

<b>UNIT</b> CODE: <b>ENS1161</b> TITLE: <b>COMPUTER FUNDAMENTALS</b>	<b>NAME OF STUDENT (PRINT CLEARLY)</b> <div> <b>PONCE</b>  <small>FAMILY NAME</small> </div> <div> <b>MARTIN</b>  <small>FIRST NAME</small> </div>	<b>STUDENT ID. NO.</b> <b>10371381</b>
<b>NAME OF TUTOR (PRINT CLEARLY)</b> <b>WLODZIMIERZ GORNISIEWICZ</b>		<b>DUE DATE</b> <b>5-SEPT-14</b>
<b>Topic of assignment</b> <b>ASSIGNMENT 1</b>		
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Edith Cowan University  
ENS1161  
Assignment 1

Martin Ponce  
ID: 10371381

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# 1 Question 1

## 1.1 A) Consider the following argument:

If bears are brown then giraffes are not green. If bears are not brown then rabbits are red. Rabbits are red. Therefore giraffes are not green.

- $b$  = bears are brown
- $g$  = giraffes are green
- $r$  = rabbits are red

### 1.1.1 State the argument in symbols:

$$b \rightarrow \sim g, \sim b \rightarrow r, r \mid \sim g$$

### 1.1.2 Rewrite the symbolic argument as a proposition:

$$(\sim b \wedge r) \rightarrow \sim g$$

### 1.1.3 Construct a truth table for the proposition:

Table 1: Question 1A Truth Table

$b$	$r$	$g$	$\sim b \wedge r$	$\sim g$	$(\sim b \wedge r) \rightarrow \sim g$
0	0	0	0	1	1
0	0	1	0	0	1
0	1	0	1	1	1
0	1	1	1	0	0
1	0	0	0	1	1
1	0	1	0	0	1
1	1	0	0	1	1
1	1	1	0	0	1

### 1.1.4 State whether the argument is valid:

The proposition is logically equivalent to the argument, as shown in the truth table. Therefore the argument is valid.

**1.2 B) The propositions below can be arranged in three groups so that each member of a group is logically equivalent to the other two. Find three groups:**

1. Either the light is not on or the system is ready.

•  $\sim l \vee s$

2. If the system is ready then the light is on.

•  $s \rightarrow l$

3. If the light is on then the system is not ready.

•  $l \rightarrow \sim s$

4. If the light is not on then the system is not ready.

•  $\sim l \rightarrow \sim s$

5. If the system is not ready then the light is not on.

•  $\sim s \rightarrow \sim l$

6. Either the system is not ready or the light is on.

•  $\sim s \vee l$

7. If the light is on then the system is ready.

•  $l \rightarrow s$

8. If the system is ready then the light is not on.

•  $s \rightarrow \sim l$

9. Either the system is not ready or the light is not on.

•  $\sim s \vee \sim l$

Table 2: Question 1B Truth Table

$s$	$l$	$\sim s$	$\sim l$	$\sim l \vee s$	$s \rightarrow l$	$l \rightarrow \sim s$	$\sim l \rightarrow \sim s$	$\sim s \rightarrow \sim l$	$\sim s \vee l$	$\rightarrow s$	$s \rightarrow \sim l$	$\sim s \vee \sim l$
0	0	1	1	1	1	1	1	1	1	1	1	1
0	1	1	0	0	1	1	1	0	1	0	1	1
1	0	0	1	1	0	1	0	1	0	1	1	1
1	1	0	0	1	1	0	1	1	1	1	0	0

**1.2.1 Question 1B Answer:**

Table 3: Group 1

Proposition number	Symbolic
1	$\sim l \vee s$
5	$\sim s \rightarrow \sim l$
7	$l \rightarrow s$

Table 4: Group 2

Proposition number	Symbolic
2	$s \rightarrow l$
4	$\sim l \rightarrow \sim s$
6	$\sim s \vee l$

Table 5: Group 3

Proposition number	Symbolic
3	$l \rightarrow \sim s$
8	$s \rightarrow \sim l$
9	$\sim s \vee \sim l$

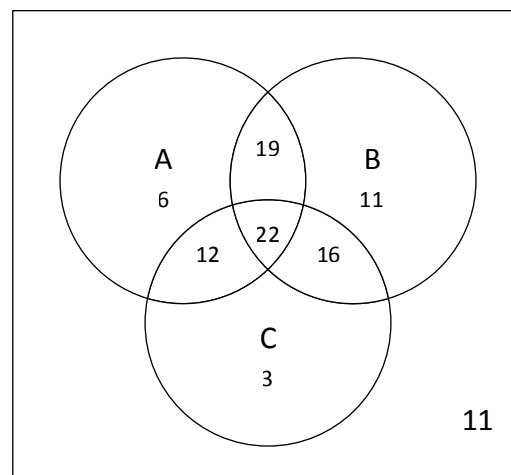
## 2 Question 2

A group of 100 students is polled to see how many watched three TV shows, Action, Buzz, and Calypso. The results showed that:

