NUXMV: Introduction*

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- 2 NUXMV interactive shell
- NUXMV Modeling
 - Basic Types
 - Initial States
 - Expressions
 - Transition Relation
 - Miscellany
 - Constraint Style Modeling
- Modules
 - Modules Definition
 - Modules Composition
- 5 Exercises

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Introduction

- NUXMV is a new symbolic model checker developed by FBK-IRST.
 - based on the NuSMV model checker
 - project url: https://nuxmv.fbk.eu/
 - the binary of NUXMV is available for non-commercial or academic purposes only!
- NUXMV allows for verifying
 - finite-state systems through state-of-the-art SAT-based algorithms;
 - infinite-state systems (e.g. systems with real and integer variables)
 through SMT-based techniques running on top of MathSAT5;
- NUXMV supports synchronous systems; asynchronous systems are no longer supported!

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Interactive shell [1/3]

- nuxmv -int (or NuSMV -int) activates an interactive shell
- help shows the list of all commands (if a command name is given as argument, detailed information for that command will be provided).
 note: option -h prints the command line help for each command.
- reset resets the whole system (in order to read in another model and to perform verification on it).
- read_model [-i filename] sets the input model and reads it.
- go, go_bmc, go_msat initialize NUXMV for verification or simulation with a specific backend engine.

Interactive shell [2/3]

- pick_state [-v] [-a] [-r | -i] picks a state from the set of initial states.
 - -v prints the chosen state.
 - -r picks a state from the set of the initial states randomly.
 - -i picks a state from the set of the initial states interactively.
 - -a displays all state variables (requires -i).
- simulate [-p | -v] [-a] [-r | -i] -k N generates a sequence of at most N transitions starting from the current state.
 - -p prints the changing variables in the generated trace;
 - \bullet -v prints changed and unchanged variables in the generated trace;
 - -a prints all state variables (requires -i);
 - -r at every step picks the next state randomly.
 - -i at every step picks the next state interactively.
- print_current_state [-h] [-v] prints out the current state.
 - v prints all the variables.

Interacting Shell [2/3] - Output Example

```
nuXmv > reset; read_model -i example01.smv ; go ; pick_state -v; simulate -v
Trace Description: Simulation Trace
Trace Type: Simulation
 -> State: 1.1 <-
   b0 = FALSE
****** Simulation Starting From State 1.1 ******
Trace Description: Simulation Trace
Trace Type: Simulation
 -> State: 1.1 <-
   b0 = FALSE
 -> State: 1.2 <-
   b0 = TRUE
 -> State: 1.3 <-
   b0 = FALSE
 -> State: 1.4 <-
   b0 = TRUE
 -> State: 1.5 <-
   b0 = FALSE
  -> State: 1.6 <-
   b0 = TRUE
```

. . .

Interacting Shell [3/3]

- goto_state state_label makes state_label the current state (it is used to navigate along traces).
- show_traces [-t] [-v] [-a | TN[.FS[:[TS]]] prints the trace *TN* starting from state *FS* up to state *TS*
 - -t prints the total number of stored traces
 - verbosely prints traces content;
 - -a prints all the currently stored traces
- show_vars [-s] [-f] [-i] [-t] [-v] prints the variables content and type
 - -s print state variables;
 - -f print frozen variables;
 - -i print input variables;
 - -t prints the number of variables;
 - v prints verbosely;
- quit stops the program.

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The first SMV program

- an SMV program is composed by a number of modules;
- each module, contains:
 - state variable declarations;
 - assignments defining the valid initial states;
 - assignments defining the transition relation;

Example:

```
MODULE main

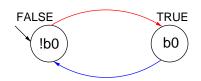
VAR

b0 : boolean;

ASSIGN

init(b0) := FALSE;

next(b0) := !b0;
```



