**Topics: Confidence Intervals**

1. For each of the following statements, indicate whether it is True/False. If false, explain why.
2. The sample size of the survey should at least be a fixed percentage of the population size in order to produce representative results.

* False

1. The sampling frame is a list of every item that appears in a survey sample, including those that did not respond to questions.

* False

1. Larger surveys convey a more accurate impression of the population than smaller surveys.

* True

1. *PC Magazine* asked all of its readers to participate in a survey of their satisfaction with different brands of electronics. In the 2004 survey, which was included in an issue of the magazine that year, more than 9000 readers rated the products on a scale from 1 to 10. The magazine reported that the average rating assigned by 225 readers to a Kodak compact digital camera was 7.5. For this product, identify the following:
2. The population

* Readers of the magazine = 9000

1. The parameter of interest

* Rating of camera (7.5)

1. The sampling frame

* Sampling frame is the 9000 readers

1. The sample size

* The sample size is 225 readers

1. The sampling design

* Voluntary response

1. Any potential sources of bias or other problems with the survey or sample

* No, because of the limited information and voluntary response of the sample design

1. For each of the following statements, indicate whether it is True/False. If false, explain why.
2. If the 95% confidence interval for the average purchase of customers at a department store is $50 to $110, then $100 is a plausible value for the population mean at this level of confidence.

* True

1. If the 95% confidence interval for the number of moviegoers who purchase concessions is 30% to 45%, this means that fewer than half of all moviegoers purchase concessions.

* True

1. The 95% Confidence-Interval for *μ* only applies if the sample data are nearly normally distributed.

* False

confidence intervals can be used with distribution that are not normal

1. What are the chances that ?
2. ¼
3. ½
4. ¾
5. 1

Ans :- B. 1/2

Because there is 50% of chance that the sample mean is greater the population mean in the normal distribution

1. In January 2005, a company that monitors Internet traffic (WebSideStory) reported that its sampling revealed that the Mozilla Firefox browser launched in 2004 had grabbed a 4.6% share of the market.
2. If the sample were based on 2,000 users, could Microsoft conclude that Mozilla has a less than 5% share of the market?

We know that

Null Hypothesis, H0: P ≥ 5%

Alternative Hypothesis, H1: P< 5%

Test statistics = (0.046 – 0.05)/√ [0.05(1-0.05)]/2000

= - 0.833

The critical value of z for 5% significance level = -1.96

Test statistics > Z (-1.96)

(-0.833)

The null hypothesis is true, hence Mozilla has more than or equal to 5% market share.

1. WebSideStory claims that its sample includes all the daily Internet users. If that’s the case, then can Microsoft conclude that Mozilla has a less than 5% share of the market?

In this case, we have data on entire population and the sample value accurately reflects to the population so we can conclude that can Microsoft conclude that Mozilla has a less than 5% share of the market

1. A book publisher monitors the size of shipments of its textbooks to university bookstores. For a sample of texts used at various schools, the 95% confidence interval for the size of the shipment was 250 ± 45 books. Which, if any, of the following interpretations of this interval are correct?
2. All shipments are between 205 and 295 books.

* Incorrect

1. 95% of shipments are between 205 and 295 books.

* Incorrect

1. The procedure that produced this interval generates ranges that hold the population mean for 95% of samples.

* Correct

1. If we get another sample, then we can be 95% sure that the mean of this second sample is between 205 and 295.

* Incorrect

1. We can be 95% confident that the range 160 to 340 holds the population mean.

* Incorrect

1. Which is shorter: a 95% *z*-interval or a 95% *t*-interval for *μ* if we know that σ =s?
2. The z-interval is shorter
3. The t-interval is shorter
4. Both are equal
5. We cannot say

Ans: A. The z-interval is shorter

Questions 8 and 9 are based on the following: To prepare a report on the economy, analysts need to estimate the percentage of businesses that plan to hire additional employees in the next 60 days.

1. How many randomly selected employers (minimum number) must we contact in order to guarantee a margin of error of no more than 4% (at 95% confidence)?
2. 600
3. 400
4. 550
5. 1000

Margin of Error = Z-Score × (S ÷ √n)

The Z – score at 95% confidence interval = 1.96 (stats.norm.ppf(0.975))

(Margin of Error)2 = (Z-Score)2 × (S2 ÷ n)

(Margin of Error)2 = (Z-Score)2 × (P(1-P) ÷ n)

n = [(Z-Score)2 × P(1-P)] / (Margin of Error)2

= 1.96^2 \* 0.5(1-0.5) / (0.04)2

N = 600

Ans :- A. 600

1. Suppose we want the above margin of error to be based on a 98% confidence level. What sample size (minimum) must we now use?
2. 1000
3. 757
4. 848
5. 543

Margin of Error = Z-Score × (S ÷ √n)

The Z-score at 98% confidence interval= 2.33 (stats.norm.ppf(0.99)

(Margin of Error)2 = (Z-Score )2× (S2 ÷ n)

(Margin of Error)2 = (Z-Score )2× (P(1-P) ÷ n)

n = [ (Z-Score )2× P(1-P)] / (Margin of Error)2

= 2.33^2 \* 0.5(1-0.5) / (0.04)2

N = 848

Ans :- C. 848