- 59 watched Action, denoted by  $A$
- 68 watched Buzz, denoted by  $B$
- 52 watched Calypso, denoted by  $C$
- 41 watched Action and Buzz
- 34 watched Action and Calypso
- 38 watched Buzz and Calypso
- 11 did not watch any of the the three shows

### 2.1 A) Calculate the number of students in each of the eight subsets. Enter the number of students in each subset:

Figure 1: Question 2A Venn diagram



### 2.2 B) Hence find how many students watched:

1. Action and Calypso, but not Buzz
  - 12
2. Buzz only
  - 11
3. Only two of the three shows
  - 47
4. At least two of the shows
  - 69



### 3 Question 3

Suppose that  $P$  is a set of people, and  $M$  is a set of movies. Define the predicate  $S(p, m)$  to mean “person  $p$  has seen movie  $m$ ”. Consider the sentences below. For each sentence, the negation is also in the list. Match each sentence with its negation. Give your answer by listing the number of each sentence and its negation, for example “4 and 10”.

1. There is at least one movie that some person has seen
  - $\exists m \in M, \exists p \in P, S(p, m)$
2. For each movie there is somebody who has not seen it
  - $\forall m \in M, \exists p \in P, \sim S(p, m)$
3. There is some movie that nobody has seen
  - $\exists m \in M, \forall p \in P, \sim S(p, m)$
4. There is at least one movie that everybody has seen
  - $\exists m \in M, \forall p \in P, S(p, m)$
5. For each movie there is somebody who has seen it
  - $\forall m \in M, \exists p \in P, S(p, m)$
6. There is some person who has not seen any of the movies
  - $\exists p \in P, \forall m \in M, \sim S(p, m)$
7. There is at least one movie that some person has not seen
  - $\exists m \in M, \exists p \in P, \sim S(p, m)$
8. Nobody has seen any of the movies
  - $\forall m \in M, \forall p \in P, \sim S(p, m)$
9. For each person there is some movie that they have not seen
  - $\exists p \in P, \exists m \in M, \sim S(p, m)$
10. Everybody has seen at least one movie
  - $\forall p \in P, \exists m \in M, S(p, m)$
11. There is some person who has seen all the movies
  - $\exists p \in P, \forall m \in M, S(p, m)$
12. Everybody has seen all of the movies
  - $\forall m \in M, \forall p \in P, S(p, m)$

### 3.1 Question 3 Answer

1. 1 and 8
2. 2 and 4
3. 3 and 5
4. 6 and 10
5. 7 and 12
6. 9 and 11

## 4 Question 4

### 4.1 Introduction

There is a simple way of representing sets using so-called *bit strings*. A bit string is simply a string of 0's and 1's. Suppose that  $U$  is the universal set. Then the rule for the bit string for a particular set  $S$  is:

If the  $k$ th element of  $U$  is in  $S$ , then the  $k$ th bit of the bit string is 1.

If the  $k$ th element of  $U$  is not in  $S$ , then the  $k$ th bit of the bit string is 0.

### 4.2 Example 1:

- Suppose the universal set is  $U = \{1, 2, 3, 4, \dots, 10\}$
- Then set  $A = \{1, 3, 5, 9\}$  is represented by the bit string 1010100010
  - The 1st element of  $U$  appears in set  $A$ , so the 1st element of the bit string is 1
  - The 2nd element of  $U$  does not appear in set  $A$ , so the 2nd element of the bit string is 0
- The set  $\{5, 6, 7\}$  is represented by bit string 0000111000
- Conversely, the bit string 0110010001 represents the set  $C = \{2, 3, 6, 10\}$ 
  - The 1st element of the bit string is 0, so the 1st element of  $U$  (which is  $\{1\}$ ) is not in  $C$
  - The 2nd element of the bit string is 1, so the 2nd element of  $U$  (which is  $\{2\}$ ) is in  $C$
- Similarly, the bit string 0000000110 represents  $\{8, 9\}$
- And the bit string 0101010101 represents  $\{2, 4, 6, 8, 10\}$

### 4.3 Example 2:

- The universal set is  $U = \{4, 6, 9, 13, 18, 25\}$
- Set  $A = \{6, 13, 18\}$
- Set  $B = \{4, 13, 18, 25\}$

Suppose we want to find  $A \cup B$ ,  $A \cap B$  and  $A'$ . Using a table and performing the operations **bitwise**.

