

# **Natural Language Processing (CS5803)**

Lecture 8  
(Parsing - Part I)

# Parsing

- Natural language sentence: sequence of text – linear structure
- The **construction** of the sentence is governed by **grammatical rules**
- How the **words connect with each other** according to the rule – structural composition of the sentence
- Identifying the **structural composition** – **parsing**
  - **Constituency Parsing:** Phrase information
  - **Dependency Parsing:** Relationship between words
  - **Semantic Parsing:** Logical interpretation

# Part I - Constituency Parsing

# Constituency

- Fundamental notion underlying the idea of constituency is that of abstraction
  - groups of words behaving as single units, or constituents.
- How do words group together in English?
  - On July ninth, I'd like to fly from Atlanta to Denver.
  - I'd like to fly on July ninth from Atlanta to Denver.
  - I'd like to fly from Atlanta to Denver on July ninth .
- How to model constituent structure in English?
  - **Context-Free Grammar (CFG)**



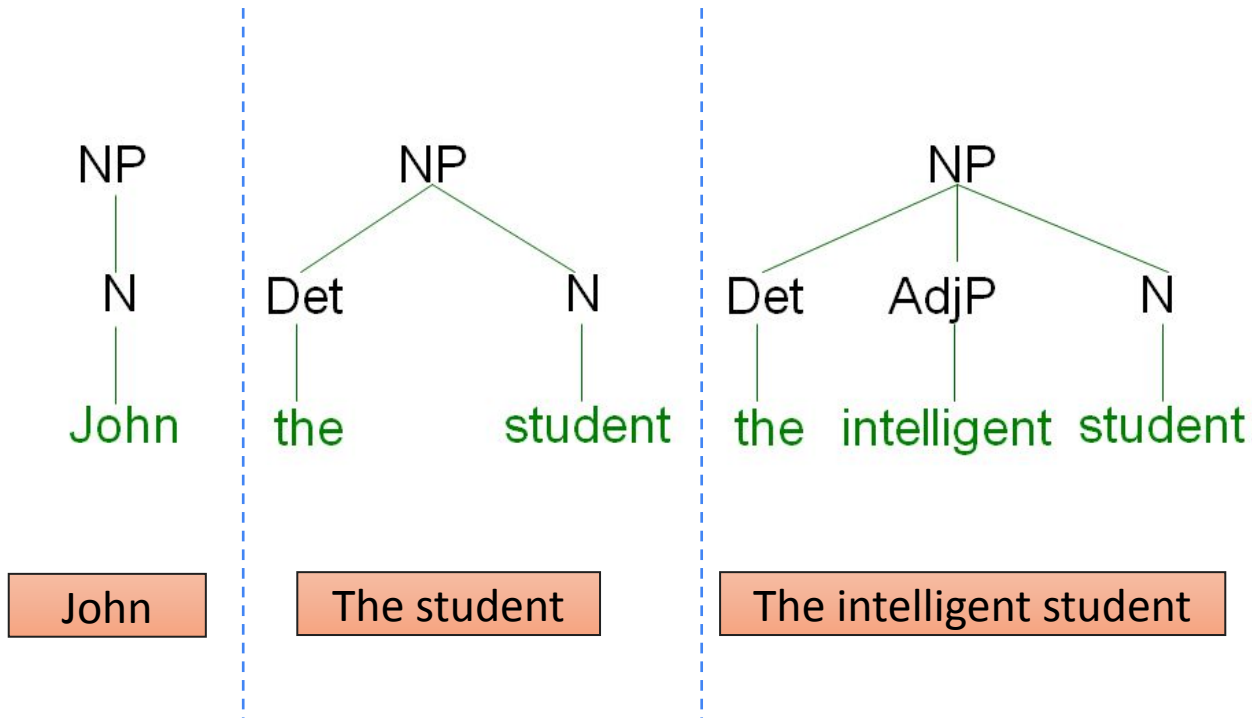
# CFG

- Also called **Phrase-Structure Grammar (PSG)**
- CFG can be viewed as a device for
  - generating sentences
  - assigning a structure to a given sentence
- A context-free grammar  $G$  is defined by four parameters:  **$(N, \Sigma, R, S)$** 
  - **$N$** : a set of **non-terminal symbols** (or variables)
  - **$\Sigma$** : a set of **terminal symbols** (disjoint from  $N$ )
  - **$R$** : a **set of rules** or productions, each of the form  $A \rightarrow \beta$ , where  $A$  is a non-terminal,  $\beta$  is a string of symbols from the infinite set of strings  $(\Sigma \cup N)^*$
  - **$S$** : a designated **start symbol** and a member of  $N$

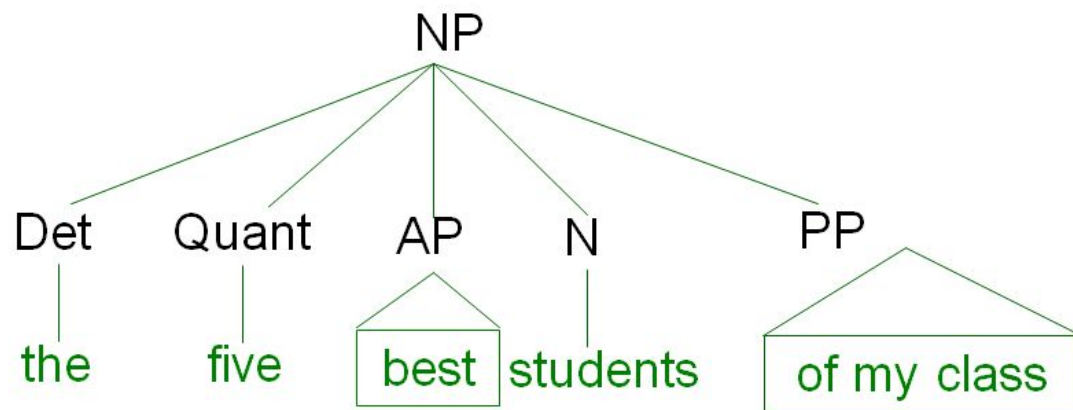
```
S -> AB  
A -> to X  
B -> in Y  
X -> HYD  
X -> BLR  
Y -> May  
Y -> Jun
```

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A -> to X  
B -> in Y  
X -> HYD | BLR  
Y -> May | Jun
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# Noun Phrase

