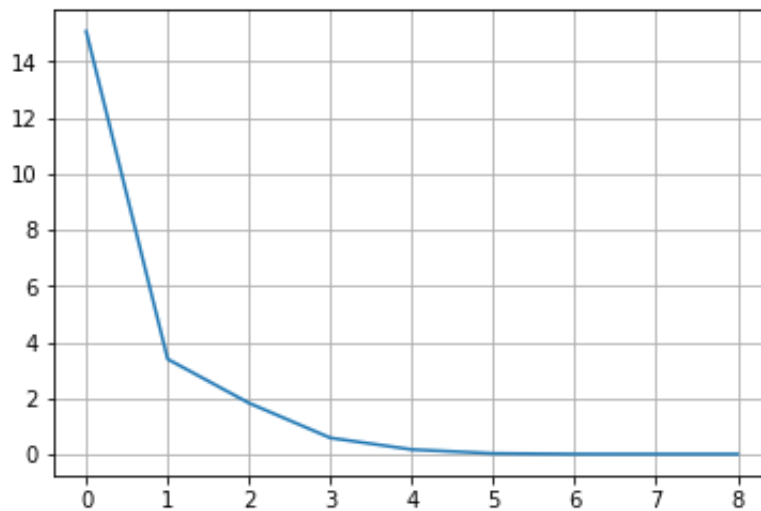
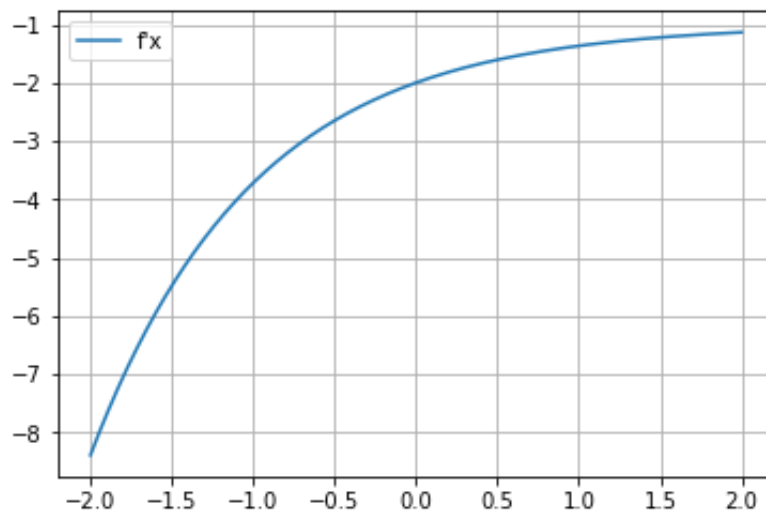
Steps taken to converge in Secant Method are 7

Out[25]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 2.000000 | 3.389056e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | -2.817182e-01 | -1.000000 | 1.076746 |
| 2 | 2.0 | 1.076746 | -1.416324e-01 | 0.076746 | 1.154340 |
| 3 | 3.0 | 1.154340 | 1.758882e-02 | 0.077594 | 1.145768 |
| 4 | 4.0 | 1.145768 | -9.118716e-04 | -0.008572 | 1.146191 |
| 5 | 5.0 | 1.146191 | -5.429890e-06 | 0.000422 | 1.146193 |
| 6 | 6.0 | 1.146193 | 1.691815e-09 | 0.000003 | 1.146193 |

