

AI1103-Assignment 1

Name: Vikhyath Sai Kothamasu, Roll Number: CS20BTECH11056

Download all python codes from

<https://github.com/Vikhyath-vec/AI1103/tree/main/Assignment-1/codes>

and latex-tikz codes from

<https://github.com/Vikhyath-vec/AI1103/blob/main/Assignment-1/Assignment-1.tex>

QUESTION

A box contains 5 red marbles, 8 white marbles, and 4 green marbles. One marble is taken out of the box at random. What is the probability that the marble taken out will be

- 1) red?
- 2) white?
- 3) not green?

SOLUTION

Total number of marbles = $5 + 8 + 4 = 17$ marbles.
Let $X \in \{0, 1, 2\}$ represent the random variable, where 0 represents a red marble, 1 represents a white marble, and 2 represents a green marble. From the given information,

- 1) Probability that the marble taken out will be red = $\Pr(X=0)$

$$\Pr(X = 0) = \frac{\text{number of red marbles}}{\text{total number of marbles}} \quad (0.0.1)$$

$$\Pr(X = 0) = \frac{5}{17} = 0.294117647 \quad (0.0.2)$$

- 2) Probability that the marble taken out will be white = $\Pr(X=1)$

$$\Pr(X = 1) = \frac{\text{number of white marbles}}{\text{total number of marbles}} \quad (0.0.3)$$

$$\Pr(X = 1) = \frac{8}{17} = 0.4705882353 \quad (0.0.4)$$

- 3) Probability that the marble taken out will not be green = $\Pr(X \neq 2)$

$\Pr(X \neq 2) + \Pr(X=2) = 1$ (since complementary events are mutually exclusive)

$$\Rightarrow \Pr(X \neq 2) = 1 - \Pr(X=2)$$

$$\Pr(X = 2) = \frac{\text{number of green marbles}}{\text{total number of marbles}} \quad (0.0.5)$$

$$\Pr(X = 2) = \frac{4}{17} \quad (0.0.6)$$

$$\Rightarrow \Pr(X \neq 2) = 1 - \frac{4}{17} = \frac{13}{17} = 0.764705883 \quad (0.0.7)$$