# Treebeard: An Optimizing Compiler for Tree Based ML Inference

#### **ABSTRACT**

Decision tree ensembles are commonly used machine learning models generated by machine learning techniques like gradient boosting and random forests. These models are used in a wide range of applications and are deployed at scale (run repeatedly on billions of data items). Several libraries such as XGBoost, LightGBM, and Sklearn expose algorithms for both training and inference with decision tree ensembles. While these libraries incorporate a limited set of hardware-specific optimizations, they do not specialize the inference code to the model being used, leaving significant performance on the table.

This paper presents a compiler-based approach that automatically generates efficient code for decision tree inference. It develops Treebeard, an extensible compiler, which progressively lowers inference code to LLVM IR through multiple intermediate abstractions. By applying model-specific optimizations at the higher levels, loop optimizations at the middle level, and machine-specific optimizations lower down, Treebeard can specialize inference code for each model on each supported hardware target. To improve model inference performance, Treebeard performs several novel optimizations such as tree tiling, tree walk unrolling, and tree walk interleaving.

We implement Treebeard using the MLIR compiler infrastructure and demonstrate the utility of Treebeard by evaluating it on a diverse set of tree ensemble models. Experimental evaluation demonstrates that Treebeard optimizations improve average latency over a batch of inputs by 2.2X over our baseline version. Further, Treebeard is significantly faster than XGBoost and Treelite in both single-core (2.8X and 5.1X respectively) and multi-core (3.2X and 2.6X respectively) settings.

#### 1. INTRODUCTION

Intro tex here!

#### 2. COMPILER OVERVIEW

Figure 1 shows the high level structure of Treebeard. The input to Treebeard is a JSON serialized decision forest model, it supports popular frameworks like XGBoost and LightGBM and is extensible to other frameworks. Given an input model our compiler generates optimized inference code. Specifically it generates a callable batch inference function predictFor-

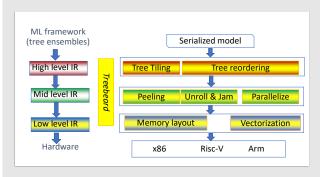


Figure 1: Treebeard Compiler Structure

est that given an array of inputs, outputs an array of model predictions.

Treebeard specializes the code generated for inference by progressively optimizing and lowering a high level representation of the predictForest function down to LLVM IR [1]. At the highest level (HIR) it tiles nodes together to transform a binary tree into an *n*-ary tree and applies transformations that determine how inputs traverse the decision forest. It then lowers to a mid-level IR (MIR) where loop optimizations like loop-reordering and unrolling are applied. The compiler also figures out which loop nest to parallelize. At the lowest level of IR Treebeard applies layout optimizations and generates vectorized code to take advantage of SIMD instructions where applicable. LLVM is then used to JIT compile the generated IR to executable code. The following sections describe each level of the IR and their lowering in more detail.

TODO Kr: consider focusing on the example instead of verbose description of optimizations. This section can be short, descriptions can come in later sections.

## 2.1 High Level IR

As a first step Treebeard parses the input and generates a single MLIR operation, predictForest that represents inference using the input model on a set of rows. At this level the operator simply contains a collection of binary trees. Two optimizations, tiling and tree ordering are applied at this level. The objective of tiling is to group nodes together so that the tree can be walked one tile at a time instead of one node at a time. We demonstrate that tiling can specialize the traversal of individual trees to either balance heavily skewed trees or proritize walks leading to higher probability leafs. Figure ?? shows examples of the tiling transformation. TODO kr: draw

and explain example. The objective of tree padding and ordering is to group identically structured trees so that they can share the same traversal code. The predictForest function is now lowered to MIR with separate loop nests generated for traversing a group of identical trees. The generated MIR code is as shown below. TODO show unoptimized loop nest as a listing.

```
func Predict(float rows[batchSize]) {
   predictions = predictForest(rows)
   return rows
4 }
```