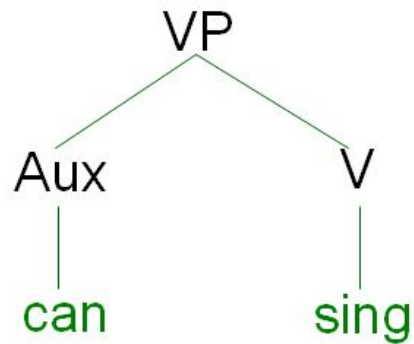


# Noun Phrase

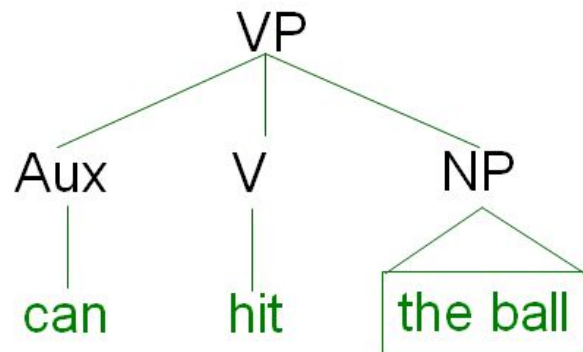


The five best students of my class

# Verb Phrase



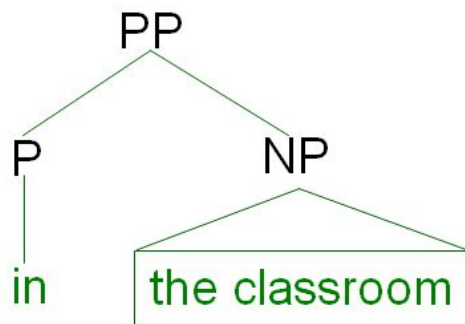
can sing



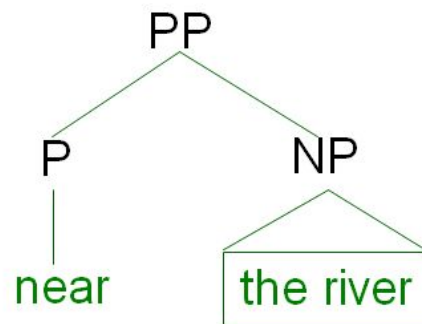
can hit the ball



# Prepositional Phrase

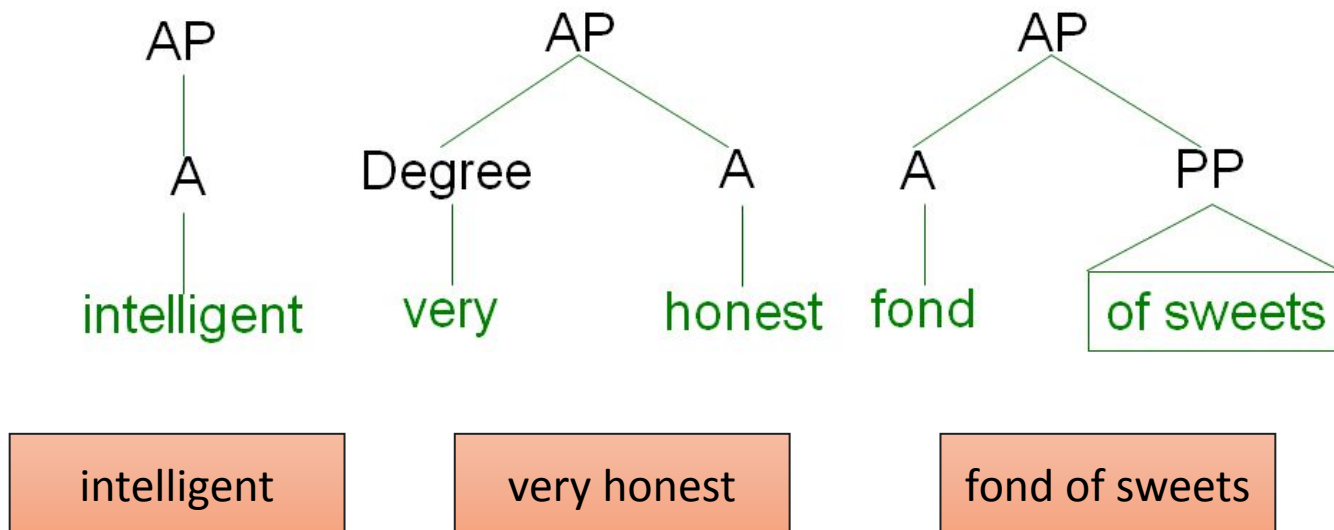


in the classroom

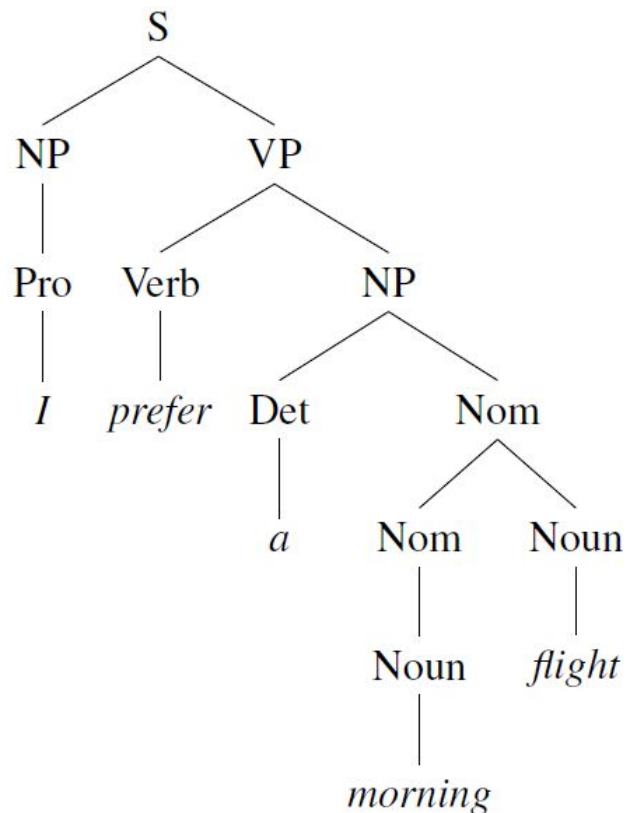


near the river

# Adjective Phrase



# CFG/PSG Parse Tree



*Noun* → *flights* | *breeze* | *trip* | *morning*  
*Verb* → *is* | *prefer* | *like* | *need* | *want* | *fly*  
*Adjective* → *cheapest* | *non-stop* | *first* | *latest*  
               | *other* | *direct*  
*Pronoun* → *me* | *I* | *you* | *it*  
*Proper-Noun* → *Alaska* | *Baltimore* | *Los Angeles*  
                   | *Chicago* | *United* | *American*  
*Determiner* → *the* | *a* | *an* | *this* | *these* | *that*  
*Preposition* → *from* | *to* | *on* | *near*  
*Conjunction* → *and* | *or* | *but*

*S* → *NP VP*  
  
*NP* → *Pronoun*  
       | *Proper-Noun*  
       | *Det Nominal*  
*Nominal* → *Nominal Noun*  
           | *Noun*  
  
*VP* → *Verb*  
       | *Verb NP*  
       | *Verb NP PP*  
       | *Verb PP*  
  
*PP* → *Preposition NP*

# Treebanks

- Syntactically annotated corpus
- Every sentence is paired with a corresponding parse tree
- Penn Treebank
  - “That cold, empty sky was full of fire and light.”

```
((S
  (NP-SBJ (DT That)
    (JJ cold) (, ,)
    (JJ empty) (NN sky) )
  (VP (VBD was)
    (ADJP-PRD (JJ full)
      (PP (IN of)
        (NP (NN fire)
          (CC and)
          (NN light) ))))
  (. .) ))
```

Penn Treebank Syntactic Annotation Format

## Penn POS Tags

■ Adjective:	JJ
■ Adverb:	RB
■ Cardinal Number:	CD
■ Determiner:	DT
■ Preposition:	IN
■ Coordinating Conjunction	CC
■ Subordinating Conjunction:	IN
■ Singular Noun:	NN
■ Plural Noun:	NNS
■ Personal Pronoun:	PP
■ Proper Noun:	NP
■ Verb base form:	VB
■ Modal verb:	MD
■ Verb (3sg Pres):	VBZ
■ Wh-determiner:	WDT
■ Wh-pronoun:	WP

# Constituency Parsing Algorithm

- Top Down :
  - Start with **S** and generate the sentence.
- Bottom up :
  - Start with the words in the sentence and use the rewrite rules backwards to reduce the sequence of symbols to produce **S**