Basic Types [1/2]

```
boolean: TRUE, FALSE, ...
  x : boolean;
enumerative:
  s : {ready, busy, waiting, stopped};
bounded integers (intervals):
  n: 1..8;
integers*: -1, 0, 1, ...
  n : integer;
rationals: 1.66, f'2/3, 2e3, 10e-1, ...
  r : real;
words: used to model arrays of bits supporting bitwise logical and
arithmetic operations.
  unsigned word[3];
  signed word[7];
*: integer numbers must be within C/C++ INT_MIN and INT_MAX bounds
```

Basic Types [2/2]

arrays:

declared with a couple of lower/upper bounds for the index and a type

```
VAR
  x : array 0..10 of boolean; -- array of 11 elements
  y : array -1..1 of {red, green, orange}; -- array of 3 elements
  z : array 1..10 of array 1..5 of boolean; -- array of array
ASSIGN
  init(x[5]) := bool(1);
  init(y[0]) := {red, green}; -- any value in the set
  init(z[3][2]) := TRUE;
```

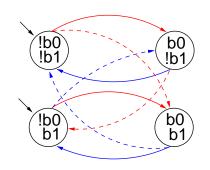
Remarks:

Array indexes must be constants;

Adding a state variable

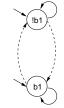
```
MODULE main
VAR
b0 : boolean;
b1 : boolean;

ASSIGN
init(b0) := FALSE;
next(b0) := !b0;
```



Remarks:

- the FSM is the result of the synchronous composition of the "subsystems" for b0 and b1
- the new state space is the cartesian product of the ranges of the variables.



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Initial States [1/2]

Example:

```
init(x) := FALSE; -- x must be FALSE
init(y) := {1, 2, 3}; -- y can be either 1, 2 or 3
init(<variable>) := <simple_expression>;
```

- constrains the initial value of <variable> to satisfy the <simple_expression>;
- the initial value of an unconstrained variable can be any of those allowed by its domain;

set of initial states

is given by the set of states whose variables satisfy all the init() constraints in a module.

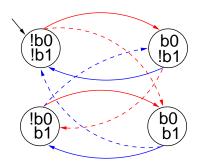
Initial States [2/2]

Example:

```
MODULE main
VAR
  b0 : boolean;
  b1 : boolean;

ASSIGN
  init(b0) := FALSE;
  next(b0) := !b0;

init(b1) := FALSE;
```



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Expressions [1/3]

arithmetic operators:

```
+ - * / mod - (unary)
```

comparison operators:

```
= != > < <= >=
```

logic operators:

```
& | xor ! (not) -> <->
```

bitwise operators:

- set operators: $\{v1, v2, \dots, vn\}$
 - in: tests a value for membership in a set (set inclusion)
 - union: takes the union of 2 sets (set union)
- count operator: counts number of true *boolean* expressions

```
count(b1 + b2 + ... + bn)
```

Expressions [2/3]

case expression:

```
case C/C++ equivalent:

c1 : e1; if (c1) then e1;

c2 : e2; else if (c2) then e2;

...

TRUE : en; else en;
```

• if-then-else expression:

```
cond_expr ? basic_epxr 1 : basic_expr2
```

- conversion operators: toint, bool, floor, and
 - swconst, uwconst: convert an integer to a signed and an unsigned word respectively.
 - word1 converts boolean to a single word bit.
 - unsigned and signed convert signed word to unsigned word and vice-versa.

Expressions [3/3]

 expressions in SMV do not necessarily evaluate to one value. In general, they can represent a set of possible values.

```
init(var) := \{a,b,c\} union \{x,y,z\};
```

- The meaning of := in assignments is that the lhs can non-deterministically be assigned to any value in the set of values represented by the rhs.
- A constant c is considered as a syntactic abbreviation for {c} (the singleton containing c).