Same Side





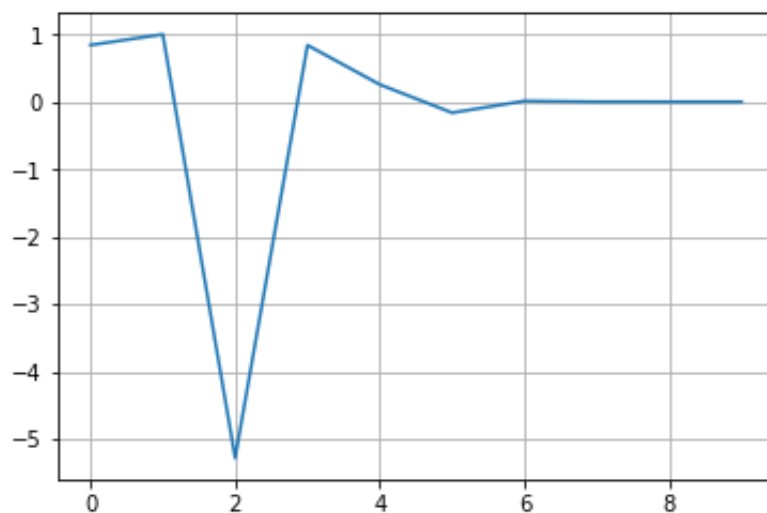
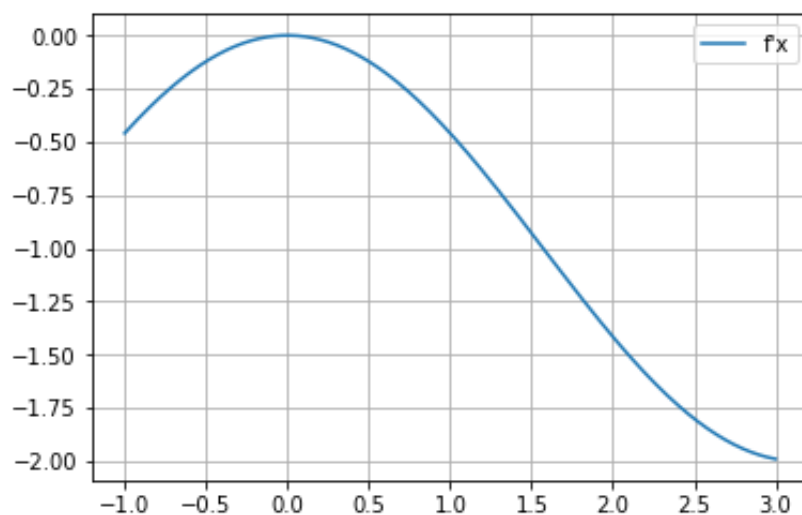
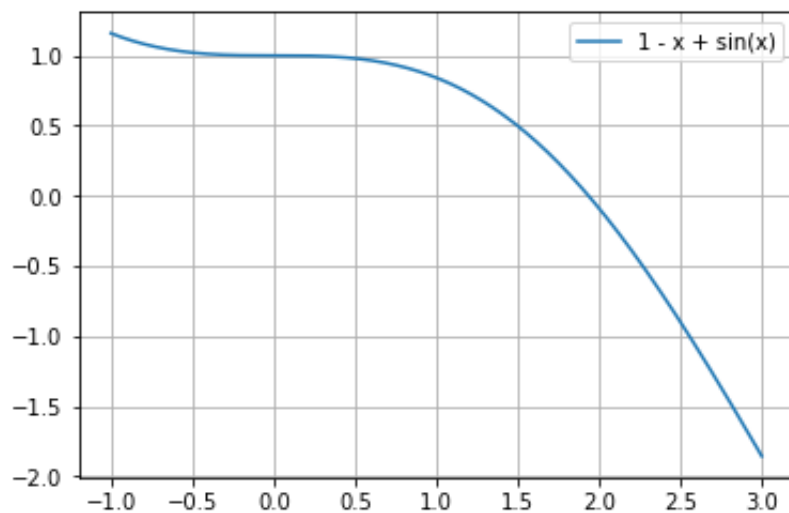
Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 5
Steps taken to converge in Secant Method are 9

Out[26]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|----------|--------------|-----------------|-----------|
| 0 | 0.0 | 3.000000 | 1.508554e+01 | 0.000000 | 0.000000 |
| 1 | 1.0 | 2.000000 | 3.389056e+00 | -1.000000 | 1.710250 |
| 2 | 2.0 | 1.710250 | 1.820094e+00 | -0.289750 | 1.374122 |
| 3 | 3.0 | 1.374122 | 5.774835e-01 | -0.336128 | 1.217912 |
| 4 | 4.0 | 1.217912 | 1.622100e-01 | -0.156210 | 1.156894 |
| 5 | 5.0 | 1.156894 | 2.314768e-02 | -0.061017 | 1.146738 |
| 6 | 6.0 | 1.146738 | 1.169207e-03 | -0.010157 | 1.146197 |
| 7 | 7.0 | 1.146197 | 9.126217e-06 | -0.000540 | 1.146193 |
| 8 | 8.0 | 1.146193 | 3.641917e-09 | -0.000004 | 1.146193 |

Find the smallest positive root of
 $f(x) = 1 - x + \sin x = 0$, with $\epsilon = 0.0001$.