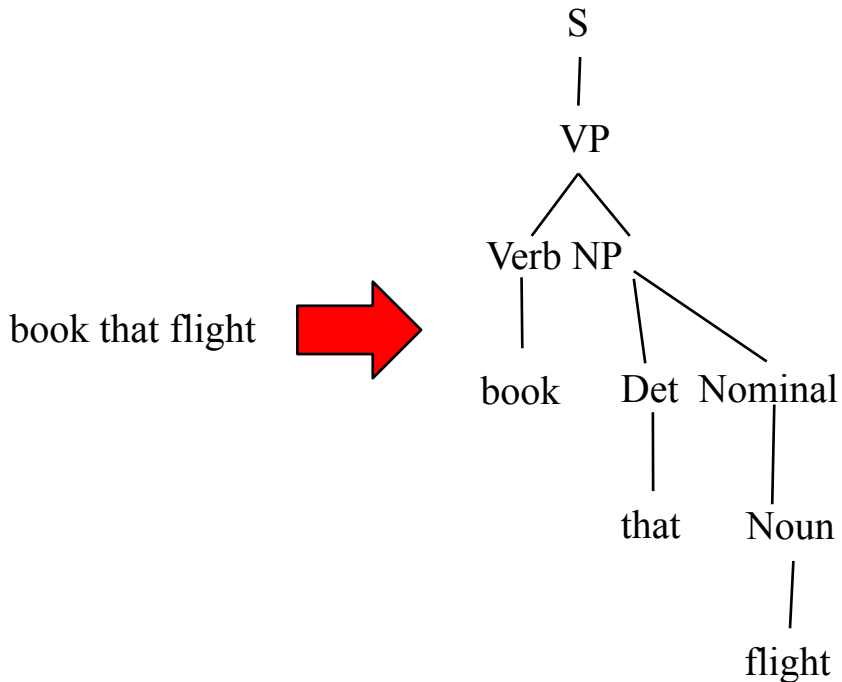
S → NP VP  
VP → V NP  
NP → NNP | ART N  
NNP → Ram  
V → ate | saw  
ART → a | an | the  
N → rice | apple |  
movie

Top Down Parsing

Ram ate the rice  
=> NNP ate the rice (rewrite Ram)  
=> NNP V the rice (rewrite ate)  
=> NNP V ART rice (rewrite the)  
=> NNP V ART N (rewrite rice)  
=> NP V ART N (rewrite NNP)  
=> NP V NP (rewrite ART N)  
=> NP VP (rewrite V NP)  
=> S

Bottom Up Parsing

# Parsing Example



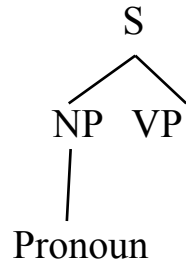
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 $VP \rightarrow Verb$   
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## Lexicon

$Det \rightarrow the \mid that$   
 $Noun \rightarrow book \mid flight$   
 $Verb \rightarrow book$   
 $Pronoun \rightarrow I \mid he \mid she \mid me$   
 $Proper-Noun \rightarrow Houston \mid NWA$   
 $Aux \rightarrow does$   
 $Prep \rightarrow from \mid to$

# Top Down Parsing



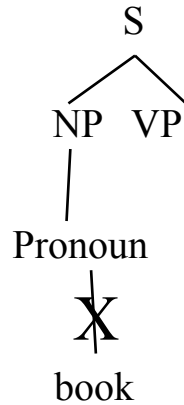
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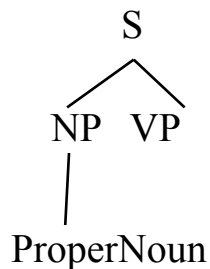
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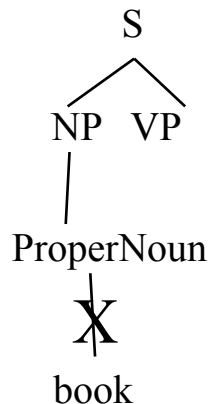
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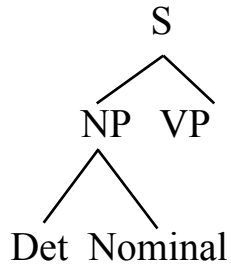
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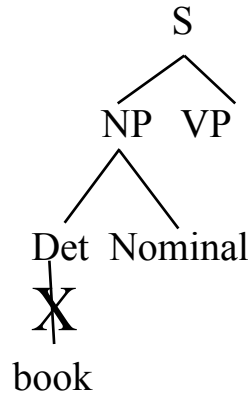
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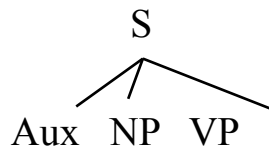
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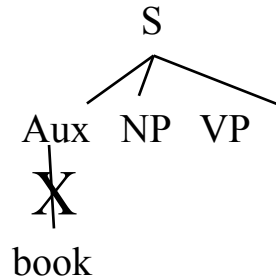
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# Top Down Parsing

S  
|  
VP

Grammar

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S  
|  
VP  
|  
Verb

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S  
|  
VP  
|  
Verb  
|  
book

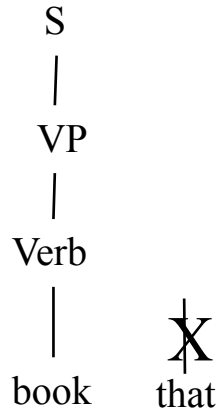
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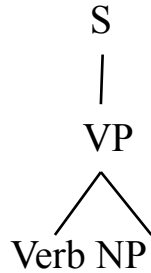
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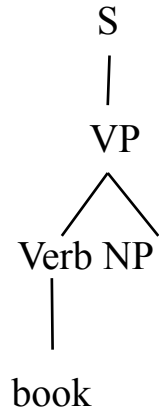
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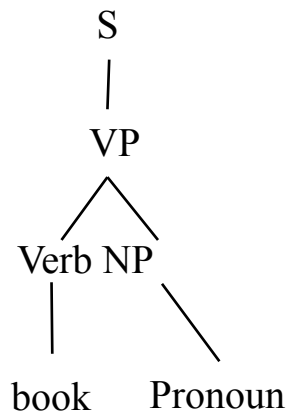
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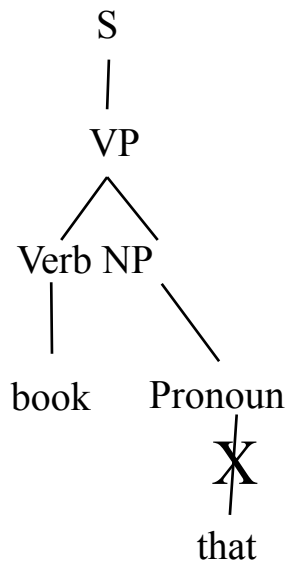
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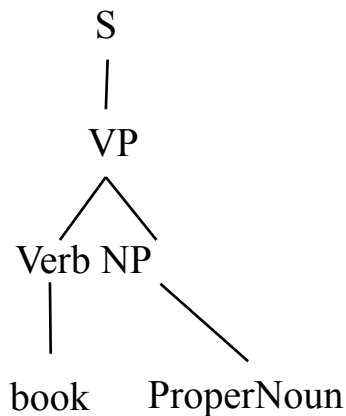
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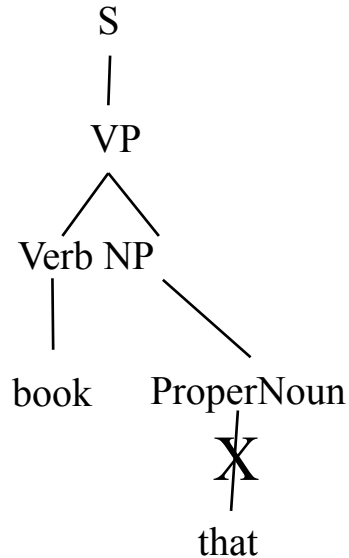
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## Lexicon

$Det \rightarrow the \mid that$   
 $Noun \rightarrow book \mid flight$   
 $Verb \rightarrow book$   
 $Pronoun \rightarrow I \mid he \mid she \mid me$   
 $Proper-Noun \rightarrow Houston \mid NWA$   
 $Aux \rightarrow does$   
 $Prep \rightarrow from \mid to$

# Top Down Parsing



## Grammar

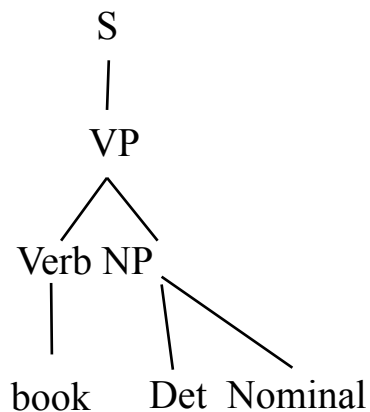
$S \rightarrow NP VP$   
 $S \rightarrow Aux NP VP$   
 $S \rightarrow VP$   
 $NP \rightarrow Pronoun$   
 $NP \rightarrow Proper-Noun$   
 $NP \rightarrow Det Nominal$   
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# Top Down Parsing