#### 2.2 Mid Level IR

The Mid Level IR optimizes the loop structures and tree walks. Firstly, the order in which the iteration space of trees and inputs is walked is determined and by re-ordering the loop nesting if necessary. Also, operations such as <code>isLeaf</code>, <code>traverseTile</code>, <code>getLeafValue</code> are introduced so that the traversal of trees explicitly represented. The following listing shows the IR for inference using a model with four trees on an input batch with two rows. The listed IR walks all trees for one input row before moving to the next row. One important point to note here is that details such as the data structure used for the trees are not explicitly encoded in the IR. This allows us to reuse optimization and lowering passes on this level of the IR regardless of what the final in memory representation of the model is.

```
// Constant that represents the model being compiled
forest = ensemble (...)
for i = 0 to 2 step 1 {
  prediction = 0
  for t = 0 to 4 step 1 {
    tree = getTree(forest, t)
    node = getRoot(tree)
    while (isLeaf(tree, n)==false) do {
      node = traverseTreeTile(tree, node, rows[i])
    }
  treePrediction = getLeafValue(tree, node)
  prediction = prediction + treePrediction
}
predictions[i] = prediction
}
```

The IR listed above is a simplification of the actual IR. The actual IR is strongly typed and in SSA form.

## 2.3 Low Level IR

The IR is finally lowered to a form where the in memory representation of the model is made explicit. Buffers to hold the model values are inserted into the generated code and all tree operations in the mid-level IR are lowered to explicitly reference these buffers. The semantics of all operations are made explicit. For example, traverseTreeTile is lowered into a series of operations to load thresholds, feature indices and features, compare the features with the thresholds and compute the next node to evaluate. This IR is then lowered directly to LLVM IR and JITted.

## 3. OPTIMIZATIONS

TODO This section needs a better name!

## 3.1 Notation

TODO Notation needs to be introduced in the background section We represent a decision tree by T = (V, E, r) where V is the set of nodes, E the set of edges and  $r \in V$  is the root. For each node  $n \in V$ , the following are given.

- 1.  $threshold(n) \in \mathbb{R}$  which gives the threshold value for n.
- 2.  $featureIndex(n) \in \mathbb{N}$  which gives the feature index for n.
- 3.  $left(n) \in V$ , the left child of n or  $\emptyset$  if n is a leaf. If  $left(n) \neq \emptyset$ , then  $(n, left(n)) \in E$ .
- 4.  $right(n) \in V$ , the right child of n or  $\emptyset$  if n is a leaf. If  $right(n) \neq \emptyset$ , then  $(n, right(n)) \in E$ .

We use  $L \subset V$  to denote the set of leaves.

## 3.2 Tiling

Treebeard vectorizes tree walks by grouping nodes of a decision tree into *tiles*. The nodes in a tile are evaluated concurrently using vector instructions. Once the nodes of the current tile are evaluated, a look up table is used to compute which child of the current tile to move to next. The listing below shows at a high level how a tiled tree is walked.

```
// A lookup table that determines the child index of // the next tile given the tile shape and the outcome
     // of the vector comparison on the current tile int16_t LUT[NUM_TILE_SHAPES, pow(2, TileSize)]
     ResultType Prediction_Function (...) {
       Node n = getRoot(tree)
        while (isLeaf(tree, n)==false) do {
  thresholds = loadThresholds(tree, n)
11
          featureIndices = loadFeatureIndices(tree, n)
          // Gather required feature from the current row
13
          features = rows[i][featureIndices]
14
          // Vector comparison of features and thresholds
15
          comparison = features < thresholds
          // Pack bits in comparison vector into an integer
18
          comparisonIndex = combineBitsIntoInt(comparison)
          // Get child index of tile we need to move to
          tileShape = loadTileShape(tree, n)
22
          childIndex = LUT[tileShapeID, comparisonIndex]
23
          // Move to the correct child of the current node
          n = getChildNode(tree, n, childIndex)
        ThresholdType prediction = getLeafValue(n)
28
```

To evaluate the current tile, the vector of thresholds is first loaded (loadThresholds). This vector contains the thresholds of all nodes in the tile. Then, the features required for comparison are gathered into a vector (lines 11 and 13). The feature vector is compared to the threshold vector and the child tile to move to is determined (lines 15 to 25). More details about tile shapes and the look up table are presented in subsequent sections.

## 3.3 Tiles and Tile Shapes

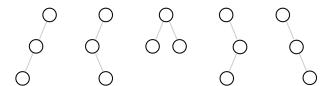


Figure 2: All possible tile shapes with tile size  $n_t = 3$ 

A *tile* is a collection of connected non-leaf nodes of a decision tree. The path connecting any pair of nodes in the tile must fully be contained within the tile. The tile size  $n_t$  is the number of nodes contained in a tile.