Opposite Side

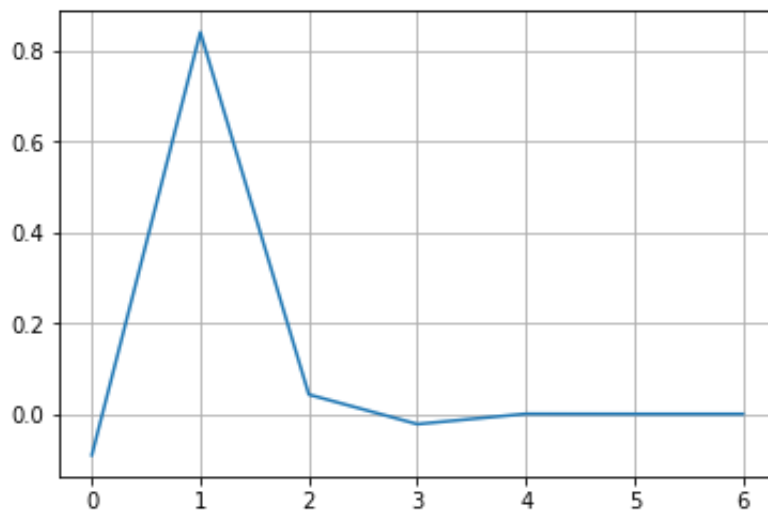


Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 6
Steps taken to converge in Secant Method are 10

Out[27]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|----------|---------------|-----------------|-----------|
| 0 | 0.0 | 1.000000 | 8.414710e-01 | 0.000000e+00 | 0.000000 |
| 1 | 1.0 | 0.000000 | 1.000000e+00 | -1.000000e+00 | 6.307994 |
| 2 | 2.0 | 6.307994 | -5.283188e+00 | 6.307994e+00 | 1.003948 |
| 3 | 3.0 | 1.003948 | 8.396496e-01 | -5.304046e+00 | 1.731313 |
| 4 | 4.0 | 1.731313 | 2.558315e-01 | 7.273653e-01 | 2.050048 |
| 5 | 5.0 | 2.050048 | -1.627075e-01 | 3.187346e-01 | 1.926139 |
| 6 | 6.0 | 1.926139 | 1.138776e-02 | -1.239084e-01 | 1.934244 |
| 7 | 7.0 | 1.934244 | 4.321935e-04 | 8.104986e-03 | 1.934564 |
| 8 | 8.0 | 1.934564 | -1.260111e-06 | 3.197389e-04 | 1.934563 |
| 9 | 9.0 | 1.934563 | 1.384806e-10 | -9.295262e-07 | 1.934563 |