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Transition Relation [1/2]

Transition Relation

specifies a constraint on the values that a variable can assume in the *next* state, given the value of variables in the *current* state.

```
next(<variable>) := <next_expression>;
```

<next_expression> can depend both on "current" and "next" variables:

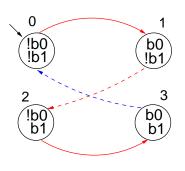
```
next(a) := { a, a+1 } ;
next(b) := b + (next(a) - a) ;
```

- the next value of an unconstrained variable evolves non-deterministically;

Transition Relation [2/2]

Example: modulo-4 counter

```
MODULE main
 VAR.
   b0 : boolean;
   b1 : boolean;
 ASSIGN
   init(b0) := FALSE;
   next(b0) := !b0;
   init(b1) := FALSE;
   next(b1) := case
       b0
            : !b1;
       TRUE: b1;
     esac;
```



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Output Variable [1/2]

output variable

is a variable whose value is deterministically depends on the value of other "current" state variables and for which no init() or next() are defined.

```
<variable> := <simple_expression>;
```

- <simple_expression> must evaluate to values in the domain of the <variable>.
- used to model outputs of a system;

Output Variable [2/2]

Example:

```
MODULE main
 VAR.
   b0 : boolean;
   b1 : boolean;
   out : 0..3;
 ASSIGN
   init(b0) := FALSE;
                                                                       3
   next(b0) := !b0;
   init(b1) := FALSE;
next(b1) := ((!b0 & b);
(t !b1));
   out := toint(b0) + 2*toint(b1);
```

Assignment Rules (:=)

single assignment rule – each variable may be assigned only once;
 lllegal examples:

Assignment Rules (:=)

single assignment rule – each variable may be assigned only once;
 lllegal examples:

 circular dependency rule – a set of equations must not have "cycles" in its dependency graph, unless broken by delays;

DEFINE declarations

```
DEFINE <id> := <simple_expression>;
```

- similar to C/C++ macro definitions: each occurrence of the defined symbol is replaced with the body of the definition
- provide an alternative way of defining output variables;

Example:

```
MODULE main

VAR

b0 : boolean;

b1 : boolean;

ASSIGN

init(b0) := FALSE;

next(b0) := !b0;

init(b1) := FALSE;

next(b1) := ((!b0 & b1) | (b0 & !b1));

DEFINE

out := toint(b0) + 2*toint(b1);
```

Example: modulo 4 counter with reset

The counter can be reset by an external "uncontrollable" signal.

```
MODULE main
VAR.
 b0 : boolean; b1 : boolean; reset : boolean;
ASSIGN
  init(b0) := FALSE;
  init(b1) := FALSE;
 next(b0) := case
                reset = TRUE : FALSE;
                reset = FALSE : !b0;
               esac;
 next(b1) := case
                                                      3
                reset : FALSE:
                TRUE : ((!b0 & b1) | (b0 & !b1));
              esac:
DEFINE
  out := toint(b0) + 2*toint(b1);
```

Exercise 1

Exercise:

simulate the system with NUXMV and draw the FSM.

```
MODULE main
VAR
  request : boolean;
  state : { ready, busy };

ASSIGN
  init(state) := ready;
  next(state) :=
    case
      state = ready & request : busy;
      TRUE : { ready, busy };
    esac;
```

Exercise 1

Exercise:

simulate the system with NUXMV and draw the FSM.

```
MODULE main
                                                                 rec
                                             rec
VAR.
  request : boolean;
  state : { ready, busy };
ASSTGN
                                             !rec
                                                                 req
  init(state) := ready;
  next(state) :=
    case
      state = ready & request : busy;
      TRUE.
                                : { ready, busy };
    esac;
```

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Constraint Style Modeling [1/3]

```
MODULE main
VAR
request : boolean; state : {ready,busy};
ASSIGN
  init(state) := ready;
  next(state) := case
        state = ready & request : busy;
        TRUE : {ready,busy};
        esac;
```

Every program can be alternatively defined in a constraint style:

```
MODULE main

VAR

request : boolean;

state : {ready,busy};

INIT

state = ready

TRANS

(state = ready & request) -> next(state) = busy
```

Constraint Style Modeling [2/3]

- a model can be specified by zero or more constraints on:
 - invariant states:INVAR <simple_expression>
 - initial states:INIT <simple_expression>
 - transitions:
 TRANS <next_expression>
- constraints can be mixed with assignments;
- any propositional formula is allowed as constraint;
- not all constraints can be easily rewritten in terms of assignments!

```
TRANS
next(b0) + 2*next(b1) + 4*next(b2) =
(b0 + 2*b1 + 4*b2 + tick) mod 8
```