Informally, the *tile shape* is the shape of the region that encloses all nodes in a tile in a diagram of the decision tree. More formally, for a tile size  $n_t$ , each unique legal binary tree containing  $n_t$  nodes (nodes being indistinguishable) corresponds to a tile shape.

Figure 2 enumerates all tile shapes with a tile size of 3. There are a total of 5 tile shapes with size 3. The number of tile shapes with a tile size  $n_t$ , denoted by  $NTS(n_t)$  is given by the following equation.

$$NTS(n) = \sum_{k=0}^{n-1} NTS(k) \times NTS(n-k-1)$$
 (1)

where NTS(0) = NTS(1) = 1.

## 3.4 Valid Tiling of a Tree

A tiling  $\mathscr{T}$  of the tree T = (V, E, r) with tile size  $n_t$  is a partition  $\{T_1, T_2, ..., T_m\}$  of the set V such that

- 1.  $T_1 \cup T_2 ... \cup T_m = V$
- 2.  $T_i \cap T_j = \emptyset$  for all  $i, j \in [1, m]$  and  $i \neq j$
- 3.  $|T_i| \le n_t$  for all  $i \in [1, m]$
- 4.  $\forall l \in L : l \in T_i \rightarrow v \notin T_i \ \forall v \in V \setminus \{l\}$
- 5. Tiles are **maximal**, i.e. if  $|T_i| < n_t$ , then there is no  $v \in V \setminus \{T_i \cup L\}$  such that  $(u, v) \in E$  for some  $u \in T_i$ .
- 6. Tiles are **connected**, i.e. for an  $u, v \in T_i$ , there is a (undirected) path connecting u and v fully contained in  $T_i$ .

## 3.5 Tiled Trees

A tiling transformation communicates the tiling to the Treebeard infrastructure by assigning a tile ID to each node in the decision tree. Using these tile IDs, Treebeard checks the validity of the tiling and then contructs a tree whose nodes are tiles. We call this tree the *tree of tiles*. TODO We need a better name for this Figure 3 shows a valid tiling with tile size 3 and the tree of tiles constructed by Treebeard. Three nodes are grouped into each of the tiles  $t_1$  and  $t_2$  as shown. Each tile is collapsed into a single node in the tree of tiles. However, each leaf in the original tree becomes a leaf in the tree of tiles.

Treebeard maintains the following invariants.

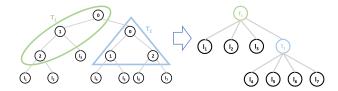


Figure 3: Example of a valid tree tiling with tile size  $n_t = 3$ 

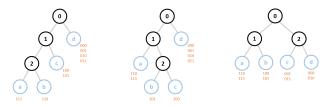


Figure 4: Example tile traversals with tile size  $n_t = 3$ 

- 1. All tiles in a tree are the same size  $n_t$ . If the tiling produces any smaller tiles, these are padded by inserting dummy nodes to make them the required size.
- 2. Nodes within tiles are always ordered in level order and left to right within a level. The numbering of the nodes in the above diagram shows this node order.
- Children of a node are numbered from left to right (regardless of level). For example, l<sub>1</sub> is the first child of t<sub>1</sub>, l<sub>2</sub> is the second and so on.

## 3.6 Tile Shapes and Decision Tree Inference

Treebeard uses vector instructions to accelerate decision tree walks. Vector instructions are used to evaluate the predicates of all the nodes in a tile simultaneously. However, once the predicates of all the nodes in the tile are evaluated, computing the next tile to move to, given the outcome of the comparison depends on the tile shape of the current tile. To illustrate this problem, consider the case of the tiles of size 3 shown in figure 4. The diagram shows 3 of the 5 possible tile shapes for a tile size of 3. The nodes drawn in black are members of the tile  $t_1$ . The nodes in blue are the entry nodes of the children tiles of  $t_1$ . TODO Define entry nodes

To traverse a tile on an input row, first, the predicate of each node in the tile is computed. Subsequently, we need to determine which of the child tiles to move to next. Note that a true predicte (bit value 1) on a node implies a move to the left child and a false predicate (bit value 0) implies a move to the right child.