Same Side



Steps taken to converge in Bisection Method are 14

Steps taken to converge in Newton Raphson are 7

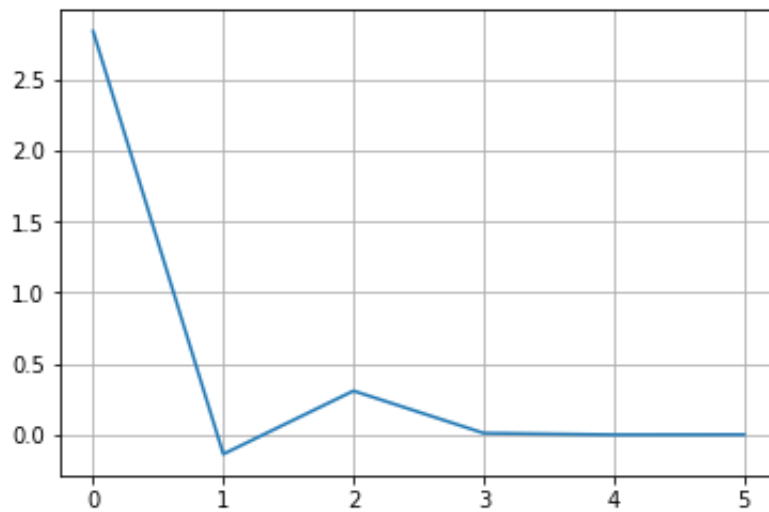
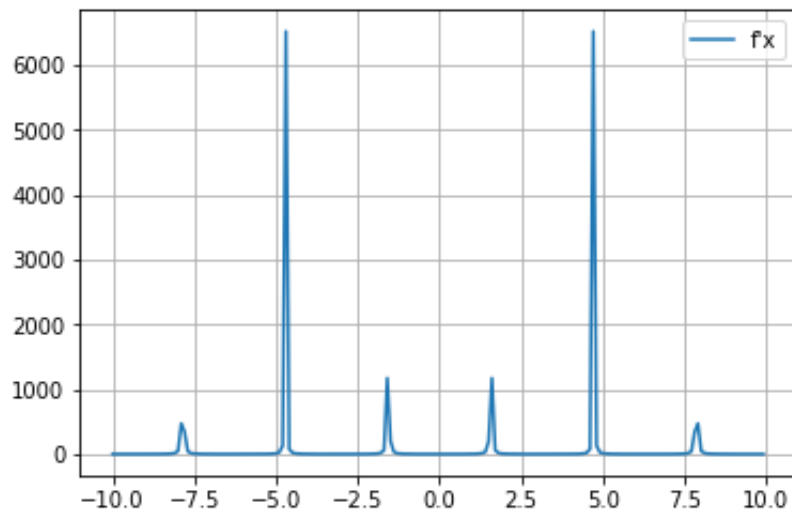
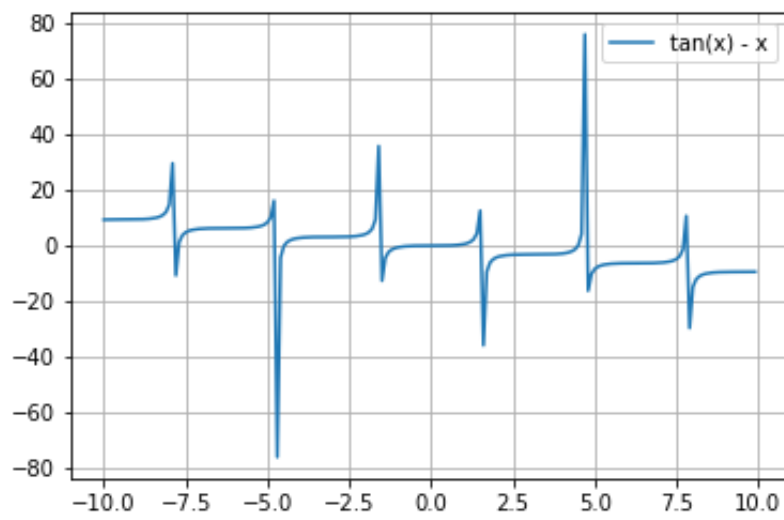
Steps taken to converge in Secant Method are 7

Out[28]:

| | n | x _(n) | f(x _n) | x _(n) - x _(n-1) | x _(n+1) |
|---|-----|------------------|--------------------|---------------------------------------|--------------------|
| 0 | 0.0 | 2.000000 | -9.070257e-02 | 0.000000 | 0.000000 |
| 1 | 1.0 | 1.000000 | 8.414710e-01 | -1.000000 | 1.902698 |
| 2 | 2.0 | 1.902698 | 4.272672e-02 | 0.902698 | 1.950985 |
| 3 | 3.0 | 1.950985 | -2.239065e-02 | 0.048287 | 1.934382 |
| 4 | 4.0 | 1.934382 | 2.462931e-04 | -0.016604 | 1.934562 |
| 5 | 5.0 | 1.934562 | 1.383453e-06 | 0.000181 | 1.934563 |
| 6 | 6.0 | 1.934563 | -8.663037e-11 | 0.000001 | 1.934563 |

4. Find the smallest non-zero positive root of $x = \tan x$, with an accuracy of 0.0001. Further solve for the root that is closest to $x = 100$.

