```
def is_variable(term):
    """Check if a term is a variable."""
    return isinstance(term, str) and term.islower()
def apply_substitution(term, subst):
    """Apply a substitution to a term."""
    if is variable(term) and term in subst:
       return apply substitution(subst[term], subst)
   if isinstance(term, tuple): # If term is a function, apply substitution to
        return (term[0], [apply substitution(arg, subst) for arg in term[1]])
    return term # Return the term as-is for constants or unbound variables
def unify(term1, term2, subst=None):
    """Unify two terms."""
    if subst is None:
        subst = {}
    if term1 == term2:
       return subst
    if is variable(term1):
        return unify variable(term1, term2, subst)
    if is variable(term2):
        return unify variable(term2, term1, subst)
    if isinstance(term1, tuple) and isinstance(term2, tuple):
        if term1[0] != term2[0] or len(term1[1]) != len(term2[1]):
            return None
        for arg1, arg2 in zip(term1[1], term2[1]):
            subst = unify(arg1, arg2, subst)
            if subst is None:
                return None
        return subst
    return None
def unify variable(var, term, subst):
    """Unify a variable with a term."""
    if var in subst:
        return unify(subst[var], term, subst)
    if occurs check(var, term, subst):
        return None
    subst[var] = term
    return subst
def occurs_check(var, term, subst):
    """Check if a variable occurs in a term."""
    if var == term:
        return True
    if isinstance(term, tuple):
        return any(occurs_check(var, arg, subst) for arg in term[1])
```

```
if var in subst and occurs check(var, subst[var], subst):
        return True
    return False
def fact in kb(fact, kb):
    Check if a fact is already in the knowledge base.
   Args:
        fact: The fact to check.
       kb: The list of known facts.
    Returns:
        True if the fact is in the knowledge base, otherwise False.
    .....
   for known fact in kb:
        if unify(fact, known_fact) is not None:
            return True
    return False
def forward reasoning(kb, query):
    Perform forward reasoning on the knowledge base (KB) to prove the query.
        kb: The knowledge base, a list of first-order logic rules or facts.
        query: The goal to prove.
    Returns:
        True if the query can be proved, otherwise False.
   known facts = [] # Store known facts as a list
   new facts = True
   while new_facts:
        new facts = False
        for rule in kb:
            if isinstance(rule, tuple) and rule[0] == "implies": # Implication
                conditions, conclusion = rule[1], rule[2]
                substitutions = [{}]
                for condition in conditions:
                    next substitutions = []
                    for fact in known facts:
                        subst = unify(condition, fact)
                        if subst is not None:
                            next substitutions.append(subst)
                    substitutions = [
                        {**s1, **s2} for s1 in substitutions for s2 in next sub:
```

for subst in substitutions:

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derived fact = apply substitution(conclusion, subst)
                    if not fact in kb(derived fact, known facts):
                        known facts.append(derived fact)
                        new facts = True
            else: # It's a fact
                if not fact_in_kb(rule, known_facts):
                    known facts.append(rule)
                    new facts = True
        # Check if the query is in the known facts
        for fact in known facts:
            if unify(fact, query) is not None:
                return True
   return False
# Example Usage
if __name__ == "__main__":
   # Knowledge Base
   kb = \Gamma
        ("implies", [("human", ["x"])], ("mortal", ["x"])), # human(x) -> mortal
        ("human", ["socrates"]), # human(socrates)
    ]
   # Query
    query = ("mortal", ["socrates"]) # Is Socrates mortal?
   # Perform forward reasoning
    result = forward reasoning(kb, query)
   if result:
        print(f"The query {query} is true based on the knowledge base.")
    else:
        print(f"The query {query} cannot be proved from the knowledge base.")
The query ('mortal', ['socrates']) is true based on the knowledge base.
```