In the diagram, the bit strings (written in red) show which child we need to move to given the outcomes of the comparison (the bits represent the comparison outcomes of nodes and are in the order of the nodes in the tile – marked 0, 1 and 2 in the diagram, i.e., the MSB is the predicate outcome of node 0 and the LSB the predicate outcome of node 2). For example, for the first tile shape, if the predicate of all nodes are true (i.e. the comparison outcome is 111), the next node to evaluate is a. However, if the predicate of node 1 is false, then we need to move to d regardless of the outcomes of nodes 2 and 3. It is easy to see from the diagram that, depending on the

tile shape, the same predicate outcomes can mean moving to different children. For example, for the outcome "011", the next tile is the 4th child (node d) for the first two tile shapes while it is the 3rd child for the other tile shape (node c).

## 3.7 Lookup Table

A lookup table (LUT) is used to solve the problem described in section 3.6, i.e. given the outcome of the comparisons on all nodes in a tile, determine the child tile we should evaluate next. The LUT is indexed by the tile shape and the comparison outcome. Formally, the LUT is a map.

```
LUT: (TileShape, < Boolean \times n_t >) \rightarrow [0, n_t] \subset \mathbb{N}
```

where  $n_t$  is the tile size,  $< Boolean \times n_t >$  is a vector of  $n_t$  booleans. The value returned by the LUT is the index of the child of the current tile that should be evaluated next. For example, if we are evaluating the first tile t in figure 4, and the result of the comparison is 110, then LUT(TileShape(t), 110) = 1 since the tile we need to evaluate next is the tile with node b, which is the second child of the current tile.

In order to realize this LUT in generated code, Treebeard associates a non-negative integer ID with every unique tile shape of the given tile size. The result of the comparison, a vector of booleans, can be interpreted as a 64-bit integer. Therefore, the LUT can be implemented as a 2 dimensional array.

```
int16_t LUT[NTS(n_t), pow(2, n_t)]
```

Treebeard computes the values in the LUT statically as the tile size is a compile time constant.

## 3.8 In Memory Representation of Tiled Trees

Treebeard currently has two in memory representations for tiled trees - an array based representation and a sparse representation. Both representations use an array of structs to represent all tiles of the model.

#### 3.8.1 Array Based Representation

Each tree in the model is represented as an array of tiles using the standard representation of trees as arrays. The root node is at index 0 and for a node at index n in the array, the index of its  $i^{th}$  child is given by  $(n_t+1)n+(i+1)$  (every node in the tree of tiles has  $n_t+1$  children). A tile is represented by an object of the following struct.

```
struct Tile {

// A vector of TileSize elements

<ThresholdType x TileSize> thresholds;

<FeatureIndexType x TileSize> featureIndices;

// Integer that identifies the tile shape

TileShapeIDType tileShapeID;

};
```

TODO AP Is this level of detail really needed? Also, the vector type notation needs to be introduced somewhere. Even though this representation is simple, the memory required for reasonable sized models is very large. The memory footprint is up to 20X that of the scalar representation. This memory bloat causes a performance degradation because the span of the L1 TLB is not sufficient to efficiently translate addresses

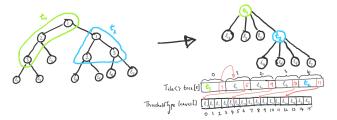


Figure 5: Sparse representation with tile size  $n_t = 3$ 

for the whole model. TODO AP There are also some cache misses. Write this better. Storing leaves as full tiles (even though leaves just have to represent one value) and the empty space introduced due to the array based representation of trees that are not complete account for most of the increase. The sparse representation described next tries to address these issues.

## 3.8.2 Sparse Representation

The sparse representation tries to address the large memory footprint of the array based representation by doing the following.

- To eliminate the wasted space in the array representation, we add a child pointer to each tile. This points to the first child of the tile. All children of a tile are stored contiguously.
- Leaves are stored in a separate array. We found that, across all our benchmarks, a large fraction of leaves are such that all their siblings are also leaves. Such leaves are directly moved into the leaves array. For leaves for which this property does not hold, an additional hop is added by making the leaf tile a comparison tile and all its children are made leaves with the same value as the original leaf.

