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import math

def alpha_beta_pruning(node, depth, alpha, beta, maximizing_player, evaluate, get_children):
    """
    Perform Alpha-Beta Pruning to find the optimal value of a game tree.

    Args:
        node: The current node (state) of the game tree.
        depth: The maximum depth to explore.
        alpha: The alpha value (initially -infinity).
        beta: The beta value (initially +infinity).
        maximizing_player: Boolean indicating if the current player is maximizing.
        evaluate: Function to evaluate the value of a terminal state.
        get_children: Function to generate child nodes from a given node.

    Returns:
        The optimal value for the current node.
    """
    # Base case: terminal node or maximum depth reached
    if depth == 0 or not get_children(node):
        return evaluate(node)

    if maximizing_player:
        max_eval = -math.inf
        for child in get_children(node):
            eval = alpha_beta_pruning(child, depth - 1, alpha, beta, False, evaluate, get_children)
            max_eval = max(max_eval, eval)
            alpha = max(alpha, eval)
            if beta <= alpha:
                break # Beta cut-off
        return max_eval
    else:
        min_eval = math.inf
        for child in get_children(node):
            eval = alpha_beta_pruning(child, depth - 1, alpha, beta, True, evaluate, get_children)
            min_eval = min(min_eval, eval)
            beta = min(beta, eval)
            if beta <= alpha:
                break # Alpha cut-off
        return min_eval

# Example usage
if __name__ == "__main__":
    # Example game tree structure
    game_tree = {
        "A": ["B", "C", "D"],
        "B": ["E", "F"],
    }

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    "C": ["G", "H"],
    "D": ["I", "J"],
    "E": [], # Leaf node
    "F": [], # Leaf node
    "G": [], # Leaf node
    "H": [], # Leaf node
    "I": [], # Leaf node
    "J": []  # Leaf node
}

# Leaf node values (evaluation function outputs)
leaf_values = {
    "E": 3,
    "F": 5,
    "G": 6,
    "H": 9,
    "I": 1,
    "J": 2
}

# Define evaluation and child generation functions
def evaluate(node):
    return leaf_values.get(node, 0) # Return leaf value, or 0 for non-leaf

def get_children(node):
    return game_tree.get(node, [])

# Perform Alpha-Beta Pruning
result = alpha_beta_pruning("A", depth=3, alpha=-math.inf, beta=math.inf,
                             maximizing_player=True, evaluate=evaluate, get_

print(f"The optimal value for the root is: {result}")

```

 The optimal value for the root is: 6

