

Signal processing by the HOG MAP kinase pathway

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Signaling pathways relay information about changes in the external environment so that cells can respond appropriately. How much information a pathway can carry depends on its bandwidth. We designed a microfluidic device to reliably change the environment of single cells over a range of frequencies. Using this device, we measured the bandwidth of the *Saccharomyces cerevisiae* signaling pathway that responds to high osmolarity. This prototypical pathway, the HOG pathway, is shown to act as a low-pass filter, integrating the signal when it changes rapidly and following it faithfully when it changes more slowly. We study the dependence of the pathway's bandwidth on its architecture. We measure previously unknown bounds on all of the *in vivo* reaction rates acting in this pathway. We find that the two-component Ssk1 branch of this pathway is capable of fast signal integration, whereas the kinase Ste11 branch is not. Our experimental techniques can be applied to other signaling pathways, allowing the measurement of their *in vivo* kinetics and the quantification of their information capacity.

bandwidth | HOG pathway | microfluidics | signal transduction

For a signaling pathway to carry accurate information about its environment, the output of the pathway must closely follow the input. Pathways measuring stimuli that change more rapidly with time need to carry more information. The information capacity of a pathway, i.e., how much information can be transmitted through the pathway per unit time, is proportional to the bandwidth of the pathway (1). The larger the bandwidth of a signaling pathway, the shorter its response time and the more accurately it can follow a rapidly varying signal. Bandwidth measurements are routinely used to characterize communications systems. In this article, we present an experimental technique combined with a microfluidic device that allows measurement of signaling-pathway bandwidth. We use this technique to measure the *in vivo* bandwidth of the hyperosmolar signaling pathway (HOG) in the yeast *Saccharomyces cerevisiae* (Fig. 1A).

Signaling pathways consist of cascades of proteins where each protein activates the next (2). A signaling cascade is triggered when a receptor is activated by an external stimulus. Often, the signals are transmitted through kinase-dependent phosphorylation (Fig. 1A). Information about the environment is then transmitted through the pathway, resulting in a response from the cell. The bandwidth of the pathway can be determined by measuring the response of the pathway to the input signal fluctuating at different frequencies. At frequencies up to the bandwidth, the pathway responds faithfully to the input stimulus. To understand how a signaling pathway responds to excitation over a range of frequencies, we numerically studied (3) the three-level branched signaling cascade shown in Fig. 1B and described in Box 1. When the input stimulus to this pathway oscillates at frequencies lower than the bandwidth ω_b , the output of the cascade measured by the levels of the activated enzyme X_3^* follows the input faithfully. When the input oscillates at frequencies higher than the bandwidth ω_b , the pathway integrates and, hence, averages over the input (Fig. 1C). Thus, the concentration of X_3^* shows a response to the mean level of the input and no response to the input oscillations. The pathway acts as a low-pass filter with a bandwidth ω_b (Fig. 1D). This model pathway can faithfully convey information about fluctuations in its stimulus that happen on time

scales slower than $\tau_b \sim 1/\omega_b$. For a linear pathway, the bandwidth ω_b is dominated by the slowest time scale in the cascade. Thus, all activation and deactivation rate constants in this cascade must be at least as large as ω_b for the cascade to respond faithfully to the inputs oscillating at frequencies lower than ω_b . For a branched pathway, the activation rate constant of the slower branch does not affect the bandwidth. However, the deactivation rate constants of both branches have to be at least as fast as the bandwidth.

To measure signaling pathway response *in vivo* over different input frequencies and, hence, the bandwidth, as it is usually done in engineering, we developed a microfluidic device that allows for rapid periodic changes in media (Fig. 2). Rapid changes in media are exceptionally difficult to achieve in conventional microfluidic devices. Our device has two fluids entering through different inlets of a Y-shaped flow chamber, as shown in Fig. 2A. The region of lateral diffusion and, hence, mixing scales as $\sqrt{Dx/u}$, with D representing the diffusion constant of the media, u the speed of the laminar flow, and x the distance from the point of union of the two fluids, measured along the direction of the flow. Near the point where the two fluids meet, mixing is minimal. By changing pressure difference between the fluids by using a computer-controlled switch, we can sweep the separation line across the width of the flow cell. This allows us to rapidly switch the conditions to which the cells in the flow chamber are exposed. The media can be changed as frequently as twice a second, i.e., at 2 Hz (Fig. 2) without perturbing cell adhesion. Appropriate alignment is achieved by observing the separation line in real time by using phase contrast microscopy [see supporting information (SI) Text and Movie S1 and Movie S2].

We used this device to measure the bandwidth of the hyperosmolar glycerol (HOG) pathway in *S. cerevisiae* single cells (Fig. 1A). This MAP kinase pathway (4) is used by *S. cerevisiae* and other fungi (5, 6) to sense osmolar pressure in the environment and maintain water homeostasis. Although the HOG pathway is well documented, its transduction kinetics and *in vivo* reaction rates have been only roughly estimated, and its filtering properties are unknown. The SLN1 (7, 8) and SHO1 (9, 10) branches, shown in Fig. 1A, are redundant for cell survival under conditions of moderate osmotic stress. However, the SLN1 branch seems more important for pathway response to low and very high osmotic stress (11–13). Additionally, it is known that in an *ssk2Δ ssk22Δ* strain, the maximal phosphorylation of Hog1 is delayed from 1 min to ≈ 3 –5 min (11, 14). Once phosphorylated, Hog1 localizes to the nucleus (15–17), where it is recruited to target promoters and activates several transcription factors.

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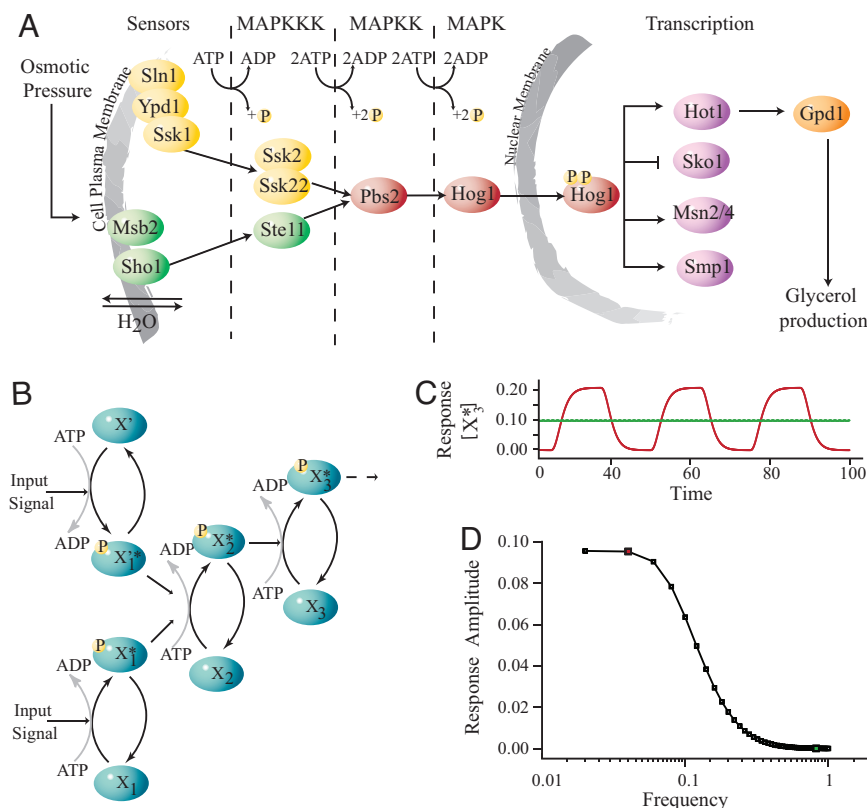
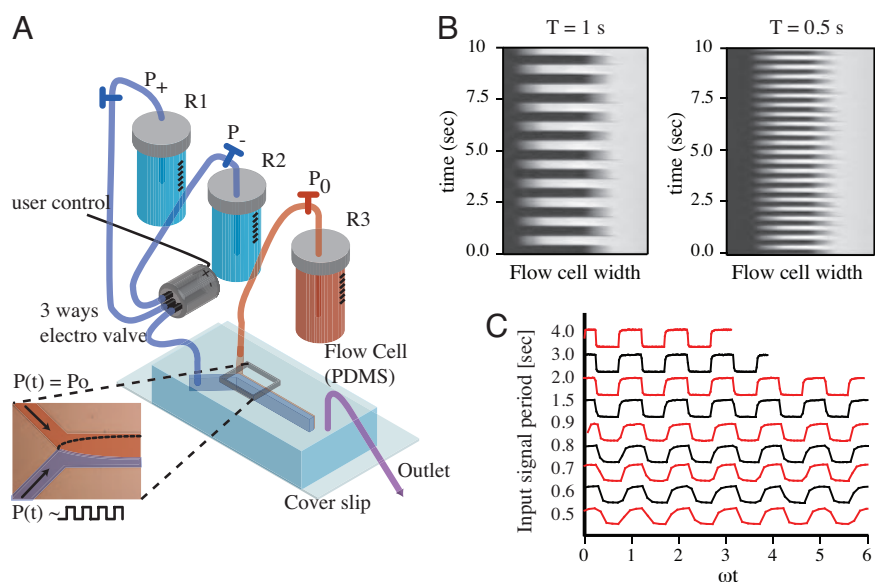