Constraint Style Modeling [3/3]

- Models written in assignment style:
 - by construction, there is always at least one initial state;
 - by construction, all states have at least one next state;
 - non-determinism is apparent (unassigned variables, set assignments...).
- Models written in **constraint style**:
 - INIT constraints can be inconsistent ⇒ no initial state!
 - any specification (also SPEC 0) is vacuously true.
 - TRANS constraints can be inconsistent: ⇒ deadlock state!

```
MODULE main

VAR b : boolean;

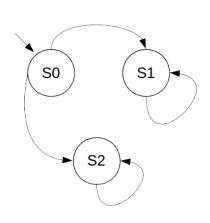
TRANS b -> FALSE;
```

- tip: use check_fsm to detect deadlock states
- non-determinism is hidden:

```
TRANS (state = ready & request) -> next(state) = busy
```

Example: Constraint Style & Case

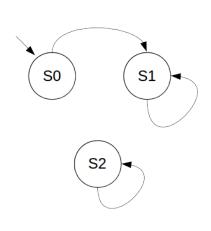
```
MODULE main()
VAR.
  state : {S0, S1, S2};
DEFINE
  go_s1 := state != S2;
  go_s2 := state != S1;
TNTT
  state = S0;
TRANS
case
  go_s1 : next(state) = S1;
  go_s2 : next(state) = S2;
esac:
```



• **Q**: does it correspond to the FSM?

Example: Constraint Style & Case

```
MODULE main()
VAR.
  state : {S0, S1, S2};
DEFINE
  go_s1 := state != S2;
  go_s2 := state != S1;
TNTT
  state = S0;
TRANS
case
  go_s1 next(state) = S1;
  go_s2 : next(state) = S2;
esac:
```

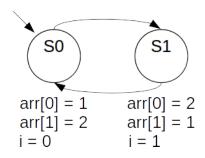


Q: does it correspond to the FSM? No: cases are evaluated in order!

Example: Constraint Style & Swap

```
MODULE main()
VAR.
   arr: array 0..1 of {1,2};
   i : 0..1;
ASSIGN
  init(arr[0]) := 1;
  init(arr[1]) := 2;
  init(i) := 0;
  next(i) := 1-i;
TRANS
```

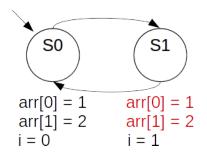
next(arr[i]) = arr[1-i] &
next(arr[1-i]) = arr[i];



• Q: does it correspond to the FSM?

Example: Constraint Style & Swap

```
MODULE main()
VAR.
   arr: array 0..1 of {1,2};
   i : 0..1;
ASSTGN
  init(arr[0]) := 1;
  init(arr[1]) := 2;
  init(i) := 0;
  next(i) := 1-i;
TRANS
```



• Q: does it correspond to the FSM? No: everything inside the next() operator is evaluated within the next state, indexes included!

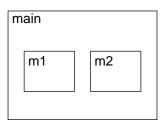
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Modules [1/3]

SMV program = main module + 0 or *more* other modules

- a module can be instantiated as a VAR in other modules
- dot notation for accessing variables that are local to a module instance (e.g., m1.out, m2.out).



Modules [2/3]

A module declaration can be parametric:

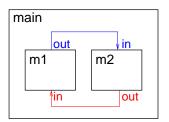
- a parameter is passed by reference;
- any expression can be used as parameter;

```
MODULE counter(in)

VAR out: 0..9;
...

MODULE main

VAR m1 : counter(m2.out);
 m2 : counter(m1.out);
```



Modules [3/3]

- modules can be composed
- modules without parameters and assignments can be seen as simple records

```
MODULE point

VAR

VAR c: circle;

x: -10..10;

y: -10..10;

MODULE circle

MODULE circle

VAR

center: point;

radius: 0..10;

MODULE main

VAR c: circle;

ASSIGN

init(c.center.x) := 0;

init(c.radius) := 5;

VAR
```