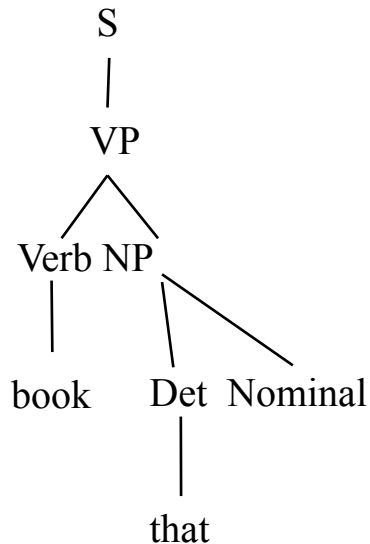
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# Top Down Parsing



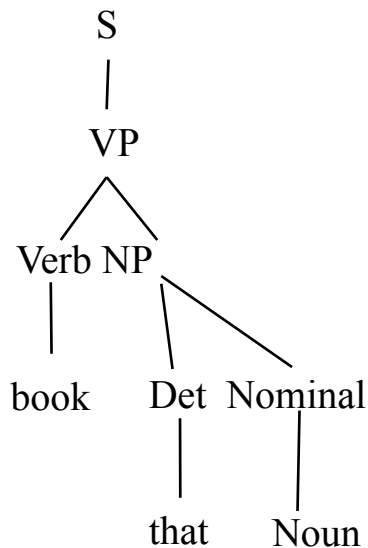
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# Top Down Parsing



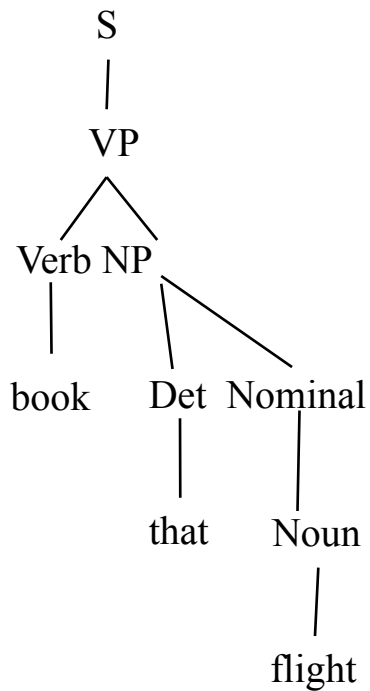
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$S \rightarrow NP VP$   
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# Top Down Parsing



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 $Aux \rightarrow does$   
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# Bottom Up Parsing

book    that    flight

## Grammar

$S \rightarrow NP VP$   
 $S \rightarrow Aux NP VP$   
 $S \rightarrow VP$   
 $NP \rightarrow Pronoun$   
 $NP \rightarrow Proper-Noun$   
 $NP \rightarrow Det Nominal$   
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# Bottom Up Parsing

Noun  
|  
book    that    flight

## Grammar

S  $\rightarrow$  NP VP  
S  $\rightarrow$  Aux NP VP  
S  $\rightarrow$  VP  
NP  $\rightarrow$  Pronoun  
NP  $\rightarrow$  Proper-Noun  
NP  $\rightarrow$  Det Nominal  
Nominal  $\rightarrow$  Noun  
Nominal  $\rightarrow$  Nominal Noun  
Nominal  $\rightarrow$  Nominal PP  
VP  $\rightarrow$  Verb  
VP  $\rightarrow$  Verb NP  
VP  $\rightarrow$  VP PP  
PP  $\rightarrow$  Prep NP

## Lexicon

Det  $\rightarrow$  the | that  
Noun  $\rightarrow$  book | flight  
Verb  $\rightarrow$  book  
Pronoun  $\rightarrow$  I | he | she | me  
Proper-Noun  $\rightarrow$  Houston | NWA  
Aux  $\rightarrow$  does  
Prep  $\rightarrow$  from | to

# Bottom Up Parsing

Nominal

|

Noun

|

book that flight

Grammar

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow Pronoun$

$NP \rightarrow Proper-Noun$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow Noun$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow Verb$

$VP \rightarrow Verb NP$

$VP \rightarrow VP PP$

$PP \rightarrow Prep NP$

Lexicon

$Det \rightarrow the \mid that$

$Noun \rightarrow book \mid flight$

$Verb \rightarrow book$

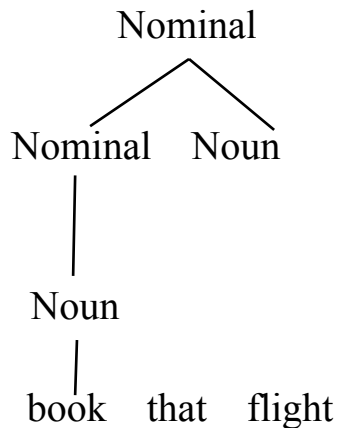
$Pronoun \rightarrow I \mid he \mid she \mid me$

$Proper-Noun \rightarrow Houston \mid NWA$

$Aux \rightarrow does$

$Prep \rightarrow from \mid to$

# Bottom Up Parsing



## Grammar

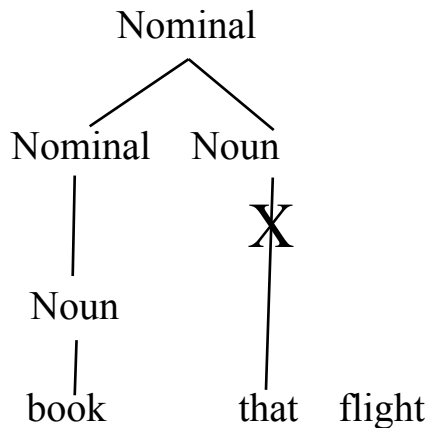
$S \rightarrow NP VP$   
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# Bottom Up Parsing



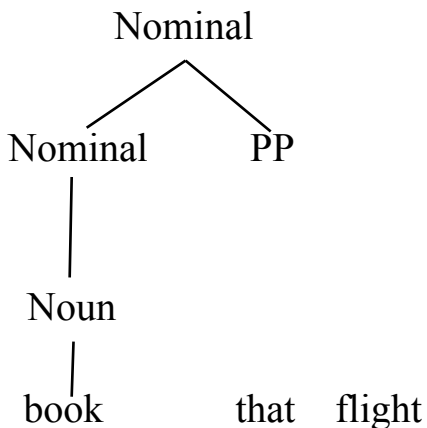
## Grammar

$S \rightarrow NP VP$   
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 $S \rightarrow VP$   
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# Bottom Up Parsing



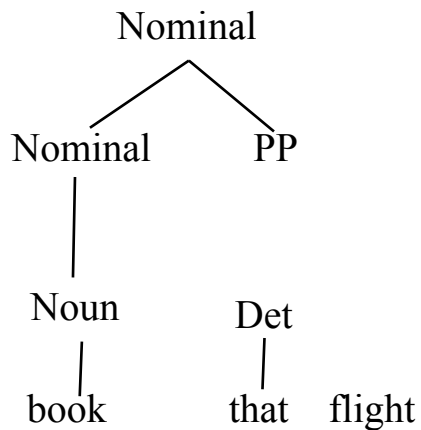
## Grammar

$S \rightarrow NP VP$   
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# Bottom Up Parsing