Fig. 1. Analysis of a model pathway and the hyperosmolar response pathway in *S. cerevisiae*. (A) The hyperosmolar glycerol response HOG pathway consists of two input branches. The SLN1 phosphorelay represses the kinase Ssk1 under osmotically neutral conditions. Hyperosmotic stress results in deactivation of Sln1. The subsequent derepression of Ssk1 allows Ssk1 to activate the MAPKKKs Ssk2 and Ssk22, which in turn phosphorylate Pbs2. The SHO1 branch activates Pbs2 through the MAPKK Ste11. Activation of Hog1 by Pbs2 leads to its nuclear localization and a hyperosmolar transcriptional response. (B) A model three-level branched signaling cascade with both X_1^+ and $X_1'^+$ activating X_2 , which in turn activates X_3 . Each level of the cascade activates the next through phosphorylation consuming one molecule of ATP. (C) The steady-state level of X_3^s is plotted as a function of time. For an input oscillating slowly, the level of X_3^s (in red) oscillates between zero and a maximum value, following the input in time. For an input oscillating rapidly, the level of X_3^s (in green) oscillates with a very small amplitude and shows a response primarily to the time-averaged value of the input. (D) The amplitude of the oscillating response of X_3^s is plotted as a function of the frequency of the input signal oscillation. The points corresponding to the input frequencies in B are shown as a red square and a green square, respectively. This amplitude of the oscillatory response drops off sharply at a characteristic frequency ω_b of the input, which is the bandwidth of this model pathway. How fast information propagates through such a cascade is proportional to this pathway bandwidth ω_b .

To determine the bandwidth of the HOG pathway, we followed the nuclear localization of Hog1 as a reporter of the output of the signaling activity of the cascade (Movie S3). We exposed yeast cells in the flow chamber to an osmolar shock oscillating between 0 and 1 M sorbitol over a range of frequencies. These measurements allowed us to extract dynamical signaling properties of the HOG pathway. We measured frequency-dependent colocalization of Hog1-GFP with the nuclear protein Htb2-mCherry (Fig. 3). As-

suming a first-order linear filter, we could obtain the bandwidth of the Hog1-GFP localization response to be $4.6 \times 10^{-3} \pm 1.1 \times 10^{-3}$ Hz (see Methods and Fig. S1). Thus cytoplasmic activity in the signal-transduction cascade results in the phosphorylation of Hog1 and its subsequent nuclear translocation upon the beginning of the input pulse and nuclear delocalization at the end of the input pulse, all in ≈ 220 seconds. At frequencies slower than 4.6×10^{-3} Hz, the nuclear level of Hog1-GFP faithfully follows the input (Fig. 3B). At

Fig. 2. Microfluidic device for studying frequency response of single cells. (A) One of the input arms of a Y-shaped flow chamber is fed by a solution of 1 M sorbitol in SC medium (in red) from reservoir R3 at a hydrostatic pressure head at P_0 . The other arm is fed by SC (in blue) from one of two reservoirs, R1 at a hydrostatic pressure head at P_+ and R2 at P_- . The choice between the two reservoirs, R1 or R2, is made by a programmable three-way electrovalve. When reservoir R2 is chosen, the fluid from reservoir R3 fills most of the chamber, whereas when R1 is chosen, the fluid from R1 fills the chamber. Periodic changes in the state of the electrovalve allow a change in the environment of the cells at a tunable period T . (B) To characterize the device, water was filled in reservoirs R1 and R2, and a dilute solution of fluorescein was filled in R3. The state of a cross-section of the flow chamber was imaged by fluorescent microscopy. This state is shown as a function of flow-cell width (along the x axis) and time (along the y axis) for both $T = 1$ -s oscillations (Left) and $T = 0.5$ -s oscillations (Right). The bright regions indicate fluorescein solution, and the dark regions indicate water. The sharp interfaces between the dark and bright regions show the efficiency of our device in changing conditions rapidly. (C) The fluorescence intensity for a typical point in the middle of the channel is shown for oscillation periods ranging from $T = 0.5$ s to $T = 4$ s. The curves have been offset along the y axis for clarity, and for each curve, time has been scaled by its input frequency ω . All the curves oscillate between the same minimum and maximum fluorescence intensities. The transition from one medium to the other gets less sharp as $T = 0.5$ s is approached, indicating the limit of resolution for our experimental device.



levels, transcription begins during each osmotic input cycle (Fig. 3D), showing a faithful response to the input signal. At high frequencies, the transcriptional response is activated just once with subsequent adaptation. The transcriptional response at high frequencies mimics the response of the cell to a step shock of lower magnitude. Thus, we again see that at high frequencies, the cell effectively integrates the signal. Although transcription and translation are not fast reporters of HOG pathway activity, these results do allow us to confirm the Hog1 localization results at both very high and very low frequencies.

Pathway bandwidth could be set by the time scale of water export and/or the resulting size change after osmotic pulse. We measured the size response of the cells by again exposing yeast cells in the flow chamber to an osmolar shock oscillating between 0 and 1 M sorbitol over a range of frequencies. We monitored accurately the change in cell size on osmolar shock by measuring the change in the cell's mean fluorescent intensity in a strain with cytoplasmic fluorescent protein Ura1-GFP (Fig. S2). We also studied changes in cell size in Hog1-GFP strains in which *PBS2* was deleted, rendering the HOG pathway inactive. By comparing cell-size response for 1 and 2 M sorbitol input over a range of frequencies, we found that the mechanical response of the cell is linear and acts as a low-pass filter (Fig. 3E) with a bandwidth of 0.033 ± 0.01 Hz. At higher frequencies, the size oscillations drop dramatically. At lower frequencies, the size oscillations follow the input (Fig. 3F). This, in turn, sets the typical time scale for water transport in and out of the cell at 30 ± 1 s, and the porosity of the cell wall to be of the order of 1.75×10^{-13} m \cdot Pa $^{-1}$ sec $^{-1}$ (SI Text). The mechanical response of the cell occurs on time scales much faster than that of Hog1 localization and therefore cannot set the time scale of pathway activation.

Because the HOG pathway bandwidth is not constrained by the cell's mechanical responses, the 4.6×10^{-3} -Hz bandwidth of the HOG signaling pathway must depend on the biochemical reaction rates during signaling. Following our model, the pathway time scale could be set at or below the level of Pbs2 where the two branches converge or by the faster of the two branches. To test the role of the Pbs2 protein, we studied signaling dynamics under conditions of extreme Pbs2 under- and overexpression. Under conditions where Pbs2 is underexpressed from the glucose-repressed *GAL1* promoter, the response of the HOG pathway is drastically slowed (Fig. S3). When highly overexpressed by induction of the *GAL1* promoter, Pbs2 does not significantly change the time scale of signaling through the HOG pathway (Fig. S3). This indicates that Pbs2 is not in limiting concentrations under wild-type conditions. We also measured the bandwidth in wild-type diploid cells and in *pbs2Δ/PBS2* diploid cells. We found that the deletion of a single copy of *PBS2* did not change the bandwidth of the diploid cell from that of the wild type (Figs. S4 and S5).