Figure 5 shows some of the details of the sparse representation. The tree on the left of the diagram is the actual decision tree with the nodes grouped into tiles  $t_1$  and  $t_2$ . The tree on the right is the tree of tiles. The arrays depicted below show how the tree is represented in memory. The first array (tree) is an array of tiles and has 5 elements. Each element of the array represents a single tile and has the thresholds of the nodes, the feature indices, a tile shape ID and a pointer to the first child (shown explicitly in red).

As a specific example, consider the tile  $t_1$ . The tile has four children  $-l_1$ ,  $l_2$ ,  $l_3$  and  $t_2$  in that order (left to right). These tiles are stored contiguously in the tree array and a pointer to the first of these,  $l_1$  is stored in the tile  $t_1$  (the index 1 is stored in the tile  $t_1$  as shown).

Now consider the tile  $t_2$ . Since all children of the tile  $t_2$  are leaves, they are all moved into the leaves array. To store a pointer into the leaves array, we add len(tree) to the element index in the leaves array. The tile  $t_2$ 's child is the element at index 12 of the leaves array. Therefore, the index 12+5=17 is stored in the tile  $t_2$ . (Any index i that is greater than the length of the tree array is regarded as an index into the leaves array. The index into the leaves array is i-len(tree).)

The other aspect of the representation is that an extra hop is added for the leaves  $l_1$ ,  $l_2$  and  $l_3$  in order to simplify code generation. This enforces the invariant that all leaves are stored in the leaves array and simplifies checking whether we've reached a leaf. Therefore, 4 new leaves are added as children for each of the original leaves  $l_1$ ,  $l_2$  and  $l_3$ . Each of these 12 newly added leaves has the same value as its parent. These are the first 12 elements of the leaves array.

Even though we currently have implementations of the two representations detailed in sections 3.8.1 and 3.8.2, support for other representations is not hard to add. All optimizing passes that work on the high level and mid level IR will continue to work as is. Programmers need only provide new lowering passes for a few operations in the low level IR.

## 3.9 Uniform Tiling

The first tree tiling algorithm we implement is uniform tiling. The basic idea of uniform tiling is to construct tiles with a tile size  $n_t$  so that we evaluate the least possible number of nodes speculatively. Intuitively, this translates to minimizing the height of the constructed tile. We minimize the height of the tile by performing a level order traversal starting at the root node of the tile. TODO AP Should we say this is optimal when probabilities are equal? Problem is we haven't said what optimal is. This traversal collects at most  $n_t$  nodes and does not include any leaves in the tile so that the constraints listed in section 3.4 are respected. Algorithm 1 lists the algorithm for uniform tiling. Tiling starts at the root and constructs a tile *Tile* by performing a level order traversal. Once the current tile is constructed, the tiling procedure is recursively performed on all nodes that are destinations for edges going out of the constructed tile. The set of tiles constructed by algorithm 1 constitutes a uniform tiling of the input tree.

#### Algorithm 1 Uniform tree tiling

```
procedure TILETREE(T = (V, E, r), n_t)

if r \in L then

return \{r\}

end if

//Level order traversal to collect n_t or fewer nodes.

//Leaves are not included in the constructed tile.

Tile \leftarrow LevelOrderTraveral(r, n_t)

Tiles = \{Tile\}

for (u, v) \in Out(Tile) do

Tiles \leftarrow Tiles \cup TileTree(T_v, n_t)

end for

return Tiles

end procedure
```

## 3.9.1 Further Opimization and Code Generation

We found that most leaf tiles for a given tree are at the same depth when uniform tiling is used. Furthermore, we see that deeper leaves are more likely to be reached. Based on these observations, we pad the tree of tiles generated with uniform tiling so that all leaves are at the same depth. This transformation is performed on the high level IR after uniform

tiling. Once the trees have been padded to make all leaves equal depth, the tree walks are fully unrolled to evaluate a fixed number of tiles and all leaf checks are elided.

