



# □ MATRICES



# Matrices

Matrices are 2 dimensional array. They have one more attribute then vector called dimension attribute. [Vector has 2 attribute, mode and length] The dimension attribute is itself an integer vector of length 2( nrow, ncol)

```
Matrix( data = NA, nrow=1, ncol=1, byrow=FALSE,  
dimnames = list(c(rowname),c(colname)) )
```

Byrow helps to decide whether rows are filled or columns are filled.

Dimnames allows to give names to the rows and columns.

# Matrices

```
m <- matrix( c(1,2,3,4),nrow=2, ncol=2)
```

```
> m
```

```
      [1] [2]  
[1]  1   3  
[2]  2   4
```

```
> dim (m)
```

```
[1] 2 3 # It shows that m has 2 rows and 3 columns
```

Matrices are constructed column-wise, so entries can be thought of starting in the “upper left” corner and running down the columns.

```
> m <- matrix(1:6, nrow=2, ncol =3)
```

```
> m
```

# Matrices

Matrices can also be created by

```
> m<- 1:10
```

```
> m
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
> dim(m) <- c(2,5)
```

```
>m
```

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	1	3	5	7	9
[2,]	2	4	6	8	10

# Vectorized Matrix Operation

```
X<-matrix(1:4,2,2);y<-matrix(rep(10,4),2,2)
```

```
> x*y ## element-wise multiplication
```

```
      [,1] [,2]  
[1,]  10   20  
[2,]  20   40
```

```
> x/y
```

```
      [,1] [,2]  
[1,]  0.1  0.3  
[2,]  0.2  0.4
```

```
> x %*% y ## true matrix multiplication
```

```
      [,1] [,2]  
[1,]  40   40  
[2,]  60   60
```

# Cbind-ing and rbind-ing

▣ Matrices can be created by column-binding or row-binding with `cbind()` and `rbind()`

▣ `> x <- 1:3`

▣ `> Y <- 10:12`

▣ `cbind(x,y)`

	x	y
▣ [1,]	1	10
▣ [2,]	2	11
▣ [3,]	3	12

▣ `rbind(x,y)`

	[,1]	[,2]	[,3]
▣ x	1	2	3
▣ y	10	11	12

# Matrices name

```
> m <- matrix(c(30,35,40,45) , nrow = 2, ncol = 2)
```

```
> dimnames(m) <- list (c("Sumit","Nikita"), c("R Prog", "C Prog"))
```

```
> m
```

	R Prog	C Prog
Sumit	30	40
Nikita	35	45

# Accessing Matrix

- Matrix can be accessed in the usual way with (i,j) type indices
- `X<-matrix(1:6,2,3)`
- `>x[1,2]`
- `[1] 3`
- `>x[2,1]`
- `[1] 2`
- Indices can be missing
- `>x[1,]`
- `1,3,5`
- `>x[,2]`
- `3,4`



# Accessing Matrix

□ By default when a single element of matrix is retrieved, it is returned as a vector of length 1 rather than a 1\*1 matrix. This behaviour can be turned off by setting drop=FALSE

```
□ >X<-matrix(1:6,2,3)
```

```
□ X[1,2]
```

```
□ [1] 3
```

```
□ >x[1,2,drop=false]
```

```
□      [,1]
```

```
□ [1,] 3
```

```
□ X[1, ]
```

```
□ [1] 1 3 5
```

```
□ X[1, ,drop = FALSE)
```

```
□      [,1] [,2] [,3]
```

```
□ [1,] 1    3    5
```

# Transpose

- Transpose is very important in matrix.
- For this R has function `t()`
- `> m<-matrix(1:4,2,2)`
- `> m`
  - `[1, ] 1 3`
  - `[2, ] 2 4`
- `> t(m)`
  - `[1, ] 1 2`
  - `[2, ] 3 4`

# Mathematical functions on Matrix

- ▣ Diagonal of Matrix – `diag(m)`
- ▣ Eigenvalue & Eigenvectors
- ▣ Eigenvectors are denoted by  $A$  and defined as a vector that when multiplied by given matrix will just increase the magnitude of matrix by scalar value  $\lambda$ . They exist for square matrix.
- ▣  $A.V = \lambda V$
- ▣ `e<-eigen(V)`
- ▣ `e$value`
- ▣ `e$vector`

# Other Matrix operations

- `solve(a,b)`: solve a set of equations. (If `b` is not given then `solve` will return the inverse of `a`)
- `ginv()`: Moore-Penrose generalized inverse of a matrix
- `rowMeans`: vector of row means
- `rowSums`: vector of row sums
- `colMeans`: vector of column means
- `colSums`: vector of column sums



# □ QUESTIONS