To understand whether either of the input branches set the bandwidth of the pathway, we studied the dynamics of Hog1-GFP in both *ste11Δ* and *sho1Δ* strains where activation of Pbs2 through the SHO1 branch is destroyed. The Hog1 localization response in these strains behaved identically to the wild-type strain (Fig. 4A). In striking contrast, blocking signaling from the SLN1 branch by deleting the *SSK1* gene caused the Hog1 localization response to slow by almost 2-fold, to a bandwidth of $2.6 \times 10^{-3} \pm 0.4 \times 10^{-3}$ Hz (Fig. 4B).

Additionally, we find that the SHO1 branch does not quickly integrate the high-frequency input signals, whereas the SLN1 branch does (Fig. 4C). The deactivation rate constants of the pathway in mutants without either the *SSK1* or the SHO1 branch are the same (Fig. S6). That the SLN1 branch is faster is consistent with previous results (9). In wild-type cells, it is the SLN1 branch that integrates high-frequency signals leading to the wild-type response.

The SLN1 branch consists of a two-component system, common in prokaryotes, in which there is no enzymatic amplification of the signal. The SHO1 branch is an enzymatic kinase cascade of the type

that constitutes most signaling pathways in eukaryotes. We find that signal transduction through the branch with the phospho-relay is more than twice as fast as the SHO1 branch employing an enzymatic cascade. Interestingly in some other yeasts and fungi, the Sho1 protein is not conserved or the SHO1 branch does not signal to the HOG pathway (6, 19–21). Furthermore, it is the faster SLN1 branch that is conserved in fungi.

The bandwidth of the HOG pathway could be set by the time for Hog1 to be activated and localize to the nucleus or the time for Hog1 to be deactivated and delocalize from the nucleus. The activation time includes the time to activate the SLN1 branch of the pathway, the time for this branch to activate Pbs2, or the time for Pbs2 to activate Hog1. The pathway deactivation time includes the time to deactivate one of the SLN1 or the SHO1 branch, the time to deactivate Pbs2, or the time to deactivate Hog1 and delocalize it from the nucleus. Consistent with the experimental evidence that the pathway is able to integrate the signal at high frequencies, the rate at which the HOG pathway turns off could be limiting for bandwidth. Accurately measuring the deactivation rate constant from nuclear Hog1 traces (such as Fig. S6) is difficult because the initial drop in intensity is due to the cell size suddenly increasing in response to a decreasing osmotic level in the environment. This is followed by nuclear Hog1 export and the nuclear signal decaying into measurement noise, leaving very few data points to fit to an exponential. To carefully measure the deactivation rate constant of the HOG pathway, we used asymmetric pulses of osmolar shock (Fig. 4C). When the off time of the pulse (t_{off}) is very short, the cell cannot tell independent pulses apart, responding as if to a step increase in sorbitol. When the pulses are very far apart (t_{off} is very large), the pathway responds to each pulse, and Hog1 oscillates in and out of the nucleus each time. The amplitude of this oscillation decreases with t_{off} , vanishing as t_{off} approaches zero. This amplitude scales as $1 - e^{-k_{\text{off}} t_{\text{off}}}$, where k_{off} is the slowest deactivation rate constant in the pathway. The fit of the amplitude to this single exponential allowed us to extract the rate constant for the slowest deactivation rate to be $4.1 \times 10^{-3} \pm 0.5 \times 10^{-3}$ Hz (Fig. 4E), which is equal to the measured bandwidth of the HOG pathway (Fig. 3) to within error bars. This, coupled with the fact that the deactivation rates in mutants with either a deactivated SHO1 branch or the SLN1 branch are identical to within error bars (Fig. S6), supports the argument that the deactivation rates of components at or downstream of Pbs2 must be limiting for pathway bandwidth. It is possible that the bandwidth of the HOG pathway is set by phosphatases responsible for deactivating Pbs2 and Hog1 (22). The study of phosphatases in controlling the signaling dynamics of the pathway is left to future work.

Our results indicate that the time scales of Hog1 localization in all strains are set by biochemical reaction rates. Time scales are not set by cell-wall mechanical response and water transport because these processes happen on a much faster time scale. The results from our experiments on wild-type and mutant strains indicate that the activation and deactivation rates of Pbs2, Hog1, and all of the components upstream of Pbs2 in the SLN1 branch must be $\geq 4.6 \times 10^{-3}$ Hz. We also show that the deactivation rates of all components in the SHO1 branch must be $\geq 4.6 \times 10^{-3}$ Hz, whereas the activation rates are significantly slower. As we saw in our model, the bandwidth of a pathway is set by the slowest time scale; thus, if any protein activation or deactivation rate were $< 4.6 \times 10^{-3}$ Hz, the bandwidth of the HOG pathway in wild-type and *sho1Δ* strains would have to be $< 4.6 \times 10^{-3}$ Hz. Similarly, the difference between the *ssk1Δ* and *sho1Δ* strains indicates that the activation rates of all proteins upstream of Pbs2 in the Sho1 branch must be $\geq 2.6 \times 10^{-3}$ Hz. Our systems-level measurements of the HOG pathway put bounds on all of the rate constants in the signaling pathway *in vivo*.

