# Statistical Inference course project - Part 1

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#### Overview

In this project you will investigate the exponential distribution in R and compare it with the Central Limit Theorem. The exponential distribution can be simulated in R with rexp(n, lambda) where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda.

#### Given instructions

- Set lambda = 0.2 for all of the simulations (lambda = 0.2)
- Investigate the distribution of averages of 40 exponentials (exponentials = 40)
- Do a thousand simulations (simulations = 1000)

### Simulating the mean

- First we set the seed for reproducibility using the set.seed() function
- We then initialize the variables lambda, exponentials and the simulations

```
# Setting the seed for reproducibility
set.seed(2000)

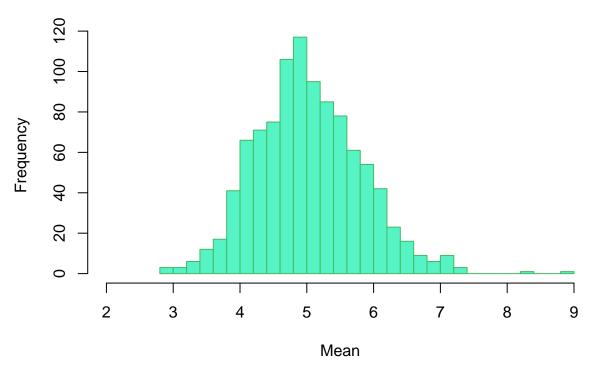
# As per given details initializing the variables
lambda <- 0.2
exponentials <- 40
simulations <- 1000

# Calculating the mean over 1000 simulations
meanexponents <- apply(replicate(simulations, rexp(exponentials, lambda)), 2, mean)

#Plotting the Mean of 40 Exponentials

hist(meanexponents, breaks = 40, xlim = c(2,9),
    main = "Mean of 40 Exponentials over 1000 Simulations",
    xlab = "Mean", ylab = "Frequency", col = "#56F4C4",
    border = "#45BA64")</pre>
```





We first compare the sample mean generated out of the 1000 simulations with the theoretical mean.

```
#Theoretical mean
theo_mean <- 1/lambda
theo_mean

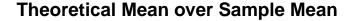
## [1] 5
#Sample mean of simulations
sample_mean <- mean(meanexponents)</pre>
```

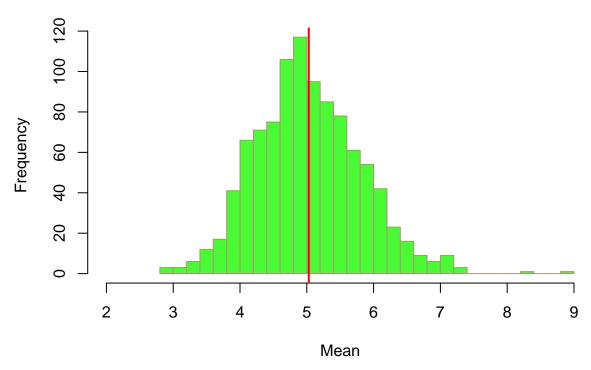
#### ## [1] 5.02941

sample\_mean

From the above observations we find the Sample mean and the theoretical mean are nearly same, now we will go ahead and plot the theoretical mean over the sample mean

```
# Plotting theoretical mean over sample mean
hist(meanexponents, breaks = 40, xlim = c(2,9),
    main = "Theoretical Mean over Sample Mean",
    xlab = "Mean", ylab = "Frequency", col = "#49FA34",
    border = "#AC947A")
abline(v= mean(sample_mean), lwd = "2", col = "#FF0000")
```





Now we compare the Theoretical Variance over the Sample Variance

```
# Sample Variance is the square of the Standard deviation
sample_variance <- (sd(meanexponents))^2
sample_variance

## [1] 0.6168082

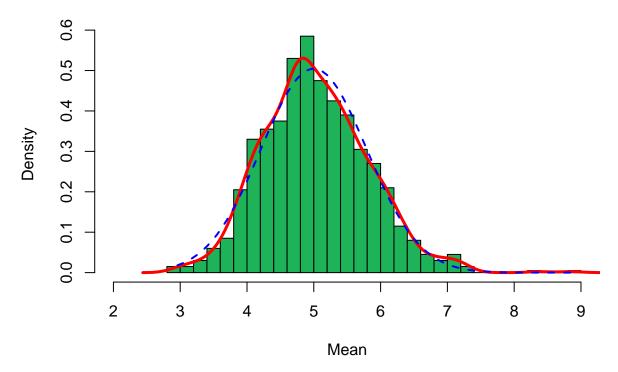
# Theoretical Variance is Theoretical mean squared divided by the exponentials
theo_variance <- (1/lambda)^2/exponentials
theo_variance</pre>
```

## [1] 0.625

## Plotting the Distributions

While plotting the distribution we will plot the histogram and then extrapolate the normal distribution.

# **Exponential Normal Distribution**



From the above calculation and graph we see that the distribution of means of our sample exponential distributions appear to follow a normal distribution, due to the Central Limit Theorem. Increasing the sample size would result in the distribution being even closer to the standard normal distribution. The dotted line above is a normal distribution curve and we can see that it is very close to our sampled curve, which is the red line above.