

TOPIC

MACHINE LEARNING (ML)

ALGORITHM

* Q. Explain me about the Linear Regression and Multiple Linear Regression with suitable Examples.

Answer

1. Simple Linear Regression:

A Linear Regression is a statistical method that models the relationship between two variables by fitting a

Linear equation to observed data.

It is used to predict the value of a dependent variable (target) based on the value of an independent variable (predictor).

* Formula :-

$$y = \beta_0 + \beta_1 x + \epsilon$$

where,

- * 'y' is the dependent variable (what we are trying to predict).
- * 'x' is the independent variable (the predictor).
- * ' β_0 ' is the y-intercept (the value of y when $x = 0$).
- * ' β_1 ' is the slope of the line (the change in y for a one-unit change in x).
- * ' ϵ ' is the error term (the difference between the observed and predicted values of y).

* Example of simple Linear Regression:

* Scenario:

predicting the height of a person based on their age.

* data:

* Age (years) : [5, 7, 10, 12, 15]

* Height (m) : [110, 120, 130, 140, 150]

* steps:

① plot the data:

plot age on the x -axis and height on the y -axis.

② Fit a Line:

draw a line that best fits to the data points.

③ Determine the Equation:

use statistical methods to determine the value of β_0 and β_1 .

* Resulting Equation:

$$\text{Height} = 100 + 3 \times \text{Age}$$

This equation suggests that the height increases by ~~30~~ 3 cm for each additional year of age, with a base height of 100 cm at age 0.

* 2. Multiple Linear Regression:

Multiple Linear Regression models the relationship between two or more independent variables and a dependent variable by fitting a linear equation to observed data.

* Formula :

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + \epsilon$$

where,

* 'y' is the dependent variable.

* x_1, x_2, \dots, x_n are the independent variables.

* β_0 is the y-intercept

* $\beta_1, \beta_2, \dots, \beta_n$ are the coefficients for the independent variables.

* ' ϵ ' is the error term.

* Example of Multiple Linear Regression:

* Scenario:

predicting a house's price based on its size, number of bedrooms & age.

* Data:

* (i) Size (sq ft): [1400, 1600, 1700, 1875, 1100]

* (ii) Number of Bedrooms: [3, 3, 2, 4, 2]

* (iii) Age (years): [20, 15, 18, 10, 25]

* (iv) Price (in \$ 1000s): [245, 312, 279, 308, 199]

* Steps :

① prepare the data :

organize the data into a table.

② Fit a model :

Use statistical software to fit a multiple linear regression model.

③ Determine the Equation :

Calculate the coefficients (β).

* Resulting Equation :

$$\text{price} = 50 + 0.1 \times \text{size} + 20 \times \text{Bedrooms} - 0.5 \times \text{Age}$$

* This equation suggests:

- ① The base price is \$50,000
- ② Each additional square foot adds \$20,000 to the price.
- ③ Each additional year of age decreases the price by \$500.

Summary

- * Simple Linear Regression involves one target variable. It fits a straight line to the data.
- * Multiple Linear Regression involves multiple predictors and one target variable. It fits a plane (or hyperplane) to the data.

Both methods are used to understand relationships between variables and make predictions.