

Simulation Exercise: Exponential Survival Data with Censoring

Objective

Simulate data from a hypothetical clinical trial with two treatment arms (Control and Treatment). The survival times should follow an exponential distribution, with non-informative right censoring.

Scenario

You're designing a simulation study to evaluate the impact of a new treatment on patient survival. You need to:

- Simulate 500 patients randomized equally to two arms.
- Generate exponentially distributed survival times with different hazard rates for each arm.
- Apply non-informative censoring using a separate exponential distribution.
- Create Kaplan-Meier survival curves and estimate hazard ratios.

Step 1: Define Simulation Parameters

- Total patients: $n < 500$
- Proportion in treatment arm: 0.5
- Hazard rates:
 - Control: $\lambda_{\text{control}} = 0.1$
 - Treatment: $\lambda_{\text{treatment}} = 0.07$
 - Censoring: $\lambda_{\text{censor}} = 0.05$

Tip: Use `rbinom()` to randomly assign groups.

Step 2: Generate Survival and Censoring Times

Use `rexp(n, rate)` to simulate:

- `true_survival`
- `censoring_time`

Observed time = `pmin(true_survival, censoring_time)`

Event indicator = `as.integer(true_survival <= censoring_time)`

Repeat for both treatment groups.

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Step 3: Combine the Data

Combine control and treatment data using `rbind()`.

Ensure the dataset has: `id`, `group`, `time`, `status`, `true_survival`, `censor_time`.

Make `group` a factor: Control vs Treatment.

Step 4: Kaplan-Meier Curves

Use `Surv(time, status)` and `survfit()` to estimate curves.

Use base R `plot()` or `ggsurvplot()` (from `survminer`) to visualize survival.

Step 5: Cox Proportional Hazards Model

Use `coxph(Surv(time, status) ~ group, data)`.

This will estimate hazard ratios and test for treatment effect.

Bonus Challenge

Add a covariate (e.g., age using `rnorm()`).

Include it in the Cox model and observe how the HR changes.

Expected Output

- Simulated dataset with 500 rows
- Kaplan-Meier plot showing separation
- Hazard ratio < 1 if treatment is effective