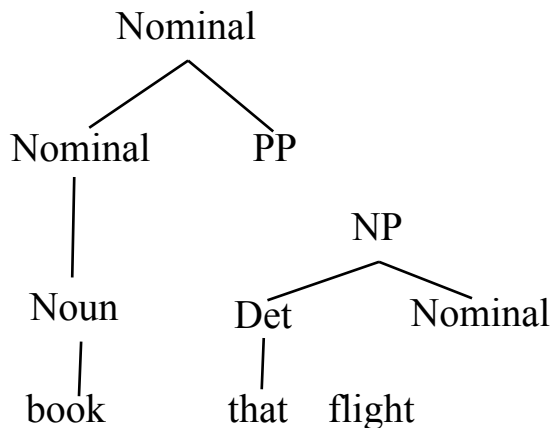
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# Bottom Up Parsing



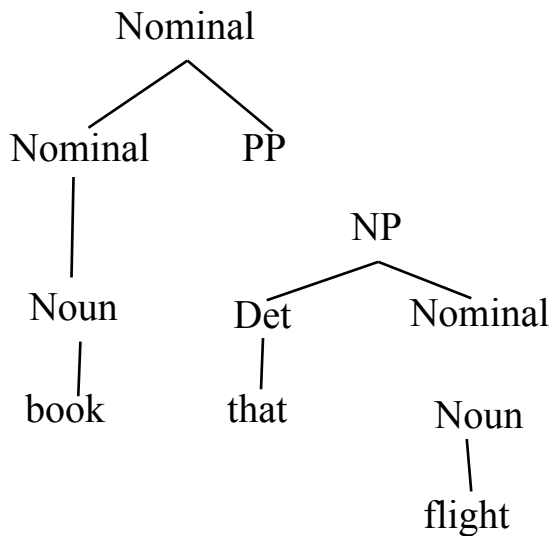
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# Bottom Up Parsing



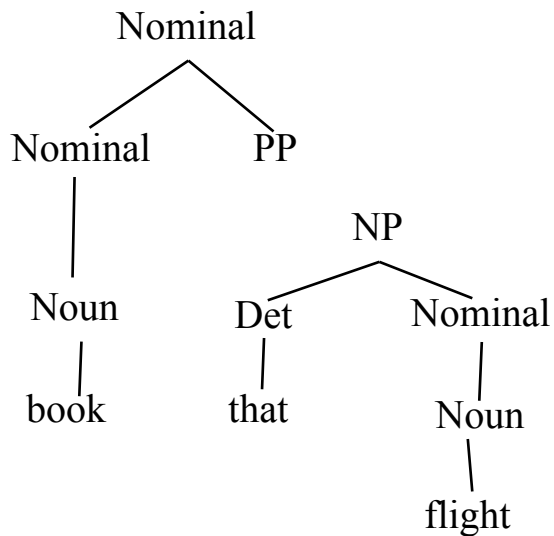
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$S \rightarrow NP VP$   
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# Bottom Up Parsing



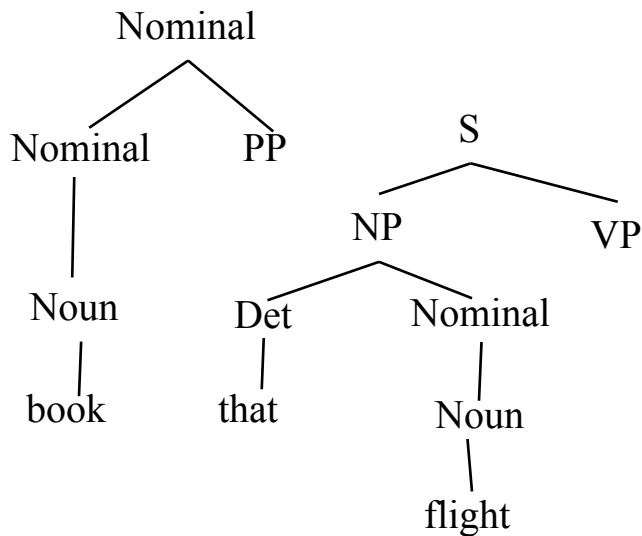
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# Bottom Up Parsing



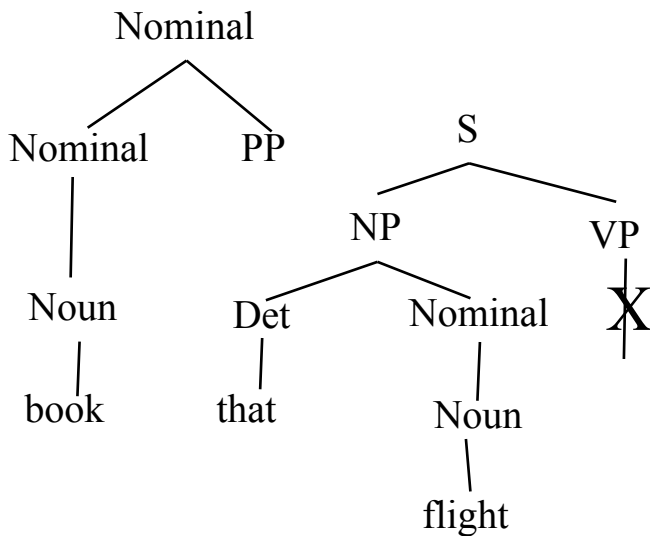
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# Bottom Up Parsing



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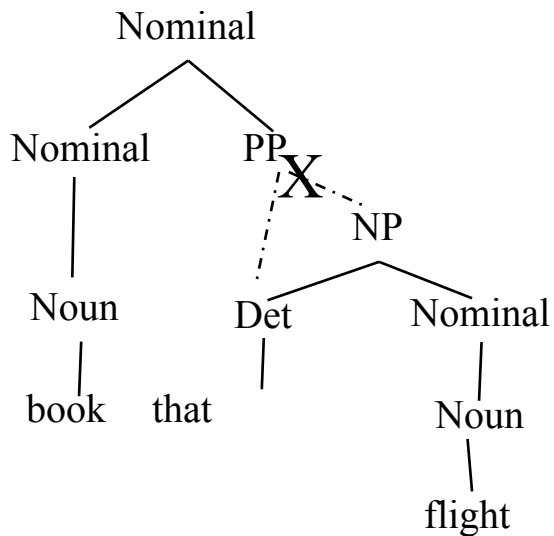
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# Bottom Up Parsing



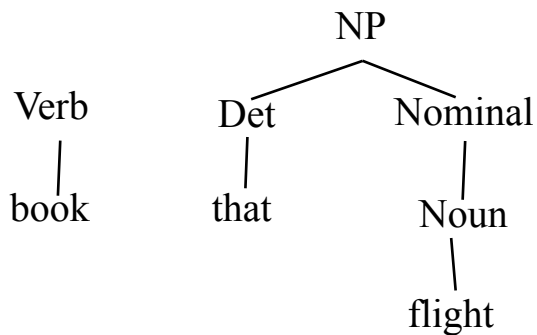
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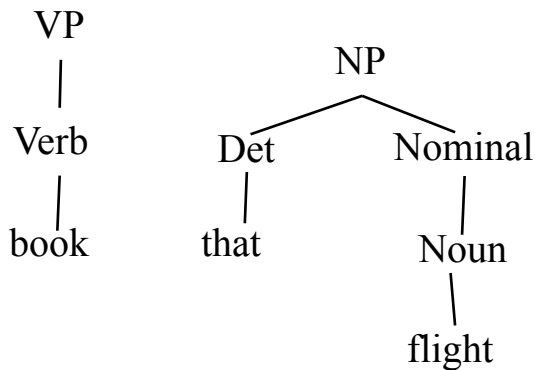
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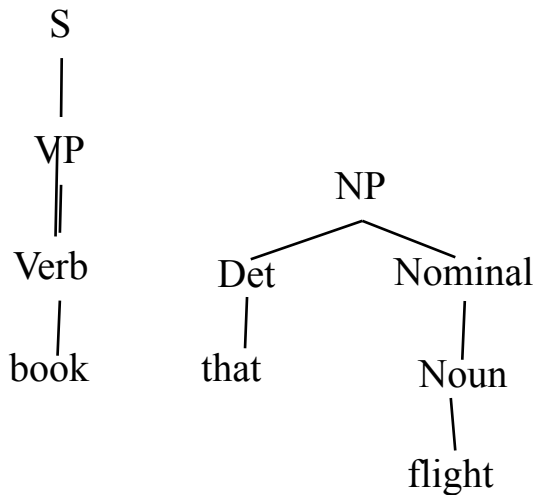
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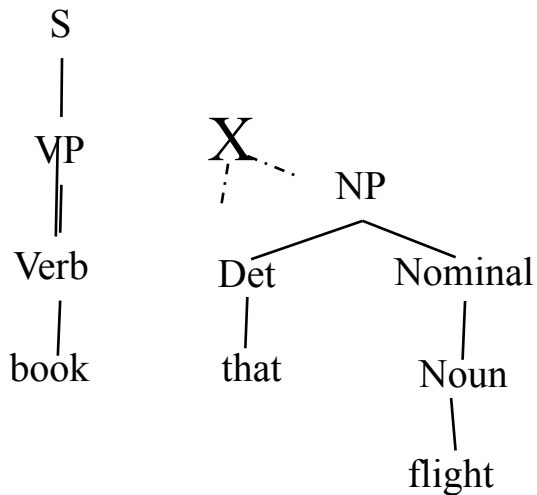
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 $S \rightarrow VP$   
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# Bottom Up Parsing



