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def is_variable(term):
    """Check if a term is a variable."""
    return isinstance(term, str) and term.islower()

def is_constant(term):
    """Check if a term is a constant."""
    return isinstance(term, str) and term.isupper()

def unify(term1, term2, subst=None):
    """
    Unify two terms.
    Args:
        term1: The first term (variable, constant, or function).
        term2: The second term (variable, constant, or function).
        subst: Current set of substitutions (dictionary).
    Returns:
        A substitution dictionary if unification is successful, otherwise None.
    """
    if subst is None:
        subst = {}

    if term1 == term2: # If terms are identical
        return subst

    if is_variable(term1): # If term1 is a variable
        return unify_variable(term1, term2, subst)

    if is_variable(term2): # If term2 is a variable
        return unify_variable(term2, term1, subst)

    if isinstance(term1, tuple) and isinstance(term2, tuple):
        # If terms are functions, unify their name and arguments
        if term1[0] != term2[0] or len(term1[1]) != len(term2[1]):
            return None # Function names or argument lengths differ
        for arg1, arg2 in zip(term1[1], term2[1]):
            subst = unify(arg1, arg2, subst)
            if subst is None:
                return None
        return subst

    return None # Terms cannot be unified

def unify_variable(var, term, subst):
    """
    Unify a variable with a term.
    Args:

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var: The variable (string).
term: The term to unify with (variable, constant, or function).
subst: Current set of substitutions (dictionary).

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Returns:

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Updated substitution dictionary or None.
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"""
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if var in subst: # Variable already substituted
    return unify(subst[var], term, subst)

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if occurs_check(var, term, subst): # Prevent infinite loops
    return None

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subst[var] = term
return subst

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def occurs_check(var, term, subst):
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"""
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Check if a variable occurs in a term (to prevent infinite loops).

Args:

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var: The variable (string).
term: The term to check against.
subst: Current set of substitutions (dictionary).

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Returns:

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True if var occurs in term, False otherwise.
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if var == term:
    return True
if isinstance(term, tuple): # If term is a function, check its arguments
    return any(occurs_check(var, arg, subst) for arg in term[1])
if var in subst and occurs_check(var, subst[var], subst):
    return True
return False

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def apply_substitution(term, subst):
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"""
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Apply a substitution to a term.

Args:

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term: The term to substitute (variable, constant, or function).
subst: The substitution dictionary.

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Returns:

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The term after applying the substitution.
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"""
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if is_variable(term) and term in subst:
    return apply_substitution(subst[term], subst)
if isinstance(term, tuple): # If the term is a function, apply substitution
    return (term[0], [apply_substitution(arg, subst) for arg in term[1]])
return term # Return the term as-is for constants or unbound variables

```

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# Example Usage
if __name__ == "__main__":
    # Example terms:
    term1 = ("f", ["x", "y"]) # f(x, y)
    term2 = ("f", ["a", "b"]) # f(a, b)

    # Perform unification
    result = unify(term1, term2)
    if result:
        print("Unification successful! Substitution:")
        print(result)

        # Apply substitution to the original terms
        term1_substituted = apply_substitution(term1, result)
        term2_substituted = apply_substitution(term2, result)

        print("\nTerms after substitution:")
        print(f"Term 1: {term1_substituted}")
        print(f"Term 2: {term2_substituted}")
    else:
        print("Unification failed.")
```

⇒ Unification successful! Substitution:
{'x': 'a', 'y': 'b'}

Terms after substitution:
Term 1: ('f', ['a', 'b'])
Term 2: ('f', ['a', 'b'])