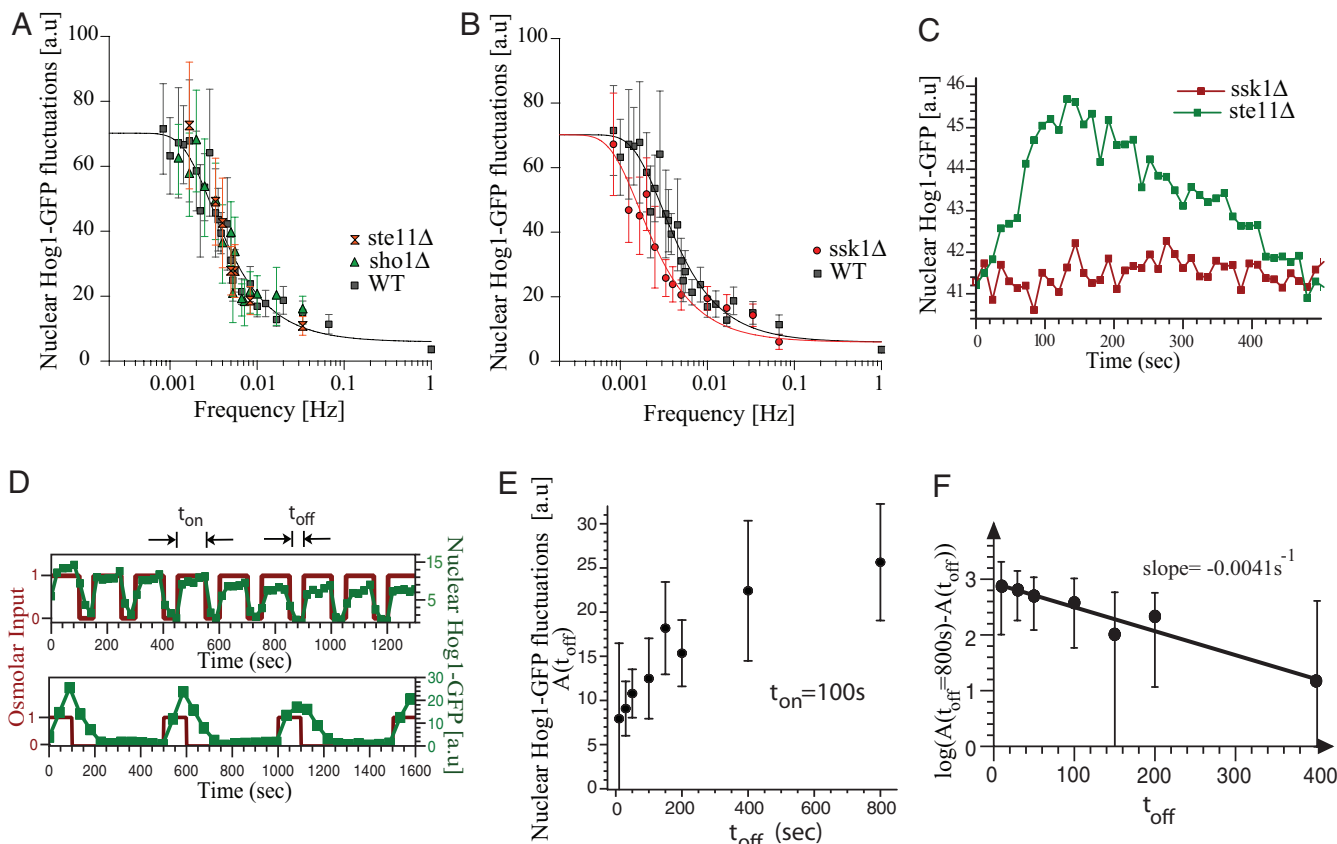


Fig. 4. The SHO1 and SLN1 branches have different bandwidths. (A) Deletion of *STE11* (red Σ) or *SHO1* (\blacktriangle) blocks input to Hog1 from the SHO1 branch. Strains with this branch blocked show no change in bandwidth compared with the wild-type strain. Time scales are in good agreement for wild type ($\omega_b = 4.6 \times 10^{-3} \pm 1.10 \times 10^{-3}$ Hz), *sho1* Δ mutants ($\omega_b = 4.6 \times 10^{-3} \pm 0.9 \times 10^{-3}$ Hz), and *ste11* Δ mutants ($\omega_b = 4.6 \times 10^{-3} \pm 1 \times 10^{-3}$ Hz), indicating that the SSK1 branch dominates the activation dynamics of the HOG pathway. (B) Deletion of SSK1 (\bullet) blocks input to Hog1 from the SLN1 branch. The *ssk1* Δ strains ($\omega_b = 2.6 \times 10^{-3} \pm 0.4 \times 10^{-3}$ Hz) show close to 2-fold decrease in bandwidth compared with the wild-type strain (\blacksquare , $\omega_b = 4.6 \times 10^{-3} \pm 1.1 \times 10^{-3}$ Hz). Each point represents the amplitude of Hog1-GFP and Htb2-mCherry colocalization over, typically, 10 cells. The error bars represent one standard deviation from the mean. (C) The time course of nuclear Hog1-GFP levels for the input oscillating 0.2 Hz (larger than the pathway bandwidth) is shown for cells of *ste11* Δ (in green) and *ssk1* Δ (in red) strain backgrounds. At such high frequencies, the cells possessing only the Ssk1 branch (*ste11* Δ) integrate the input just as the wild type (see Fig. 3C), whereas the cells possessing just the Sho1 branch (*ssk1* Δ) do not respond at all. Thus it is the Ssk1 branch of the pathway that allows the cells to integrate fluctuating inputs from the environment. (D) Time course of nuclear Hog1::GFP intensity as a function of time shown for different temporally changing inputs. In both *Upper* and *Lower* graphs, the input amplitude (shown in red) oscillates between 0 and 1 M sorbitol starting at time $t = 0$ s. In *Upper*, the input stays at 1 M for $t_{on} = 100$ s and at 0 M for $t_{off} = 50$ s. In *Lower*, $t_{on} = 100$ s, whereas $t_{off} = 400$ s. The nuclear Hog1::GFP intensity oscillates according to the input. The amplitude of the oscillation for $t_{off} = 400$ is larger than for $t_{off} = 50$ s. (E) The amplitude of the oscillations in Hog1 nuclear intensity is plotted as a function of t_{off} for a fixed $t_{on} = 100$ s. With increasing t_{off} , the amplitude of Hog1::GFP oscillations in steady-state increase, reaching a maximum at and above $t_{off} = 800$ s. (F) The log of the difference in the amplitude of the oscillation at a given t_{off} (shown in D) from that at $t_{off} = 800$ s is plotted as a function of t_{off} . This plot gives an accurate measure of the rate constant for the turn off of the osmolar pathway when the osmolar input is turned off, and from the slope of this plot, we find it to be 0.0041 ± 0.0005 Hz, which corresponds to within error bars to the bandwidth of the Hog pathway shown in Fig. 3. This shows that the rate-limiting step is the turn off of the Hog pathway.

Our microfluidic device allows for measurement of pathway bandwidth and elucidation of how bandwidth is set. Bandwidth measurement places bounds on all of the rate constants in the pathway. Similar experiments can help compare the design and dynamics of different signaling pathways within the same cell as well as the same pathway in different evolutionarily related species.

Methods

Box1: Model. The proteins X_1 and X'_1 are directly activated by the input I (Fig. 1) to their excited form X_1^* and X'^*_1 at rates given by

$$\frac{dX_1^*}{dt} = \frac{k_a^0 I}{1 + K_{M0}^{-1} X_1} X_1 - \frac{X_1^*}{T_1} \quad [1]$$

$$\frac{dX_1^*}{dt} = \frac{k_a'^0 I}{1 + K_{M_0}^{-1} X_1'} X_1' - \frac{X_1^*}{T_1'} \quad [2]$$

These proteins in turn excite X_2 to X_2^* at a rate

$$\frac{dX_2^*}{dt} = \left(\frac{k_a^1 X_1^*}{1 + K_{M1}^{-1} X_2} + \frac{k_a'^1 X_1'^*}{1 + K_{M1}'^{-1} X_2} \right) X_2 - \frac{X_2^*}{T_2}, \quad [3]$$

which in turn excites X_3 to X_3^* at a rate

$$\frac{dX_3^*}{dt} = \frac{k_a^2 X_2^*}{1 + K_M^{-1} X_3} X_3 - \frac{X_3^*}{T_3}. \quad [4]$$

k_{fs}^i are the rate constant, K_{Mf}^i are the Michaelis–Menten constants for the reactions activated by X_f^i , and T_i is the lifetime of activated protein X_f^i . For an input that fluctuates in time about a constant value \bar{I} by a small $\delta(I)$, we can linearize the above equations in fluctuations in the concentrations of excited forms of the proteins about the steady-state. The Fourier transform of the fluctuations, $\delta X_s^i(\omega)$ is found to be proportional to:

$$\delta X_3^*(\omega) \sim \left(\frac{1}{1 + i\omega\tau_1} + \frac{1}{1 + i\omega\tau_1'} \right) \frac{1}{1 + i\omega\tau_2} \frac{1}{1 + i\omega\tau_3} - \delta I(\omega), \quad [5]$$

where $\delta(\omega)$ is the Fourier transform of the input and τ_1 , τ'_1 , τ_2 , and τ_3 are the sum of the time scales of excitation and deexcitation of X_1 , X'_1 , X_2 , and X_3 , respectively. At high frequencies [$\omega > \max(1/\tau_1, 1/\tau'_1, 1/\tau_3)$], the amplitude of the fluctuations in the excited proteins fall rapidly, and the linearization is valid. The bandwidth of the pathway $\omega_c \sim \max[\min(1/\tau_1, 1/\tau_2, 1/\tau_3), \min(1/\tau'_1, 1/\tau_2, 1/\tau_3)]$ and, similarly, the slowest time scale in the pathway $\tau_c \sim \min[\max(\tau_1, \tau_2, \tau_3), \max(\tau'_1, \tau_2, \tau_3)]$. For excitations above this critical frequency ω_c , the pathway integrates the signal, whereas below it, the pathway follows the signal faithfully. It is important to note that all of the activation and deactivation times of all of the proteins in the pathway have to be faster than or equal to this slowest time scale.

Yeast Strains and Plasmids. Yeast strains and plasmids were constructed by using standard molecular biology techniques. Table S1 contains the list of strains and plasmids used in this study.

Yeast Growth Conditions. Cells were grown overnight at 30°C in synthetic complete (SC) medium, reinoculated into fresh SC medium and grown at 30°C for 4–6 h before microscopy.