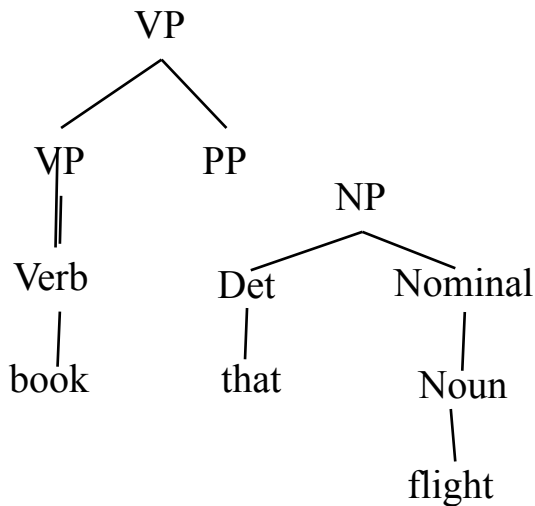
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# Bottom Up Parsing



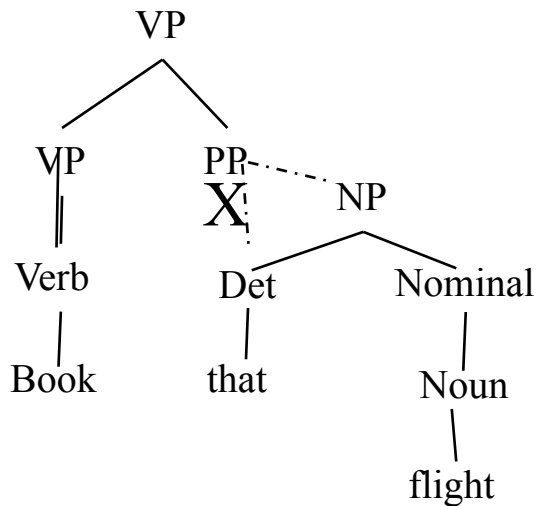
## Grammar

S → NP VP  
S → Aux NP VP  
S → VP  
NP → Pronoun  
NP → Proper-Noun  
NP → Det Nominal  
Nominal → Noun  
Nominal → Nominal Noun  
Nominal → Nominal PP  
VP → Verb  
VP → Verb NP  
VP → VP PP  
PP → Prep NP

## Lexicon

Det → the | that  
Noun → book | flight  
Verb → book  
Pronoun → I | he | she | me  
Proper-Noun → Houston | NWA  
Aux → does  
Prep → from | to

# Bottom Up Parsing



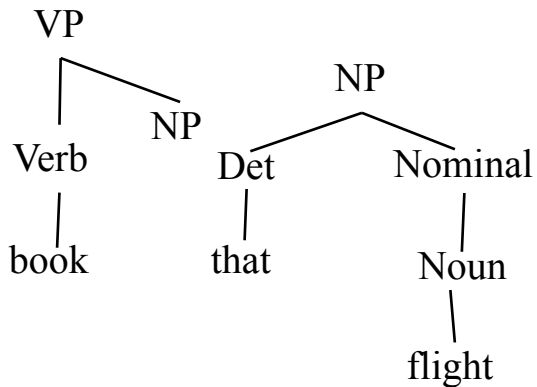
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$S \rightarrow NP VP$   
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# Bottom Up Parsing



## Grammar

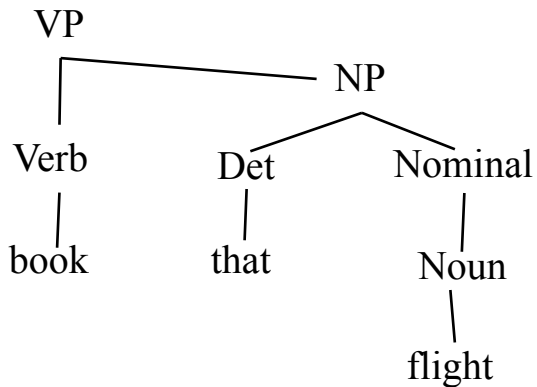
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 $Aux \rightarrow does$   
 $Prep \rightarrow from \mid to$



# Bottom Up Parsing



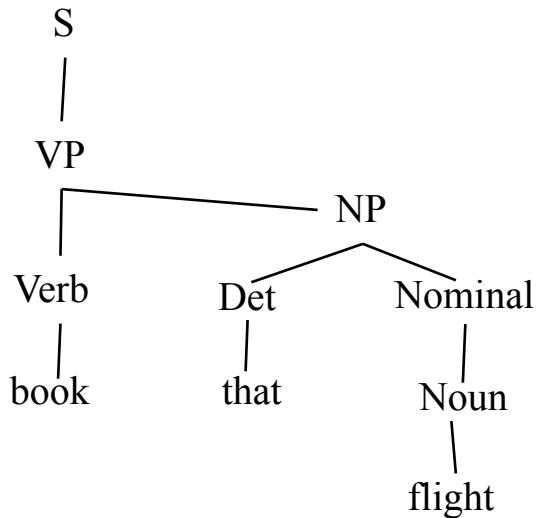
## Grammar

$S \rightarrow NP VP$   
 $S \rightarrow Aux NP VP$   
 $S \rightarrow VP$   
 $NP \rightarrow Pronoun$   
 $NP \rightarrow Proper-Noun$   
 $NP \rightarrow Det Nominal$   
 $Nominal \rightarrow Noun$   
 $Nominal \rightarrow Nominal Noun$   
 $Nominal \rightarrow Nominal PP$   
 $VP \rightarrow Verb$   
 $VP \rightarrow Verb NP$   
 $VP \rightarrow VP PP$   
 $PP \rightarrow Prep NP$

## Lexicon

$Det \rightarrow the \mid that$   
 $Noun \rightarrow book \mid flight$   
 $Verb \rightarrow book$   
 $Pronoun \rightarrow I \mid he \mid she \mid me$   
 $Proper-Noun \rightarrow Houston \mid NWA$   
 $Aux \rightarrow does$   
 $Prep \rightarrow from \mid to$

# Bottom Up Parsing



## Grammar

$S \rightarrow NP VP$   
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 $Nominal \rightarrow Nominal PP$   
 $VP \rightarrow Verb$   
 $VP \rightarrow Verb NP$   
 $VP \rightarrow VP PP$   
 $PP \rightarrow Prep NP$