Table 6: Question 4 Example 2 Truth Table

$U$	4	6	9	13	18	25
$A$	0	1	0	1	1	0
$B$	1	0	0	1	1	1
$A \cup B$	1	1	0	1	1	1
$A \cap B$	0	0	0	1	1	0
$A'$	1	0	1	0	0	1

From the table we get:

- $A \cup B$  bit string is 110111
  - $A \cup B = \{4, 6, 13, 18, 25\}$
- $A \cap B$  bit string is 000110
  - $A \cap B = \{13, 18\}$
- $A'$  bit string is 101001
  - $A' = \{4, 9, 25\}$

### 4.4 Task:

$U = \{Argentina, Australia, Belgium, Brazil, Cameroon, Chile, Cuba, Denmark, Egypt, Ethiopia, Fiji, France, Germany, Ghana, Greece, Haiti\}$

- Find the bit string that represents the set  $L = \{Brazil, Fiji, Ghana, Greece\}$ 
  - Bit string  $L = 0001\ 0000\ 0010\ 0110$
- Find the set  $M$  represented by bit string 0000 0110 1001 0001
  - $M = \{Chile, Cuba, Egypt, France, Haiti\}$
- Let  $P$ ,  $Q$ ,  $R$  and  $S$  be sets represented by the following bit strings respectively (see Table 7)
  - Find the bit string that represent the set  $T = (P \cap Q') \cup (R' \cap S)$ 
    - Bit string  $T = 1000\ 0010\ 1010\ 0100$
- List the countries in the set  $T$ 
  - $T = \{Argentina, Cuba, Egypt, Fiji, Ghana\}$

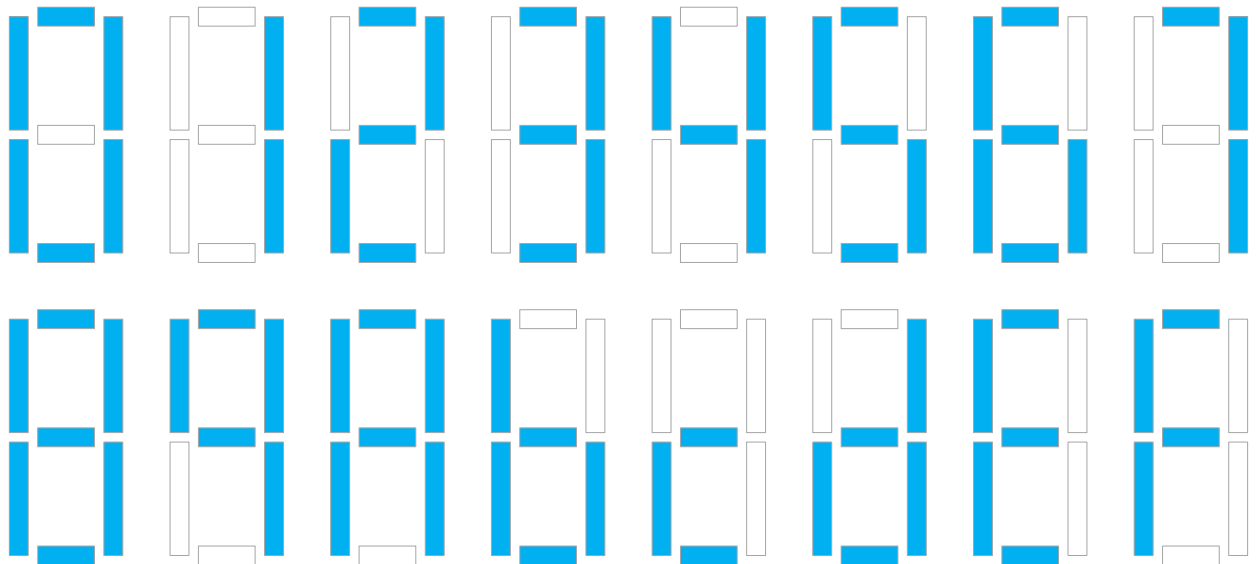
Table 7: Question 4 Task Truth Table

$U$	Ar	Au	Be	Br	Ca	Ch	Cu	De	Eg	Et	Fi	Fr	Ge	Gh	Gr	Ha
$L$	0	0	0	1	0	0	0	0	0	0	1	0	0	1	1	0
$M$	0	0	0	0	0	1	1	0	1	0	0	1	0	0	0	1
$P$	1	1	0	1	0	1	0	0	1	0	1	0	1	1	1	0
$Q$	0	1	1	1	1	1	0	0	0	1	0	0	1	0	1	1
$R$	0	1	0	1	1	1	0	1	1	0	0	1	1	0	0	1
$S$	1	1	0	1	0	0	1	1	0	1	1	0	1	0	0	1
$Q'$	1	0	0	0	0	0	1	1	1	0	1	1	0	1	0	0
$P \cap Q'$	1	0	0	0	0	0	0	0	1	0	1	0	0	1	0	0
$R'$	1	0	1	0	0	0	1	0	0	1	1	0	0	1	1	0
$R' \cap S$	1	0	0	0	0	0	1	0	0	1	1	0	0	0	0	0
$T$	1	0	0	0	0	0	1	0	1	0	1	0	0	1	0	0