Microfluidic Chamber and Attachment of Yeast Cells. Microfluidic chambers were made in PDMS (polydimethylsiloxane) by using classic soft lithography techniques and then adhered to a coverslip (24 × 60 × 1 mm) by using a plasma oven. Our device used a three-way electrovalve (The Lee Company) controlled by a computer. A saturated solution of Con A (25 mg/ml; Sigma-Aldrich) was added into the chamber, and after washing the chamber with fresh SC, yeast cells were injected and allowed 5–10 min to settle down and stick to the coverslip. Once started, the flow removed the unattached cells. The visual basic code for controlling the switch and flow cell design will be made freely available upon publication.

Microscopy and Image Processing. The cells were observed by using a Zeiss 200M fluorescent microscope with an Orca-II-ER camera and a 100×/1.45 N.A. plan α fluar objective. Emission from GFP was visualized at 528 nm (38-nm bandwidth) upon excitation at 490 nm (20-nm bandwidth), and emission of mCherry was visualized at 617 nm (73-nm bandwidth) upon excitation at 555 nm (28-nm bandwidth). Cells were allowed to adapt to the oscillating conditions for up to 20 min before starting acquisition. Subsequently cells were photographed at regular intervals and faster than twice the frequency of the oscillations of the flowing

media. Image analysis was done by using ImageJ (<http://rsb.info.nih.gov/ij/>). Localization of Hog1-GFP was obtained by measuring the GFP intensity colocalized with Htb2-mCherry. Cell size was measured as the variations of cytoplasmic fluorescently labeled proteins (HOG1 in the main text and URA1 in *S1 Text*). When the cell volume changes, the concentration changes, and hence the fluorescent intensity per unit projected area of the cell changes. This method was more accurate at measuring cell-size fluctuations than the one by estimating the size of cells from the DIC image. Hog1 nuclear localization was measured in individual cells. The data points in all plots denote the means over cells, and the error bars denote standard deviation in the response of these cells.

Bandwidth Measurements. Amplitude measurements as in Figs. 3 and 4 were fit to the classic low-pass filter form

$$\chi = \sqrt{\frac{G}{1 + (\omega\tau)^2}} + \delta, \quad [6]$$

with ω representing the frequency and τ the time scale of the filter. We also fit the measured amplitudes with the response of a model pathway with the slowest activation, k_{on} and the slowest deactivation rate k_{off} , to the periodic inputs of our flow cell. This leads to a fit of the amplitude χ of the form

$$\chi = A \frac{(1 - e^{-k_{on}T/2})(1 - e^{-k_{off}T/2})}{1 - e^{-(k_{on}+k_{off})T/2}} + \delta, \quad [7]$$

with T representing the period of oscillation of the stimulus in the flow cell, A representing the gain of the system, and an offset value, δ , that takes into account the fact that, even at high frequencies, the amplitude of nuclear amplitude of the oscillatory signal is non-zero because of the autofluorescence intensity changes due to size variations. Both fits lead to consistent extraction of the slowest rate constant in the pathway.

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- Shannon CE (1948) A mathematical theory of communication. *Bell Syst Tech J* 27:379–423 and 623–656.
- Alberts B, et al. (2002) *Molecular Biology of the Cell* (Garland, New York), 4th Ed.
- Ramanathan S, Detwiler PB, Sengupta AN, Shraiman BI (2005) G-protein-coupled enzyme cascades have intrinsic properties that improve signal localization and fidelity. *Biophys J* 88:3063–3071.
- Gustin MC, Albertyn J, Alexander M, Davenport K (1998) MAP kinase pathways in the yeast *Saccharomyces cerevisiae*. *Microbiol Mol Biol Rev* 62:1264–1300.
- Hohmann S (2002) Osmotic stress signaling and osmoadaptation in yeasts. *Microbiol Mol Biol Rev* 66:300–372.
- Bahn Y, et al. (2007) Sensing the environment: Lessons from fungi. *Nat Rev Microbiol* 5:57–69.
- Posas F, Saito H (1998) Activation of the yeast SSK2 MAP kinase kinase by the SSK1 two-component response regulator. *EMBO J* 17:1385–1394.
- Posas F, (1996) Yeast HOG1 MAP kinase cascade is regulated by a multistep phosphorylation mechanism in the SLN1-YPD1-SSK1 “two-component” osmosensor. *Cell* 86:865–875.
- Posas F, Saito H (1997) Osmotic activation of the HOG MAPK pathway via Ste11p MAPKKK: Scaffold role of Pbs2p MAPKK. *Science* 276:1702–1705.
- Tatebayashi K, et al. (2006) Adaptor functions of Cdc42, Ste50, and Sho1 in the yeast osmoregulatory HOG MAPK pathway. *EMBO J* 25:3033–3044.
- Maeda T, Takekawa M, Saito H (1995) Activation of yeast PBS2 MAPKK by MAPKKs or by binding of an SH3-containing osmosensor. *Science* 269:554–558.
- Van Wuytswinkel O, et al. (2000) Response of *Saccharomyces cerevisiae* to severe osmotic stress: Evidence for a novel activation mechanism of the HOG MAP kinase pathway. *Mol Microbiol* 37:382–397.
- O'Rourke SM, Herskowitz I (2004) Unique and redundant roles for HOG MAPK pathway components as revealed by whole-genome expression analysis. *Mol Biol Cell* 15:532–542.
- Hao N, et al. (2007) A systems-biology analysis of feedback inhibition in the Sho1 osmotic-stress-response pathway. *Curr Biol* 17:659–667.
- Ferrigno P, Posas F, Koepp D, Saito H, Silver PA (1998) Regulated nucleocytoplasmic exchange of HOG1 MAPK requires the importin beta homologs NMD5 and XPO1. *EMBO J* 17:5606–5614.
- Reiser V, Ruis H, Ammerer G (1999) Kinase activity-dependent nuclear export opposes stress-induced nuclear accumulation and retention of Hog1 mitogen-activated protein kinase in the budding yeast *Saccharomyces cerevisiae*. *Mol Biol Cell* 10:1147–1161.
- Sharma P, Mondal AK (2005) Evidence that C-terminal non-kinase domain of Pbs2p has a role in high osmolarity-induced nuclear localization of Hog1p. *Biochem Biophys Res Commun* 328:906–913.
- Alepuz PM, de Nadal E, Zapater M, Ammerer G, Posas F (2003) Osmotically-induced transcription by Hot1 depends on a Hog1-mediated recruitment of the RNA Pol II. *EMBO J* 22:2433–2442.
- Krantz M, Becit E, Hohmann S (2006) Comparative genomics of the HOG-signalling system in fungi. *Curr Genet* 49:137–151.
- Krantz M, Becit E, Hohmann S (2006) Comparative analysis of HOG pathway proteins to generate hypotheses for functional analysis. *Curr Genet* 49:152–165.
- Furukawa K, Hoshi Y, Maeda T, Nakajima T, Abe K (2005) *Aspergillus nidulans* HOG pathway is activated only by two-component signalling pathway in response to osmotic stress. *Mol Microbiol* 56:1246–1261.
- Mattison CP, Ota IM (2000) Two protein tyrosine phosphatases, Ptp2 and Ptp3, modulate the subcellular localization of the Hog1 MAP kinase in yeast. *Genes Dev* 14:1229–1235.