One other complication the code generator needs to handle is the fact that trees potentially have different depths. In order to handle this, Treebeard sorts the trees by their depth. This ensures that all trees with equal depth are grouped together. Once this is done, the loop over the trees is fissed so that each of the resulting loops only walks trees of a single depth. Consider for example a forest with 4 trees  $T_1$ ,  $T_2$ ,  $T_3$ , and  $T_4$  in that order. Further, assume that  $T_1$  and  $T_4$  have depth 2 while  $T_2$  and  $T_3$  have depth 3. First, Treebeard reorders the trees to be in the order  $T_1$ ,  $T_4$ ,  $T_2$ ,  $T_3$ . Then, the loop over the trees is fissed as shown in the following listing.

```
forest = ensemble (...)
for i = 0 to batchSize step 1 {
  prediction = 0
  for t = 0 to 2 step 1 {
    tree = getTree (forest, t)
   node = getRoot(tree)
   node = traverseTreeTile(tree, node, rows[i])
    treePrediction = getLeafValue(tree, node)
   prediction = prediction + treePrediction
  for t = 2 to 4 step 1 {
    tree = getTree(forest, t)
   node = getRoot(tree)
    node = traverseTreeTile(tree, node, rows[i])
   node = traverseTreeTile(tree, node, rows[i])
    treePrediction = getLeafValue(tree, node)
   prediction = prediction + treePrediction
 predictions[i] = prediction
```

TODO AP: This listing is unnecessarily long. Can we maybe leave out the loop bodies and say something like "depth 2 walk"?

## 3.10 Probability Based Tiling

#### 3.10.1 Motivation

As discussed in section 3.9, uniform tiling optimizes tree walks assuming that all paths in the tree from root to leaf are equally likely. However, we find that this is not always the case. We performed inference on the complete training set of each of our benchmarks and measured how many times each leaf was reached. While for some benchmarks all leaves are roughly equally likely, for others, a small number of leaves are extremely likely while the rest aren't reached often. We call trees with a small number of extremely likely leaves **skewed**. Figures 6 and 7 show this. Each line in these graphs corresponds to a fixed fraction of the input (say f). A point on a line at coordinate (x, y) means that y percent of trees in the model could handle a fraction f of all training inputs with x percent of leaves. TODO Explain with a specific point in one of the graphs Figure 6 shows that very few leaves are reached for a very large fraction of inputs for the benchmark airline-ohe. This means that a small fraction of leaves are very likely. On the other hand, figure 7 shows that a large fraction of trees need a large fraction of their leaves to handle any fraction of the test input for the benchmark epsilon. One other observation we made is that most models have some skewed trees while the rest of the trees have equally likely leaves.

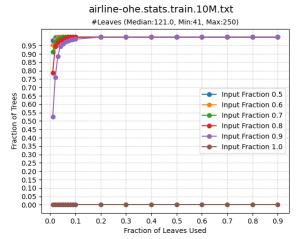


Figure 6: Statistical profile for airline-ohe

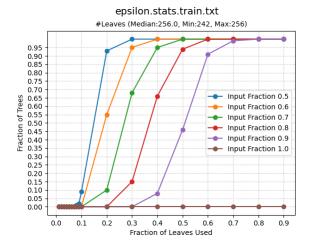


Figure 7: Statistical profile for epsilon

TODO AP Define a term for trees with roughly equally likely leaves. We design the probability based tiling algorithm to take advantage of this property of decision tree ensembles. TODO This section needs to be rewritten. Define "leaves covering inputs" to clarify the presentation.

#### *3.10.2 Notation*

In order to formulate the probability based tiling algorithm as an optimization problem, we define the following.

- 1. For every leaf  $l \in L$ , we define  $p_l$  as the probability that the leaf l is reached.
- 2. For each node  $n \in V$ , we define the absolute probability  $p_v$  as

$$p_{v} = \begin{cases} p_{l} & \text{if } l \in L \\ p_{left(v)} + p_{right(v)} & \text{otherwise} \end{cases}$$
 (2)

- 3. For any tree T,  $\mathscr{C}(T)$  represents the set of all valid tilings of T.
- 4. For every  $v \in V$ , we define  $S_v$  as the subtree rooted at v.
- 5. For every  $v \in V$ , we define  $L_v$  as the set of leaves of  $S_v$ .
- For a every tile T<sub>i</sub>, we define root(T<sub>i</sub>) as the node v ∈ T<sub>i</sub> such that v has no incoming edges from any other node u ∈ T<sub>i</sub>.
- 7. For a tile  $T_i$ ,  $out(T_i) \subseteq E$  is the set of edges (u, v) such that  $u \in T_i$  and  $v \notin T_i$ .