Opposite Side

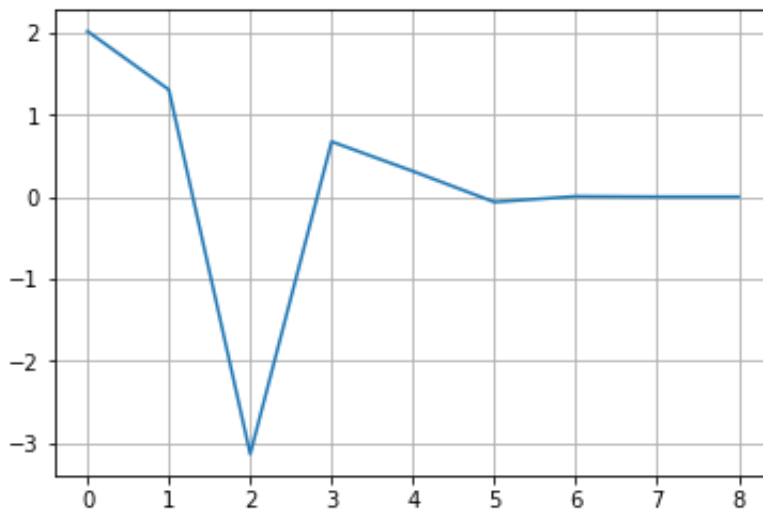


Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 4
Steps taken to converge in Secant Method are 6

Out[29]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|----------|-----------|-----------------|-----------|
| 0 | 0.0 | 4.000000 | 2.842179 | 0.000000 | 0.000000 |
| 1 | 1.0 | 4.500000 | -0.137332 | 0.500000 | 4.476954 |
| 2 | 2.0 | 4.476954 | 0.308268 | -0.023046 | 4.492897 |
| 3 | 3.0 | 4.492897 | 0.010316 | 0.015943 | 4.493449 |
| 4 | 4.0 | 4.493449 | -0.000805 | 0.000552 | 4.493409 |
| 5 | 5.0 | 4.493409 | 0.000002 | -0.000040 | 4.493409 |

Same Side

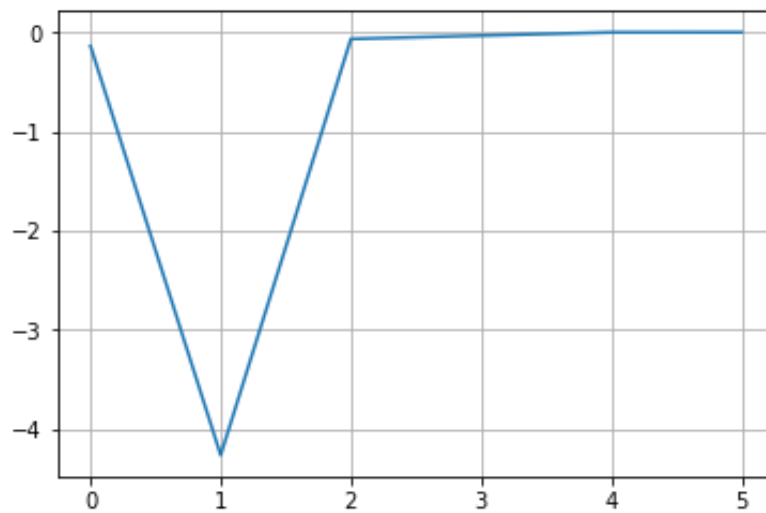


Steps taken to converge in Bisection Method are 14
Steps taken to converge in Newton Raphson are 4
Steps taken to converge in Secant Method are 9