Supporting Information

Hersen *et al.* 10.1073/pnas.0710770105

SI Text

Single-Cell Permeability Estimation. From the measurements of size fluctuations (Fig. 3 and Fig. S1), it is possible to extract a precise value for the water permeability of yeast cells in the S288C background. Size fluctuations are due to water exchange between the environment and the cytoplasm that is driven by an osmotic pressure gradient across the cell wall and the plasma membrane. Using a d'Arcy's law to model the water transport across the cell plasma membrane, the water flux is proportional to the gradient of pressure across the membrane:

$$\vec{q} = -\frac{k}{v} \nabla P. \quad [1]$$

Using mass conservation and assuming a spherical shape leads to:

$$\rho \partial_t R = -\frac{k}{v} \partial_r P. \quad [2]$$

The driving force is the gradient of osmotic pressure that can be estimated as:

$$\partial_r P \sim \frac{\Pi_{\text{out}} - \Pi_{\text{in}}}{e}. \quad [3]$$

This leads us to write for a dilute solution and after linearization that the size fluctuations follow the osmotic fluctuations with a typical timescale $\tau = ev\rho R_{\text{eq}}/3k\Pi_{\text{eq}}$, where e is the plasma membrane thickness, v the viscosity of water, and ρ its density. R_{eq} and Π_{eq} are the size and internal osmotic pressure at equilibrium. This time scale is related to the water permeability by

$$L_p = \frac{k}{ev\rho} = \frac{R_{\text{eq}}}{3\Pi_{\text{eq}}\tau}. \quad [4]$$

Using our experimental result for the mechanical response of yeast cells ($\tau = 4.8 \pm 0.9$ s) and assuming reasonable values for $R_{\text{eq}} = 2.5 \mu\text{m}$ and $\Pi_{\text{eq}} = 1$ MPa gives the following water permeability:

$$L_p = 1.75 \times 10^{-13} \text{ m}\cdot\text{Pa}^{-1}\cdot\text{s}^{-1}. \quad [5]$$

This value is in excellent agreement with data from the literature for various organisms. This shows how this setup can be used to measure precisely the dynamics of water transport.

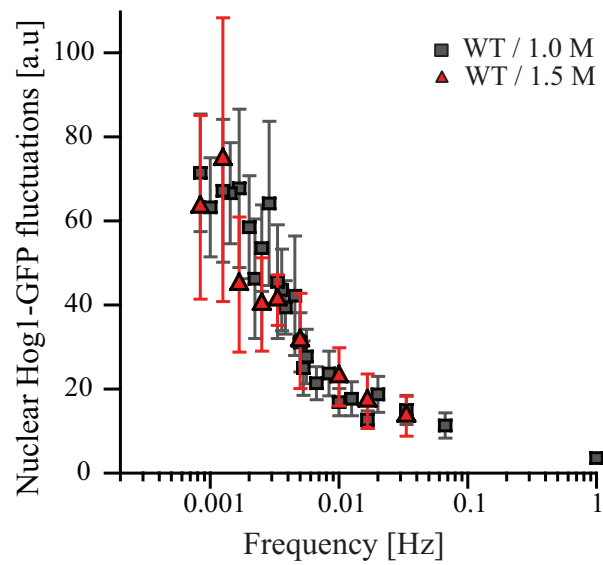


Fig. S1. Hog1 localization responses of the HOG pathway in *S. cerevisiae* at different osmolar pressures. The response of Hog1 localization to oscillating input is studied for different sorbitol concentrations. Each point represents the average response amplitude as measured by Hog1-GFP colocalization with Htb2-mCherry over, typically, 5–10 cells. Error bars denote one standard deviation from the mean. Yeast cells have bandwidths of $\omega_b = 4.6 \times 10^{-3} \pm 1 \times 10^{-3}$ Hz (filled squares) for 1 M sorbitol oscillation and (filled triangles) $\omega_b = 4.6 \times 10^{-3} \pm 2 \times 10^{-3}$ Hz for a 1.5 M sorbitol oscillation.

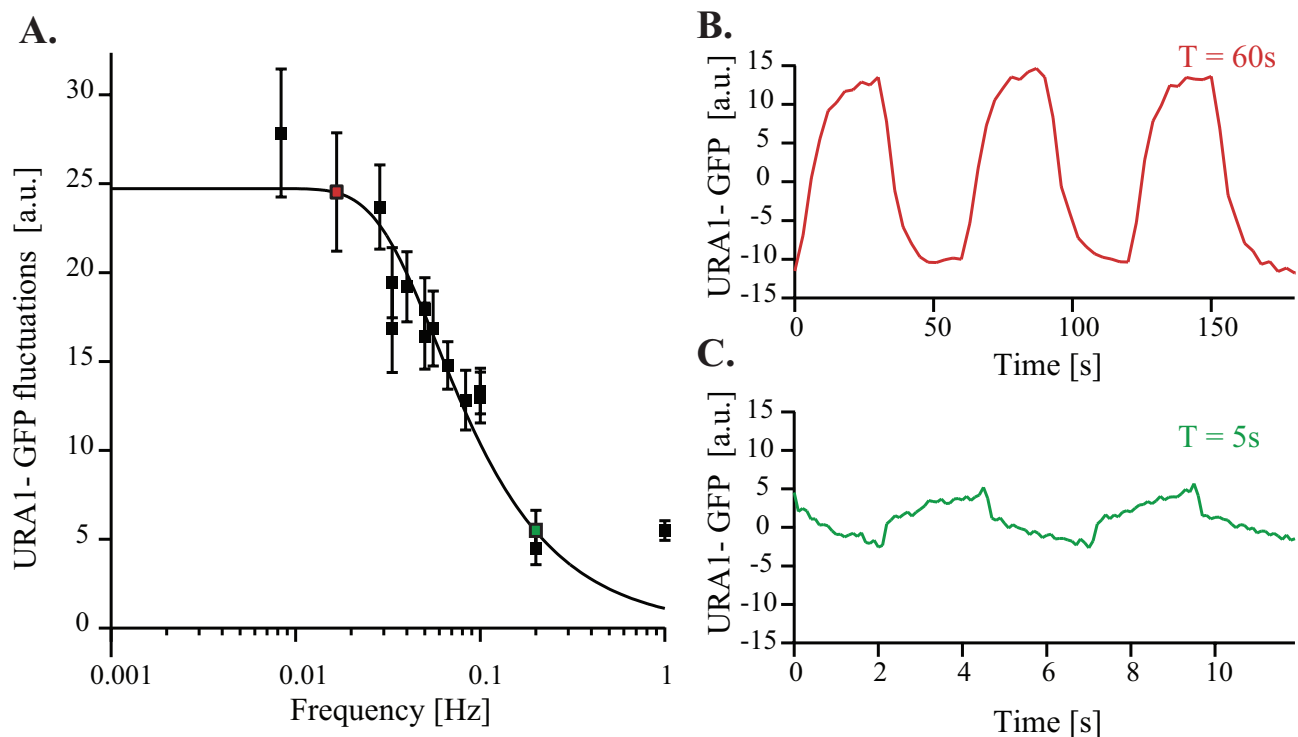
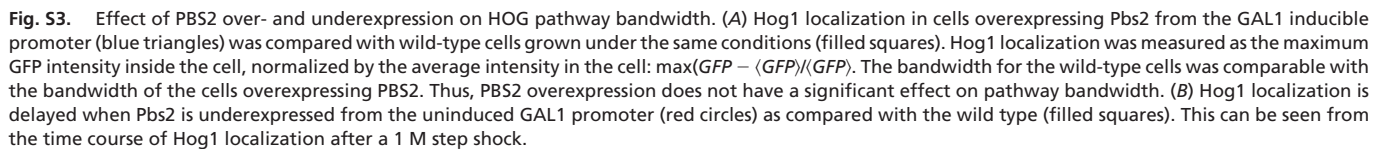


Fig. S2. The mechanical response of *S. cerevisiae*. (A) The mechanical response of a *S. cerevisiae* cell to oscillating 1 M sorbitol input is measured as amplitude variation in cytoplasmic fluorescence as a function of input frequency. The strain used contains the cytoplasmic Ura1 protein tagged with GFP. Each point represents 5–10 cells. Error bars denote one standard deviation from the mean. Size response is a low-pass filter with a bandwidth $\omega_b \sim 0.03 \pm 0.02$ Hz. This bandwidth is consistent with the mechanical response results discussed in the main text (Fig. 3). (B) At frequencies slower than ω_b , the cell size response follows the input faithfully ($\omega = 17 \times 10^{-3}$ Hz, red squares, red line). (C) At frequencies higher than the bandwidth ($\omega = 0.2$ Hz, green squares, green line), the magnitude of cell size response drops dramatically.