## Lexicon

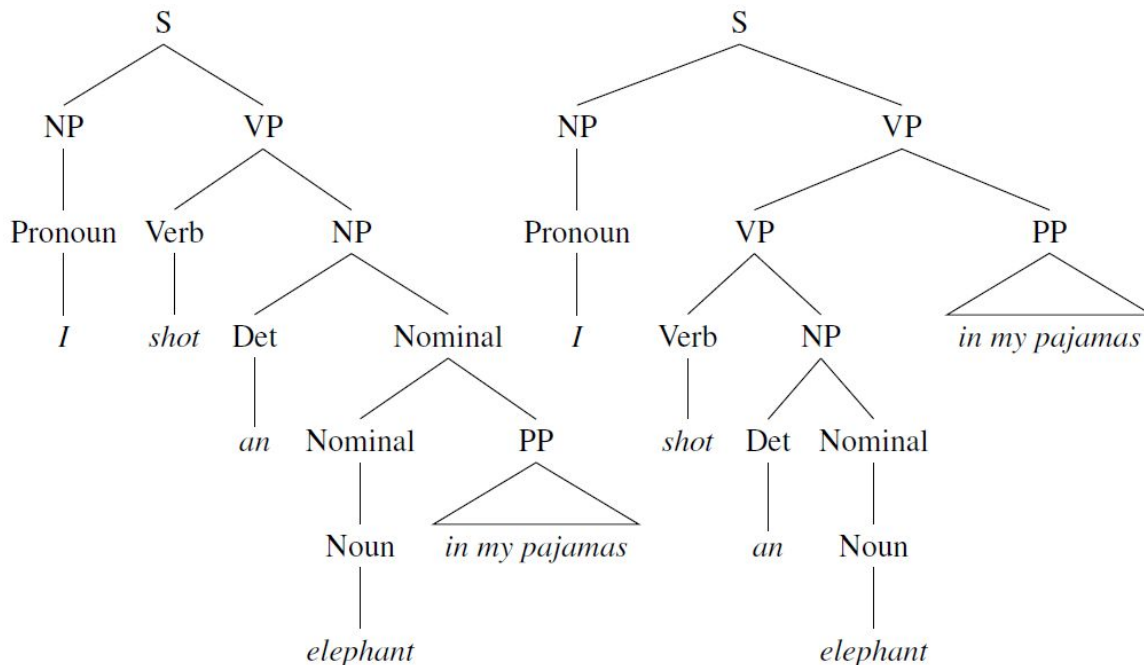
$Det \rightarrow the \mid that$   
 $Noun \rightarrow book \mid flight$   
 $Verb \rightarrow book$   
 $Pronoun \rightarrow I \mid he \mid she \mid me$   
 $Proper-Noun \rightarrow Houston \mid NWA$   
 $Aux \rightarrow does$   
 $Prep \rightarrow from \mid to$

# Top Down vs. Bottom Up

- Top down never explores options that will not lead to a full parse for the current sentence, but can explore many options that never connect to the actual sentence.
- Bottom up never explores options that do not connect to the actual sentence but can explore options that can never lead to a full parse.
- Relative amounts of wasted search depend on how much the grammar branches in each direction.

# Structural Ambiguity

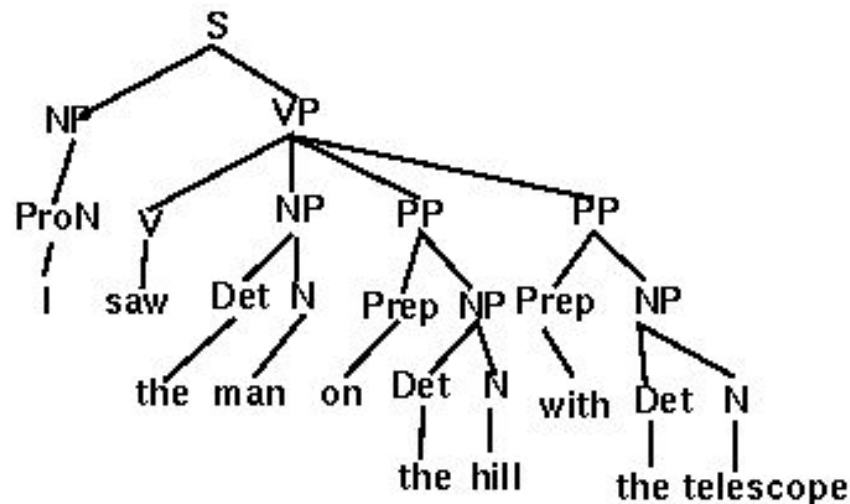
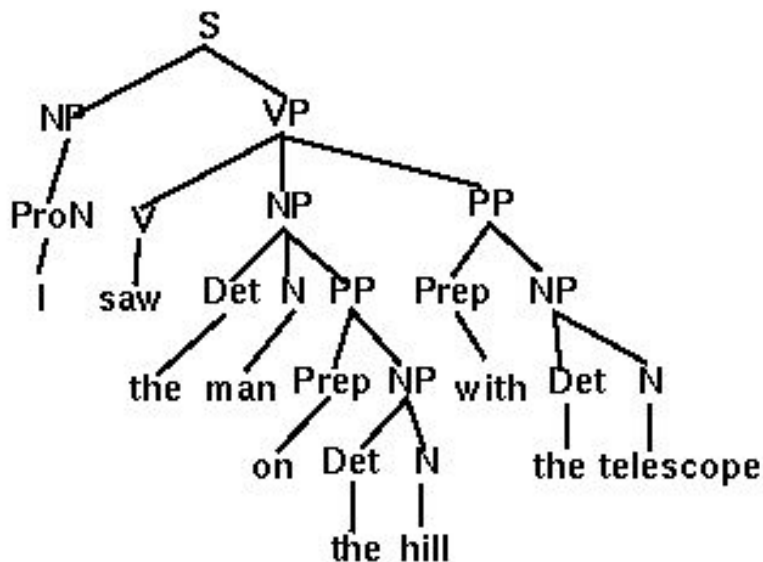
- “I shot an elephant in my pyjamas”



Grammar
$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$
$S \rightarrow VP$
$NP \rightarrow Pronoun$
$NP \rightarrow Proper-Noun$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow Noun$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$
$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

# Structural Ambiguity

- “I saw the man on the hill with telescope”



# Syntactic Disambiguation

- The process of choosing a single correct parse from the multitude of possible parses is called **syntactic disambiguation**
- Effective disambiguation algorithms require statistical, semantic, and contextual knowledge sources
- How to efficiently handle structural ambiguities?

# CYK Parsing : A Dynamic Programming Approach

- Requires the grammar to be in **Chomsky Normal Form (CNF)**
  - restricted to rules of the form  $A \rightarrow BC$  or  $A \rightarrow w$
- CYK(**Cocke–Younger–Kasami**) Algorithm
  - Convert CFG to CNF
  - Construct a triangular table
  - Check if  $X_{1,n}$  contains start symbol  $S$
- Time Complexity
  - $O(n^3 \cdot |G|)$
  - $n$  : length of string
  - $|G|$  : size of the CNF Grammar

$X_{1,5}$				
$X_{1,4}$	$X_{2,5}$			
$X_{1,3}$	$X_{2,4}$	$X_{3,5}$		
$X_{1,2}$	$X_{2,3}$	$X_{3,4}$	$X_{4,5}$	
$X_{1,1}$	$X_{2,2}$	$X_{3,3}$	$X_{4,4}$	$X_{5,5}$
$w_1$	$w_2$	$w_3$	$w_4$	$w_5$

# CKY parsing example

1. S -> NP VP
2. NP -> Det N
3. NP -> NP PP
4. VP -> V NP
5. VP -> VP PP
6. PP -> P NP
7. NP -> Tom
8. N -> Ball
9. N -> Net
10. V -> Net
11. V -> Sent
12. P -> to
13. Det -> The
14. Det -> a

Tom sent the ball to the net

Tom (1)	Sent (2)	The (3)	Ball (4)	To (5)	The (6)	Net (7)



