

Row-Diagonal Parity for Double Disk Failure Correction



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Background and Motivation



- Data is important
- Disks fail
 - Types of disk failures
 - ✦ Media
 - ✦ Full Disk
 - RAID
 - ✦ Parity
 - ✦ Example
 - Double failures?
 - ✦ Mirrored disks

Single Disk Failure Example



D	D	D	D	P
3	1	2	3	9

Algorithm



- **Goal**
 - Any 2 disks failing should still allow all data to be reconstructed
- **Hardware Setup**
 - 2 Parity Disks
 - Data disks
- **Strategy**
 - Row and diagonal parity for every block of data
 - Stagger parity
 - For single failure: Reconstruct disk from row parity

Algorithm



- Strategy (cont.)
 - 2nd failure during reconstruction
 - ✦ Row and diagonal parity are staggered in such a way that some data block will always have only 1 missing disk
 - ✦ Reconstruct whichever block you can using diagonal parity
 - ✦ Then reconstruct block using row parity
 - ✦ Can now reconstruct another block from diagonal parity, repeat
 - Example

Double Disk Failure Example



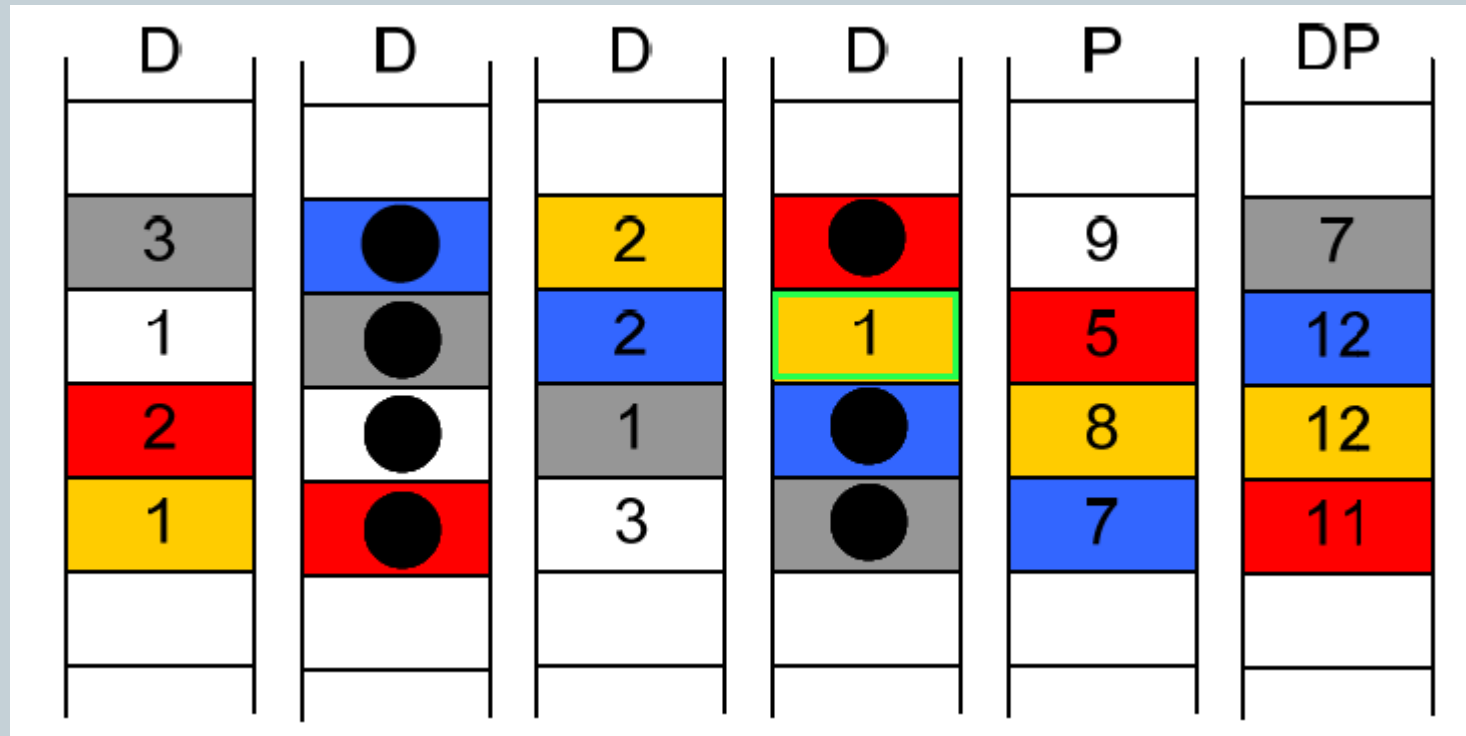
D	D	D	D	P	DP
3	1	2	3	9	7
1	1	2	1	5	12
2	3	1	2	8	12
1	1	3	2	7	11