#### 3.10.3 The Optimization Problem

We observe that the latency of one tree walk is proportional to the number of tiles that need to be evaluated to reach the leaf. Therefore, the average inference latency can be modelled as the expected number of tiles that are evaluated to compute one tree prediction. More formally, the problem is to find a tiling  $\mathcal{T}$  such that the following objective is minimized.

$$\min_{\mathcal{T} \in \mathcal{C}(T)} \sum_{l \in L} p_l.depth_{\mathcal{T}}(l)$$

where the minimization is over all valid tilings  $\mathscr{T}$  of the tree T,  $depth_{\mathscr{T}}(l)$  is the depth of the leaf l given tiling  $\mathscr{T}$ .

The constraints on the optimization are the constraints listed in Section 3.4. The above optimization problem can be solved optimally using dynamic programming. We leave this out in the interest of space. Instead, we use the simple greedy algorithm listed in algorithm 2 to construct a valid tiling given the node probabilities. The algorithm starts at the root and greedily keeps adding the most probable legal node to the current tile until the maximum tile size is reached. Subsequently, the tiling procedure is recursively performed on all nodes that are destinations for edges going out of the constructed tile.

When we tried to apply algorithm 2 on all trees in our benchmarks, we found that even minor variations in probability caused the tiling algorithm to generate a large number of tile shapes. This in turn caused a loss in performance because the large size of the lookup table needed (section

### Algorithm 2 Greedy Probability Based Tree Tiling

```
procedure TILETREE(T = (V, E, r), n_t)
    if r \in L then
        return \{r\}
    end if
    Tile \leftarrow \{r\}
    while |Tile| < n_t do
        e = (u, v) \in Out(Tile) st p(v) is max and v \notin L
        if e = \emptyset then
             break
        end if
        Tile = Tile \cup \{v\}
    end while
    Tiles = \{Tile\}
    for (u, v) \in Out(Tile) do
        Tiles \leftarrow Tiles \cup TileTree(S_v, n_t)
    end for
    return Tiles
end procedure
```

3.7) caused increased L1 cache misses. In order to alleviate this, we only perform probability based tiling on trees that are skewed. We say a tree is skewed if a small fraction of leaves, say  $\alpha$ , cover a large fraction of training inputs, say  $\beta$ . We only perform probability based tiling on skewed trees and fall back to uniform tiling otherwise. In our experiments we use  $\alpha = 0.05$  and  $\beta = 0.9$ .

#### 3.10.4 Code Generation

As probability based tiling pulls the most probable leaves of a decision tree nearest the root, it poses some implementation challenges. By design, the tiling process makes the tree of tiles imbalanced. Therefore, the simple array based representation described in section 3.8.1 cannot be used because of the memory footprint blow up (a large part of the tree is empty, but would need to be allocated). On the other hand, the sparse representation in section 3.8.2 adds an extra hop for leaves that have non-leaf siblings. But this would mean that we add extra hops for the most probable leaves after probability based tiling. To address these problems, Treebeard peels the tree walk and specializes the leaf checks at higher levels to avoid the extra hop. Currently, we determine the maximum depth of leaves needed to cover 90 percent of the inputs and peel the tree walk by as many iterations. For example, consider the case where leaves until depth 2 are needed to cover 90 percent of the training input. Then, Treebeard generates the following IR.

```
30
      tree = getTree(forest, t)
31
      node = getRoot(tree)
      node = traverseTreeTile(tree, node, rows[i])
       if (isLeafTile(node)) {
33
           treePrediction = getLeafValue(tree, node)
34
35
36
           node = traverseTreeTile(tree, node, rows[i])
37
           if (isLeafTile(node)) {
               treePrediction = getLeafValue(tree, node)
39
               // Loop based traversal
```

```
treePrediction = getLeafValue(tree, node)
// ...
```

The if statements check whether a node is a leaf tile and hence avoid the extra hop. The memory requirement is also not increased because only a small fraction of leaves are represented as full tiles. While walk peeling is used to improve the performance of probability based tiling by specializing leaf tests, the transformation is by itself general and can be used in different contexts. For example, it could be used to elide leaf checks until a depth d is reached if we know all leaves are at a depth greater than d.