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Synchronous composition [1/2]

The composition of modules is **synchronous** by default: *all modules move at each step*.

```
MODULE cell(input)

VAR

val : {red, green, blue};

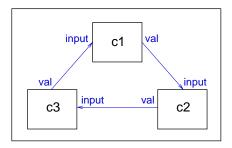
ASSIGN

next(val) := input;

MODULE main

VAR

c1 : cell(c3.val);
c2 : cell(c1.val);
c3 : cell(c2.val);
```



Synchronous composition [2/2]

A possible execution:

step	c1.val	c2.val	c3.val
0	red	green	blue
1	blue	red	green
2	green	blue	red
3	red	green	blue
4			
5	red	green	blue

Asynchronous composition [1/2]

Asynchronous composition can be obtained using keyword process: one process moves at each step.

```
MODULE cell(input)
VAR

val : {red, green, blue};
ASSIGN next(val) := input;
FAIRNESS running

MODULE main
VAR

c1 : process cell(c3.val);
c2 : process cell(c1.val);
c3 : process cell(c2.val);
```

Each process has a boolean running variable:

- true iff the process is selected for execution;
- can be used to guarantee a fair scheduling of processes.

Asynchronous composition [2/2]

A possible execution:

step	running	c1.val	c2.val	c3.val
0	-	red	green	blue
1	c2	red	red	blue
2	c1	blue	red	blue
3	c1	blue	red	blue
4	c3	blue	red	red
5	c2	blue	blue	red
6	c3	blue	blue	blue
		blue	blue	blue

Warning: in ${\tt NUXMV}$ processes are deprecated!

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Exercise: Adder [1/3]

```
MODULE bit-adder(in1, in2, cin)
VAR.
  sum : boolean:
 cout : boolean;
ASSTGN
  next(sum) := (in1 xor in2) xor cin:
  next(cout) := (in1 & in2) | ((in1 | in2) & cin);
MODULE adder(in1. in2)
VAR.
  bit[0] : bit-adder(in1[0], in2[0], 0):
  bit[1] : bit-adder(in1[1], in2[1], bit[0].cout);
  bit[2] : bit-adder(in1[2], in2[2], bit[1].cout):
  bit[3] : bit-adder(in1[3], in2[3], bit[2].cout);
DEFINE
  sum[0] := bit[0].sum:
  sum[1] := bit[1].sum;
  sum[2] := bit[2].sum:
  sum[3] := bit[3].sum:
  overflow := bit[3].cout;
```

Exercise: Adder [2/3]

```
MODULE main
VAR.
  in1: array 0..3 of boolean;
  in2: array 0..3 of boolean;
 a : adder(in1, in2):
ASSIGN
 next(in1[0]) := in1[0]; next(in1[1]) := in1[1];
 next(in1[2]) := in1[2]; next(in1[3]) := in1[3];
 next(in2[0]) := in2[0]: next(in2[1]) := in2[1]:
 next(in2[2]) := in2[2]: next(in2[3]) := in2[3]:
DEFINE
 op1 := toint(in1[0]) + 2*toint(in1[1]) + 4*toint(in1[2]) +
         8*toint(in1[3]):
 op2 := toint(in2[0]) + 2*toint(in2[1]) + 4*toint(in2[2]) +
         8*toint(in2[3]):
  sum := toint(a.sum[0]) + 2*toint(a.sum[1]) + 4*toint(a.sum[2]) +
         8*toint(a.sum[3]) + 16*toint(a.overflow):
```

Exercise: Adder [3/3]

Exercise:

- simulate a random execution of the "adder" system;
- after how many steps the adder stores the computes the final sum value?
- add a reset control which changes the values of the operands and restarts the computation of the sum

Exercises Solutions

- will be uploaded on course website within a couple of days
- send me an email if you need help or you just want to propose your own solution for a review

 learning programming languages requires practice: try to come up with your own solutions first!