Out[30]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|----------|---------------|-----------------|-----------|
| 0 | 0.0 | 4.300000 | 2.014152e+00 | 0.000000 | 0.000000 |
| 1 | 1.0 | 4.400000 | 1.303676e+00 | 0.100000 | 4.583493 |
| 2 | 2.0 | 4.583493 | -3.131710e+00 | 0.183493 | 4.453934 |
| 3 | 3.0 | 4.453934 | 6.713330e-01 | -0.129560 | 4.476804 |
| 4 | 4.0 | 4.476804 | 3.108701e-01 | 0.022871 | 4.496528 |
| 5 | 5.0 | 4.496528 | -6.390743e-02 | 0.019724 | 4.493165 |
| 6 | 6.0 | 4.493165 | 4.935044e-03 | -0.003363 | 4.493406 |
| 7 | 7.0 | 4.493406 | 7.263344e-05 | 0.000241 | 4.493409 |
| 8 | 8.0 | 4.493409 | -8.382428e-08 | 0.000004 | 4.493409 |

Same Side



Steps taken to converge in Bisection Method are 14

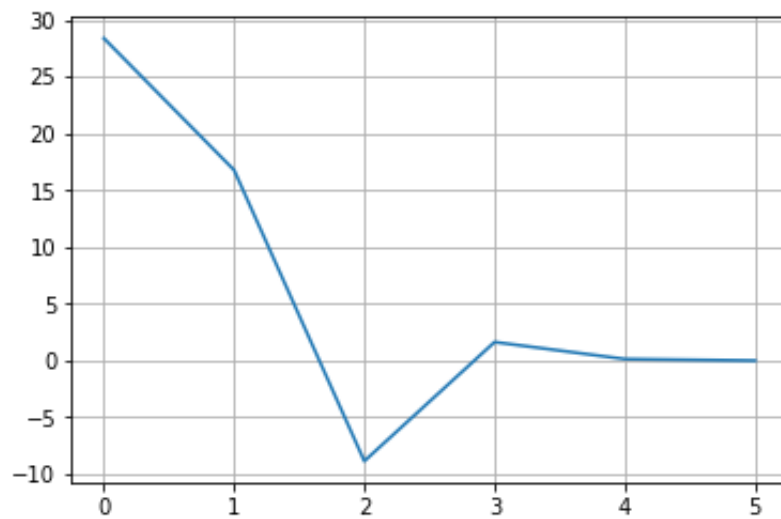
Steps taken to converge in Newton Raphson are 4

Steps taken to converge in Secant Method are 6

Out[31]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|----------|-----------|-----------------|-----------|
| 0 | 0.0 | 4.500000 | -0.137332 | 0.000000 | 0.000000 |
| 1 | 1.0 | 4.600000 | -4.260175 | 0.100000 | 4.496669 |
| 2 | 2.0 | 4.496669 | -0.066839 | -0.103331 | 4.495022 |
| 3 | 3.0 | 4.495022 | -0.032807 | -0.001647 | 4.493434 |
| 4 | 4.0 | 4.493434 | -0.000500 | -0.001588 | 4.493410 |
| 5 | 5.0 | 4.493410 | -0.000004 | -0.000025 | 4.493409 |

Same Side



Steps taken to converge in Bisection Method are 17

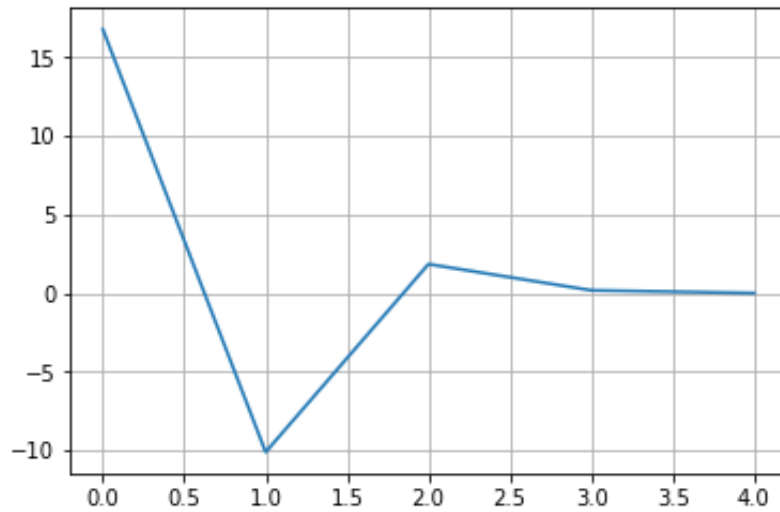
Steps taken to converge in Newton Raphson are 2

