Easy

| easy.t> 7 8 4 6 1 9 2 3 5 | | 1 5 6 3 2 7 4 8 9 | | |
|--------------------------------------------------------------|-------|-------------------------|--|--|
| 5 7 8 | 2 6 1 | 9 3 4 | | |
| 3 4 1 | 8 9 7 | 5 6 2 | | |
| 9 2 6 | 5 4 3 | 8 7 1 | | |
| 4 5 3 | 7 2 9 | 6 1 8 | | |
| 8 6 2 | 3 1 4 | 7 9 5 | | |
| 1 9 7 | 6 5 8 | 2 4 3 | | |
| Number of backtrack calls: 1 Number of backtrack failures: 0 | | | | |

Figure 1: Solution for the easy sudoku board. The backtrack function was called only once, and there were no instances in which the backtrack function returned a failure.

Medium

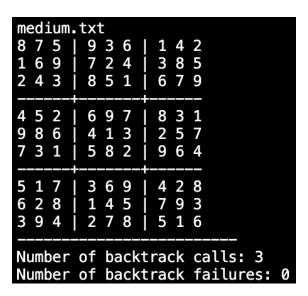


Figure 2: Solution for the medium sudoku board. The backtrack function was called a total of 3 times, and there were still no instances in which the backtrack function returned a failure.

Hard

| hard.tx 1 5 2 4 3 7 6 8 9 | 3 4 6 | 8 9 7 6 5 2 3 1 4 | | |
|------------------------------------------------------------------|-------------------------|-----------------------------|--|--|
| 8 2 1 5 4 3 9 7 6 | 6 3 7 8 9 1 4 2 5 | 9 4 5 7 2 6 1 8 3 | | |
| 7 9 8 3 6 5 2 1 4 | 9 1 4 | 4 6 1 2 7 8 5 3 9 | | |
| Number of backtrack calls: 12 Number of backtrack failures: 4 | | | | |

Figure 3: Solution for the hard sudoku board. The backtrack function was called a total of 12 times, and there were 4 instances in which the function returned a failure.

Very hard

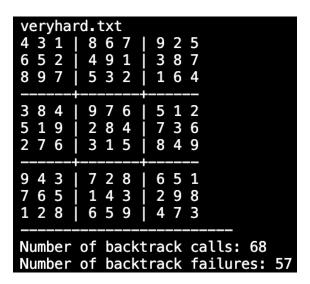


Figure 4: Solution for the very hard sudoku board. In this solution, the backtrack function was called a total of 68 times, and a total of 57 failures were returned.

We see in the results that the backtrack function was called around 1 - 12 times in total for the first three boards, and the first four times failures were returned was in the hard puzzle. The very hard puzzle however, had a total of 68 calls to the backtrack function, and 57 of those calls returned a failure. This makes sense since the easier puzzles have more filled cells, and thus less empty cells to fill, which reduces the search space for the backtracking algorithm, and it therefore needs fewer calls to the backtrack function and will also not encounter failures as often. On the other hand, the very hard puzzle has a lot fewer filled cells, which means the algorithm must explore a higher number of possibilities, in addition to these attempts also leading to more invalid states, when it returns a failure.