

Ponce
Family nameMartin
Given name10371381
Student number

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ENS1161 Computer Fundamentals**Test 5**

10/10.

- (a) Consider sets $A = \{a, b, c, d\}$, $B = \{e, f, g\}$ and $C = \{m, p, q\}$, and relations R between A and B , and S between B and C , defined by:

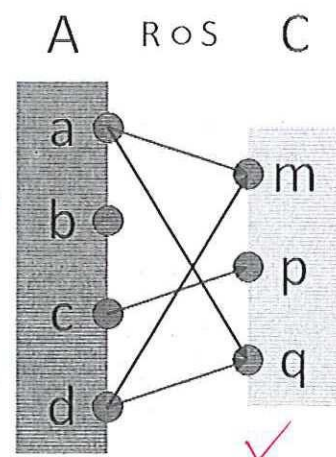
$$R = \{(a, f), (b, e), (c, e), (c, g), (d, f)\} \text{ and } S = \{(f, m), (f, q), (g, p)\}$$

- (i) Find matrices $M(R)$ and $M(S)$ that represent R and S ,

$$M(R) = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad M(S) = \begin{pmatrix} 0 & 0 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

- (ii) Find the matrix $M(R \circ S)$ that represents the composition $R \circ S$, and represent the relation $R \circ S$ with an arrow diagram.

$$M(R \circ S) = \begin{pmatrix} 1 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix}$$



- (b) In each of the following, there is a set and a relation defined on that set. For each indicate with "Y" or "N" whether the relation is reflexive, symmetric or transitive, and hence whether it is an equivalence relation.

| | Set | Relation | Reflex? | Symm? | Trans? | Equiv? |
|---|----------|-----------------------------|---------|-------|--------|--------|
| 1 | people | lives no more than 1km from | Y | Y | N | N |
| 2 | people | likes to play chess with | N | N | N | N |
| 3 | students | attends the same class as | Y | Y | Y | Y |

- (c) A relation P between sets {k, l} and {r, s, t} is represented by the matrix

$$M(P) = \begin{pmatrix} 1 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

. Represent the inverse relation P^{-1} as a set of ordered pairs.

$$P^{-1} = \{(r, k), (r, l), (t, k)\}$$

[5 + 3 + 2 = 10 marks]