Steps taken to converge in Secant Method are 6

Out[32]:

| | n | x_n | $f(x_n)$ | $x_n - x_{n-1}$ | x_{n+1} |
|---|-----|-----------|-----------|-----------------|-----------|
| 0 | 0.0 | 98.946000 | 28.372060 | 0.000000 | 0.000000 |
| 1 | 1.0 | 98.948000 | 16.773253 | 0.002000 | 98.950892 |
| 2 | 2.0 | 98.950892 | -8.847033 | 0.002892 | 98.949894 |
| 3 | 3.0 | 98.949894 | 1.630469 | -0.000999 | 98.950049 |
| 4 | 4.0 | 98.950049 | 0.135882 | 0.000155 | 98.950063 |
| 5 | 5.0 | 98.950063 | -0.002280 | 0.000014 | 98.950063 |

Opposite Side



Steps taken to converge in Bisection Method are 17

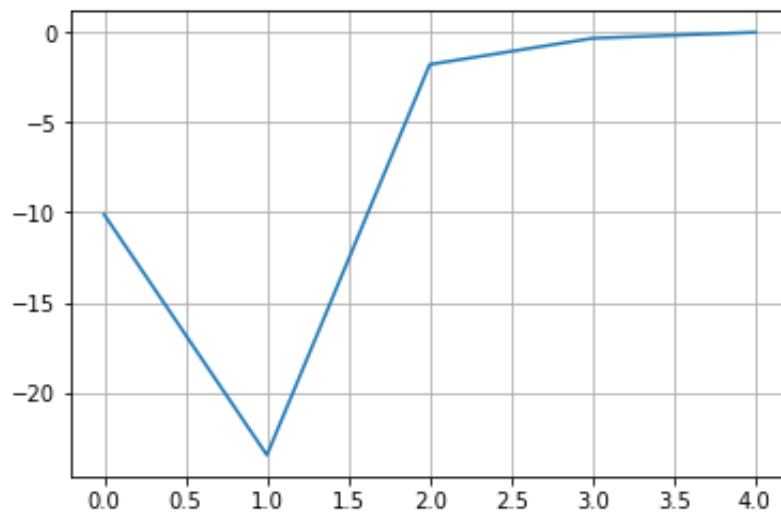
Steps taken to converge in Newton Raphson are 2

Steps taken to converge in Secant Method are 5

Out[33]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|-----|-----------|------------|-------------------|-------------|
| 0 | 0.0 | 98.948000 | 16.773253 | 0.000000 | 0.000000 |
| 1 | 1.0 | 98.951000 | -10.113991 | 0.003000 | 98.949872 |
| 2 | 2.0 | 98.949872 | 1.838371 | -0.001128 | 98.950045 |
| 3 | 3.0 | 98.950045 | 0.173419 | 0.000174 | 98.950063 |
| 4 | 4.0 | 98.950063 | -0.003289 | 0.000018 | 98.950063 |

Same Side



Steps taken to converge in Bisection Method are 17

Steps taken to converge in Newton Raphson are 2

Steps taken to converge in Secant Method are 5

Out[34]:

| | n | x_n | $f(x_n)$ | $x_n - x_{(n-1)}$ | $x_{(n+1)}$ |
|---|-----|-----------|------------|-------------------|-------------|
| 0 | 0.0 | 98.951000 | -10.113991 | 0.000000 | 0.000000 |
| 1 | 1.0 | 98.952000 | -23.465454 | 0.001000 | 98.950242 |
| 2 | 2.0 | 98.950242 | -1.790876 | -0.001758 | 98.950097 |
| 3 | 3.0 | 98.950097 | -0.338361 | -0.000145 | 98.950063 |
| 4 | 4.0 | 98.950063 | -0.005996 | -0.000034 | 98.950063 |