One other issue that the code generator needs to handle is that walks of different trees in the same ensemble may need to be peeled to different depths. In order to handle this, trees are reordered so that all trees with equal peeling depth are grouped together and the loops in the IR are fissed so that tree walks for these groups of trees can be specialized differently. This is very similar to the code generation strategy used for uniform tiling.

## 3.11 Unroll and Jam

While tiling and subsequent vectorization gives significant performance gains, profiling the generated code showed that true dependencies between instructions were still causing a significant number of stall cycles. In order to fill these stall cycles, Treebeard does an unroll and jam on the inner most loops of the loop nest. This transformation has the effect of walking multiple tree and input row pairs in an interleaved fashion. The dependency stalls can be hidden by scheduling instructions from independent tree walks in the stall cycles.

This optimization is performed across both the mid-level IR and low-level IR. Loops on which to perform unroll and jam are identified in the mid-level IR. This information is communicated to the lowering passes by replacing these tree walks with specialized tree walk operations. The lowering passes that transform the mid-level IR to low-level IR interleave operations across independent tree walks.

The following listing shows the mid-level IR when the inner loop over the input rows is unrolled by a factor of 2 and the two resulting tree walks are jammed together.

```
forest = ensemble(...)
for t = 0 to 4 step 1 {
   for i = 0 to 2 step 2 {
      tree = getTree(forest, t)
      prediction1, prediction2 = InterleavedWalk((tree, rows[i]), (tree, rows[i+1]))
   }
}
```

When lowered to low-level IR, the operations to traverse each of the tree, input row pairs (the arguments to the InterleavedWalk) are interleaved. One step of the interleaved walk is listed below.

```
1  // ...
2  n1 = n2 = getRoot(tree)
3  // ...
4  threshold1 = loadThresholds(n1)
5  threshold2 = loadThresholds(n2)
6  featureIndex1 = loadFeatureIndices(n1)
7  featureIndex2 = loadFeatureIndices(n2)
8  feature1 = rows[i][featureIndex1]
9  feature2 = rows[i][featureIndex2]
pred1 = feature1 < threshold1
pred2 = feature2 < threshold2</pre>
```

These transformations are fairly general and are not aware of the in memory representation of the model. Therefore, they are reusable across different in memory representations - the ones that are currently built into Treebeard or ones that are added in the future. TODO AP I feel the way this section is currently written makes the optimization seem extremely trivial. Is there a different way to present it?

## 3.12 Vectorization

Vectorization performed by Treebeard is enabled by the tiling transformations described in section 3.2. When the low level IR is translated to LLVM IR, Treebeard generates LLVM instructions that operate on the threholds and feature indices of nodes within a tile in a vector fashion. Therefore, thresholds and feature indices are loaded using vector loads and predicates are evaluated using vector comparisons. These vector LLVM IR instructions are then converted to vector instructions in the target ISA by the LLVM JIT.

#### 3.13 Parallelization

Currently, Treebeard performs a naive parallelization of the inference computation. When parallelism is enabled, the loop over the input rows is parallelized using OpenMP. Treebeard rewrites the mid-level IR by tiling the loop over the input rows with a tile size equal to the number of cores. As a concrete example, consider the case where we intend to perform inference using a model with 4 trees on a batch of 64 rows. Further, assume that we wish to parallelize this computation across 8 cores. Treebeard then generates the following IR.

```
forest = ensemble(...)
parallel.for i0 = 0 to 64 step 8 {
    for i1 = 0 to 8 step 1 {
        i = i0 + i1
        prediction = 0
    for t = 0 to 4 step 1 {
            tree = getTree(forest, t)
            treePrediction = WalkTree(tree, rows[i])
            prediction = prediction + treePrediction
        }
    predictions[i] = prediction
}
```

Currently, as our focus is on single core performance, we do not do any parallelism related optimizations (such as loop tiling). We leave a more thorough exploration of parallelization to future work.

#### REFERENCES

 C. Lattner and V. Adve, "Llvm: a compilation framework for lifelong program analysis amp; transformation," in *International Symposium on Code Generation and Optimization*, 2004. CGO 2004., 2004, pp. 75–86.