Double Disk Failure Example



D	D	D	D	P	DP
3	●	2	●	9	7
1	●	2	●	5	12
2	●	1	●	8	12
1	●	3	●	7	11

Double Disk Failure Example



Double Disk Failure Example



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Performance



- Theoretical
 - Read
 - ✦ Data stored in the clear
 - Write
 - ✦ Creating double parity cost = $2(p-1)(p-2)$ xors
 - ✦ Provably optimal when creating double disk failures
 - Reconstruction
 - ✦ Reconstruction from double parity cost = $2(p-1)(p-2)$ xors

Construction Per Row XOR Counts



Data Disks	RDP	EVENODD	Difference
4	6	6.67	11.1%
6	10	10.8	8.0%
8	14	14.86	6.1%
12	22	22.91	4.1%
16	30	30.93	3.1%

Reconstruction Per Row XOR Counts

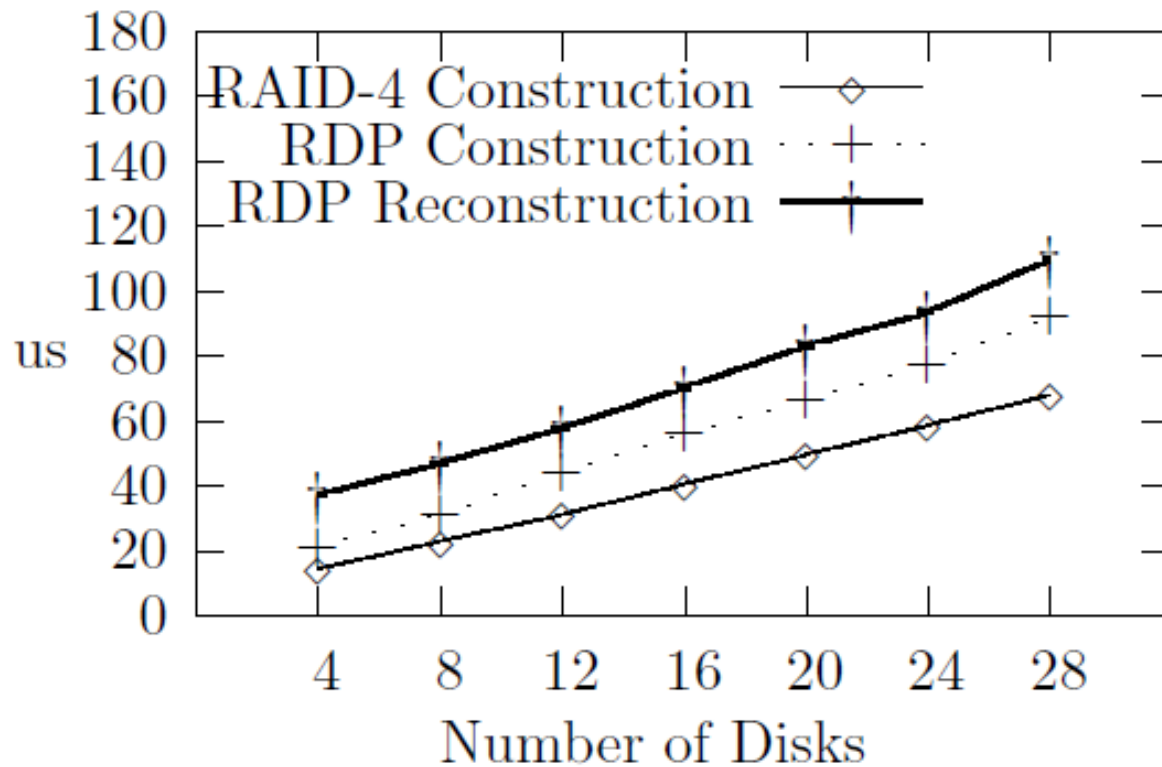


Data Disks	RDP	EVENODD	Difference
4	6	9.67	61.2%
6	10	13.80	38.0%
8	14	17.86	27.6%
12	22	25.91	17.8%
16	30	33.93	13.1%

Performance



- Implemented



Questions?



- **References:**

- **RAID-DP: NETWORK APPLIANCE
IMPLEMENTATION OF RAID DOUBLE PARITY FOR
DATA PROTECTION A HIGH-SPEED
IMPLEMENTATION OF RAID 6; Chris Lueth,
Network Appliance, Inc. [12/2006]**