## 5 Question 5

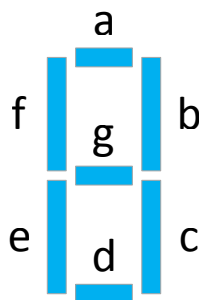
In lecture notes there is an application of Karnaugh maps to a 7-segment display that is used in some calculators and similar digital devices. The display is sometimes *extended* to include *all* hexadecimal digits. A typical extended display is:

Figure 2: 7-Segment Characters



Notice the display for the hexadecimal digits for 10 through 15. Some are shown as upper case and some lower case: A, b, c, d, E, F. As in the lecture notes we label each of the seven segments as shown:

Figure 3: 7-Segment Segments



When any of the keys, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F is pressed, a 4-bit binary signal  $wxyz$  is generated, as shown in Table 8.

For each of the seven segments, there is a corresponding Boolean function and a circuit that has output 0 or 1 as the various keys are pressed. Denote these functions by  $a(w, x, y, z)$ ,  $b(w, x, y, z)$ , ...,  $g(w, x, y, z)$ .

## 5.1 Task:

Your task concerns the two segments  $d$  and  $g$ , and is as follows. For **each** of the two functions  $d(w, x, y, z)$  and  $g(w, x, y, z)$ :

### 5.1.1 Construct a truth table for functions $d(w, x, y, z)$ and $g(w, x, y, z)$ :

Table 8: Question 5 Task Truth Table

Key	w	x	y	z	a	b	c	d	e	f	g
0	0	0	0	0	1	1	1	1	1	1	0
1	0	0	0	1	0	1	1	0	0	0	0
2	0	0	1	0	1	1	0	1	1	0	1
3	0	0	1	1	1	1	1	1	0	0	1
4	0	1	0	0	0	1	1	0	0	1	1
5	0	1	0	1	1	0	1	1	0	1	1
6	0	1	1	0	1	0	1	1	1	1	1
7	0	1	1	1	1	1	1	0	0	0	0
8	1	0	0	0	1	1	1	1	1	1	1
9	1	0	0	1	1	1	1	0	0	1	1
A	1	0	1	0	1	1	1	0	1	1	1
B	1	0	1	1	0	0	1	1	1	1	1
C	1	1	0	0	0	0	0	1	1	0	1
D	1	1	0	1	0	1	1	1	1	0	1
E	1	1	1	0	1	0	0	1	1	1	1
F	1	1	1	1	1	0	0	0	1	1	1

### 5.1.2 Construct the corresponding Karnaugh map:

Use the *simple* labelling on the Karnaugh maps and show your groups clearly.

Figure 4:  $d(w, x, y, z)$  Karnaugh map

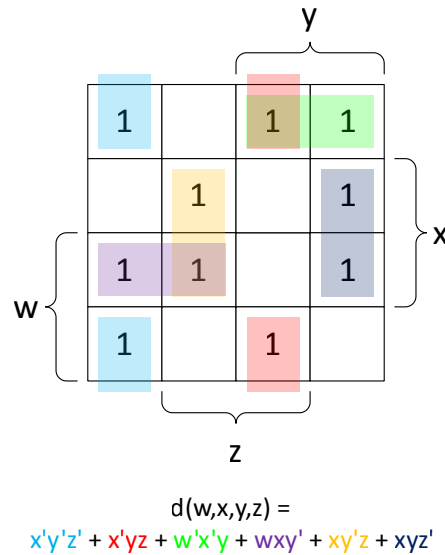
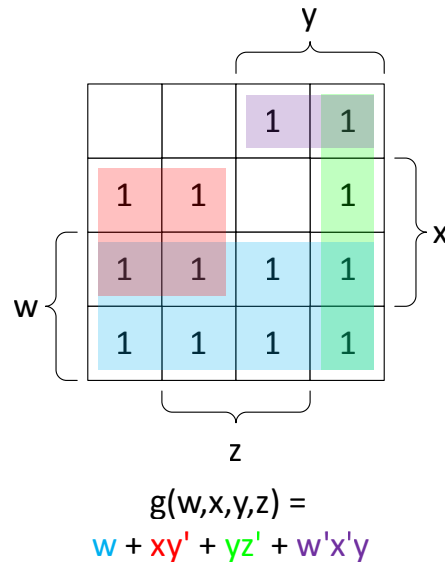


Figure 5:  $g(w, x, y, z)$  Karnaugh map



### 5.1.3 Find the minimal sum of products for the functions

$$d(w, x, y, z) = x'y'z' + x'y'z + w'x'y + wxy' + xy'z + xyz'$$

$$g(w, x, y, z) = w + xy' + yz' + w'x'y$$