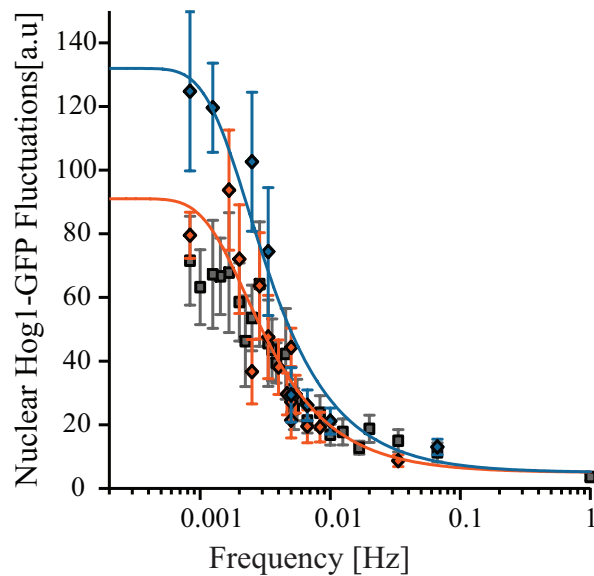


Fig. S4. Hog1 localization response for diploid cells. The response of Hog1 localization to 1 M sorbitol oscillating input is studied for haploid and diploid cells. Each point represents the average response amplitude as measured by Hog1-GFP colocalization with Htb2-mCherry over, typically, 5–10 cells. Error bars denote one standard deviation from the mean. Haploid cells (filled squares) are compared with PBS2/PBS2 diploids (blue diamonds, $\omega_b = 4.6 \times 10^{-3} \pm 1.5 \times 10^{-3}$ Hz), and PBS2/pbs2 diploid cells (red diamonds, $\omega_b = 4.2 \times 10^{-3} \pm 1.5 \times 10^{-3}$ Hz). Homozygous and heterozygous diploids show the same bandwidth. Interestingly, the diploid bandwidth is very close to the haploid bandwidth (filled squares, $\omega_b = 4 \times 10^{-3} \pm 1 \times 10^{-3}$ Hz).

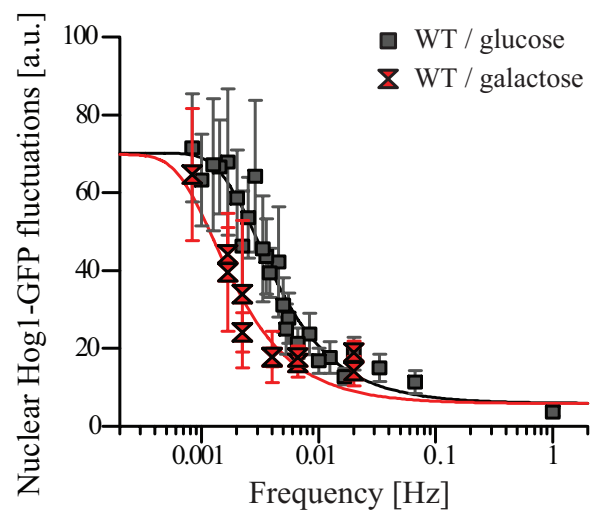


Fig. S5. Effect of carbon source and selective media on HOG pathway bandwidth. Comparison of Hog1-GFP nuclear colocalization in wild-type cells grown in 2% galactose selective (–Leu) synthetic complete (SC) media (▲) with measurements of cells grown in 2% glucose SC (filled squares) shows that growth conditions have an effect on pathway bandwidth. Thus in Fig. S3, we compare cells grown under the same growth conditions.

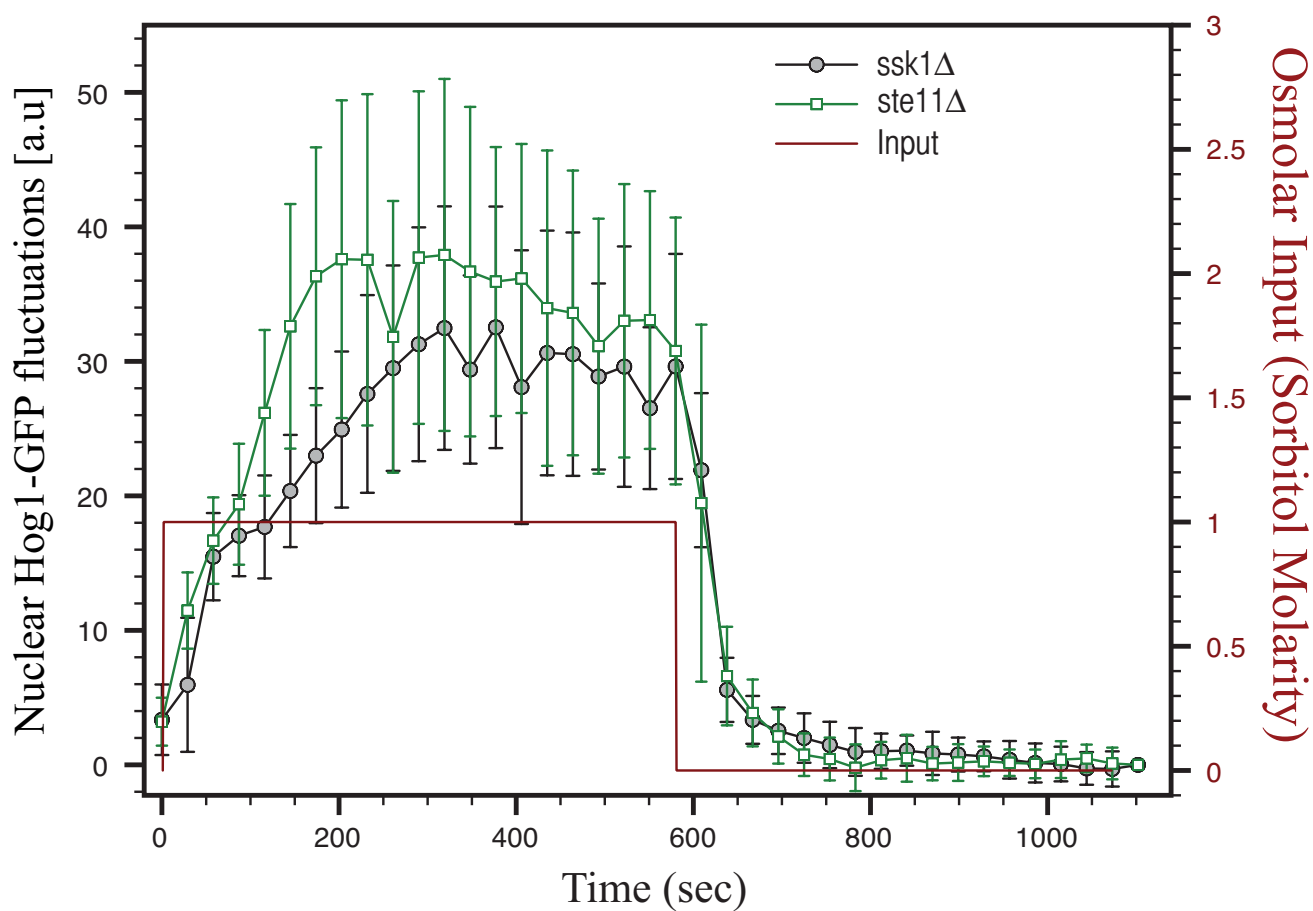
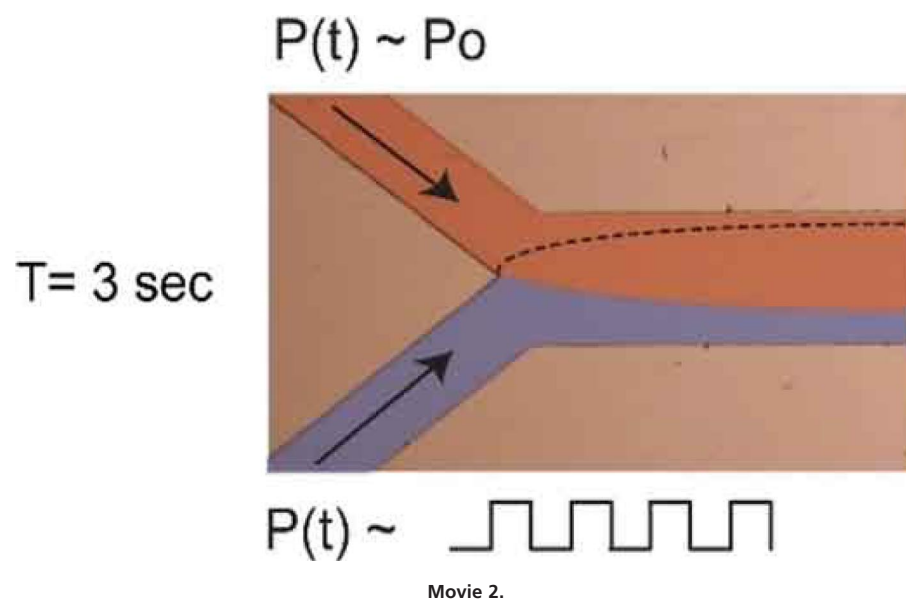


Fig. S6. Comparison of activation and deactivation rates of the Ste11 and Ssk1 branches. The time course of Hog1 nuclear GFP levels are shown for *ste11Δ* (green) and *ssk1Δ* (gray) cells in response to a 1 M impulse of sorbitol (red) as a function of time. Although the time to accumulate Hog1 in the nucleus is clearly slower in cells lacking the Ssk1 branch of the pathway, the deactivation profiles of both mutants, when the pulse of sorbitol is turned off, is identical to within error bars. This suggests that the deactivation rates of the two branches are set by that of either Pbs2 or Hog1.

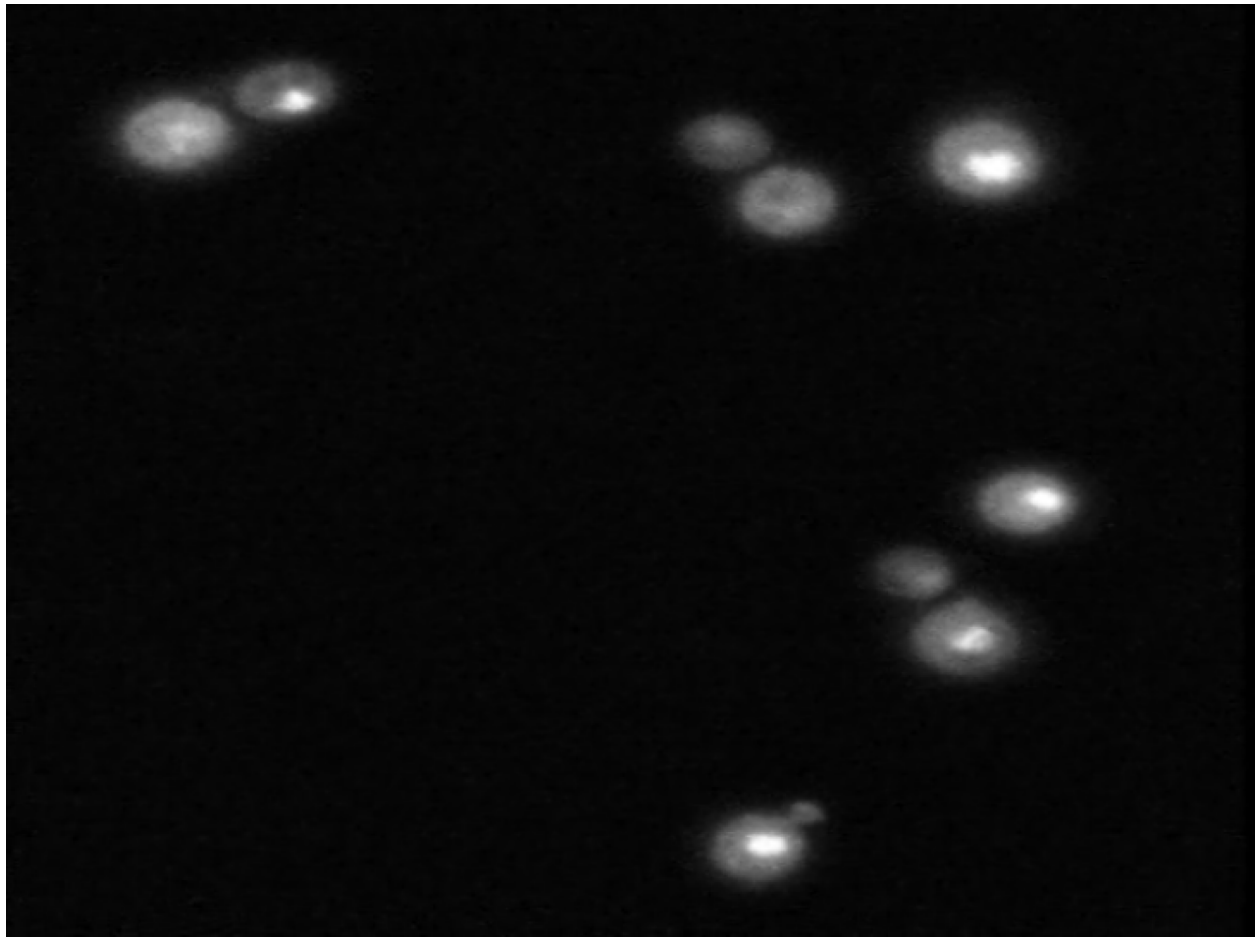


Movie 1.

[Movie S1 \(WMV\)](#)



[Movie S2 \(WMV\)](#)



Movie 3.

[Movie S3 \(WMV\)](#)

Table S1. Yeast strains and plasmids

Name	Genotype	Source
BY4742	Mat a, his3 Δ 1, leu2 Δ 0, ura3 Δ 0, met15 Δ 0	Deletion collection (1)
BY4741	Mat α , his3 Δ 1, leu2 Δ 0, lys2 Δ 0, ura3 Δ 0	GFP collection (2)
ySR229	Mat a, leu2 Δ 0, lys2 Δ 0, ura3 Δ 0 HOG1-GFP-HIS3	GFP collection (2)
ySR255	MAT a, leu2 Δ 0, lys2 Δ 0, HOG1-GFP-HIS3, HTB2-mCherry-URA3	This study
ySR448	MAT a, leu2 Δ 0, met15 Δ 0, HOG1-GFP-HIS3, HTB2-mCherry-URA3, sho1::KAN	This study
ySR450	MAT a, leu2 Δ 0, lys2 Δ 0, met15 Δ 0, HOG1-GFP-HIS3, HTB2-mCherry-URA3, pbs2::KAN	This study
ySR555	Mat a, leu2 Δ 0, lys2 Δ 0, ura3 Δ 0, GPD1-GFP-HIS3	GFP collection (2)
ySR648	Mat a/ α , leu2 Δ 0, HOG1-GFP-HIS3/HOG1-GFP-HIS3, HTB2-mCherry-URA3/HTB2-mCherry-URA3, pbs2::KAN/PBS2	This study
ySR649	Mat a/ α , leu2 Δ 0, HOG1-GFP-HIS3/HOG1-GFP-HIS3, HTB2-mCherry-URA3/HTB2-mCherry-URA3, PBS2/PBS2	This study
ySR654	MAT a, met15 Δ 0, HOG1-GFP-HIS3, HTB2-mCherry-URA3, ste11::LEU2	This study
ySR669	MAT a, met15 Δ 0, HOG1-GFP-HIS3, HTB2-mCherry-URA3, ssk1::LEU2	This study
ySR676	MAT a, leu2 Δ 0, met15 Δ 0 HOG1-GFP-HIS3, pbs2::URA3	This study

All strains are in the S288C background. To titrate the expression of PBS2, we constructed pSR261, which contains a P_{GAL1}-PBS2-mCherry fusion inserted between the XhoI and PacI restriction sites on the LEU2 CEN plasmid pRS415 (3).

1. Winzeler EA, et al. (1999) Functional characterization of the *S. cerevisiae* genome by gene deletion and parallel analysis. *Science* 285:901–906.
2. Huh WK, et al. (2003) Global analysis of protein localization in budding yeast. *Nature* 425(6959):686–691.
3. Simons RW, Houman F, Kleckner N (1987) Improved single and multicopy lac-based cloning vectors for protein and operon fusions. *Gene* 53:85–96.