# Statistical Constituency Parsing

- Can CYK Algorithm resolve ambiguity? **NO**
  - It can only represent ambiguities
- How to resolve ambiguity?
  - Compute the probability of each interpretation and choose the most probable interpretation
  - Need a **probabilistic parser**

# Pseudocode

```
function CKY-PARSE(words, grammar) returns table

  for  $j \leftarrow$  from 1 to LENGTH(words) do
    for all  $\{A \mid A \rightarrow \text{words}[j] \in \text{grammar}\}$ 
       $\text{table}[j-1, j] \leftarrow \text{table}[j-1, j] \cup A$ 
    for  $i \leftarrow$  from  $j-2$  downto 0 do
      for  $k \leftarrow i+1$  to  $j-1$  do
        for all  $\{A \mid A \rightarrow BC \in \text{grammar} \text{ and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$ 
           $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$ 
```

```

function PROBABILISTIC-CKY(words, grammar) returns most probable parse
                                                    and its probability

for  $j \leftarrow$  from 1 to LENGTH(words) do
    for all  $\{ A \mid A \rightarrow \text{words}[j] \in \text{grammar} \}$ 
         $\text{table}[j-1, j, A] \leftarrow P(A \rightarrow \text{words}[j])$ 
    for  $i \leftarrow$  from  $j-2$  downto 0 do
        for  $k \leftarrow i+1$  to  $j-1$  do
            for all  $\{ A \mid A \rightarrow BC \in \text{grammar},$ 
                and  $\text{table}[i, k, B] > 0$  and  $\text{table}[k, j, C] > 0 \}$ 
                if  $(\text{table}[i, j, A] < P(A \rightarrow BC) \times \text{table}[i, k, B] \times \text{table}[k, j, C])$  then
                     $\text{table}[i, j, A] \leftarrow P(A \rightarrow BC) \times \text{table}[i, k, B] \times \text{table}[k, j, C]$ 
                     $\text{back}[i, j, A] \leftarrow \{k, B, C\}$ 
    return BUILD_TREE( $\text{back}[1, \text{LENGTH}(\text{words}), S]$ ),  $\text{table}[1, \text{LENGTH}(\text{words}), S]$ 

```

# Probabilistic Context-Free Grammars (PCFG)

- Probabilistic augmentation of context-free grammars
- Differs from CFG by augmenting each rule in  $R$  with a conditional probability
  - $\alpha \rightarrow \beta$  [ $p$ ]
  - $p$  is the conditional probability of  $\beta$  given  $\alpha$
  - Defined as  $P(\alpha \rightarrow \beta)$  or  $P(\alpha \rightarrow \beta | \alpha)$
  - $\sum_i P(\alpha \rightarrow \beta_i) = 1$
- How to learn the probabilities?

$$P(\alpha \rightarrow \beta | \alpha) = \frac{\text{Count}(\alpha \rightarrow \beta)}{\sum_{\gamma} \text{Count}(\alpha \rightarrow \gamma)} = \frac{\text{Count}(\alpha \rightarrow \beta)}{\text{Count}(\alpha)}$$

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	$\mid meal [.05] \mid money [.05]$
$NP \rightarrow Pronoun$	[.35]	$\mid flight [.40] \mid dinner [.10]$
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book [.30] \mid include [.30]$
$NP \rightarrow Det Nominal$	[.20]	$\mid prefer [.40]$
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I [.40] \mid she [.05]$
$Nominal \rightarrow Noun$	[.75]	$\mid me [.15] \mid you [.40]$
$Nominal \rightarrow Nominal Noun$	[.20]	$Proper-Noun \rightarrow Houston [.60]$
$Nominal \rightarrow Nominal PP$	[.05]	$\mid NWA [.40]$
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does [.60] \mid can [.40]$
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from [.30] \mid to [.30]$
$VP \rightarrow Verb NP PP$	[.10]	$\mid on [.20] \mid near [.15]$
$VP \rightarrow Verb PP$	[.15]	$\mid through [.05]$
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	

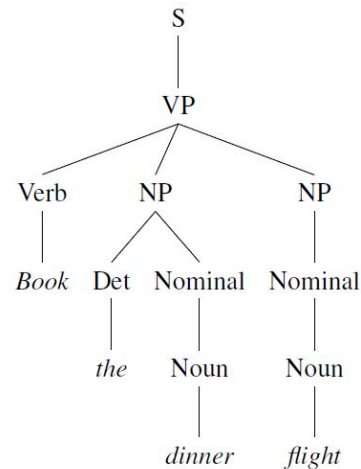
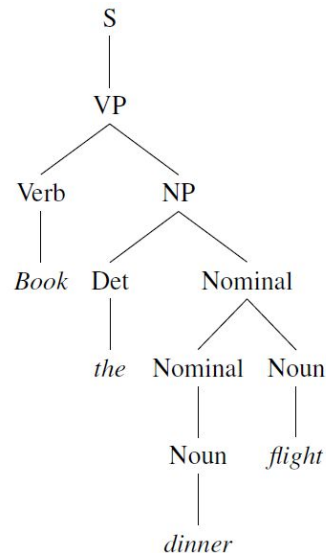
# PCFGs for disambiguation

Choose the parse tree with highest probability

Rules			Rules		
Rules		P	Rules		P
S	→ VP	.05	S	→ VP	.05
VP	→ Verb NP	.20	VP	→ Verb NP NP	.10
NP	→ Det Nominal	.20	NP	→ Det Nominal	.20
Nominal	→ Nominal Noun	.20	NP	→ Nominal	.15
Nominal	→ Noun	.75	Nominal	→ Noun	.75
Verb	→ book	.30	Nominal	→ Noun	.75
Det	→ the	.60	Verb	→ book	.30
Noun	→ dinner	.10	Det	→ the	.60
Noun	→ flight	.40	Noun	→ dinner	.10
			Noun	→ flight	.40

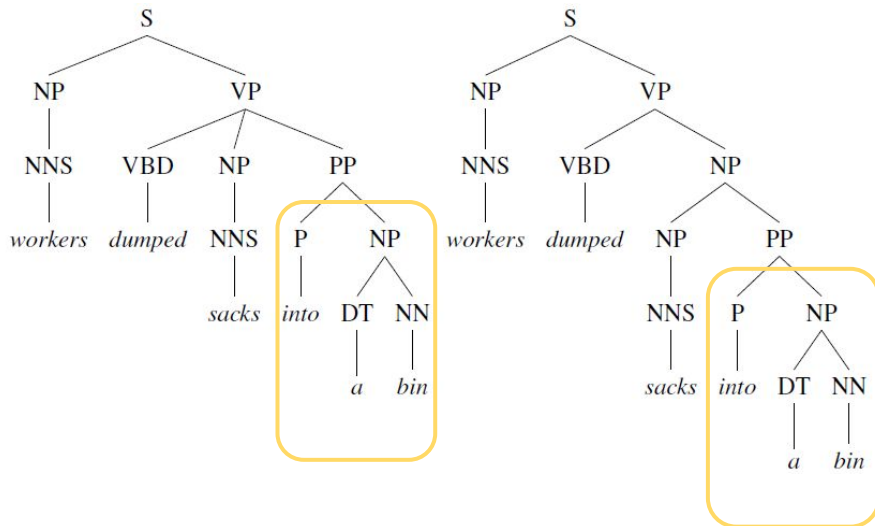
$$P(T_{left}) = .05 * .20 * .20 * .20 * .75 * .30 * .60 * .10 * .40 = 2.2 \times 10^{-6}$$

$$P(T_{right}) = .05 * .10 * .20 * .15 * .75 * .75 * .30 * .60 * .10 * .40 = 6.1 \times 10^{-7}$$



# Problems with PCFG

- Poor Independence assumption
  - Expansion of a non-terminal is independent of the context
  - Expansion can depend on the location of the node in the parse tree
- Lack of sensitivity to Lexical dependencies
  - Example : Prepositional phrase(PP) attachment
  - Solution : **Probabilistic Lexicalized CFGs**

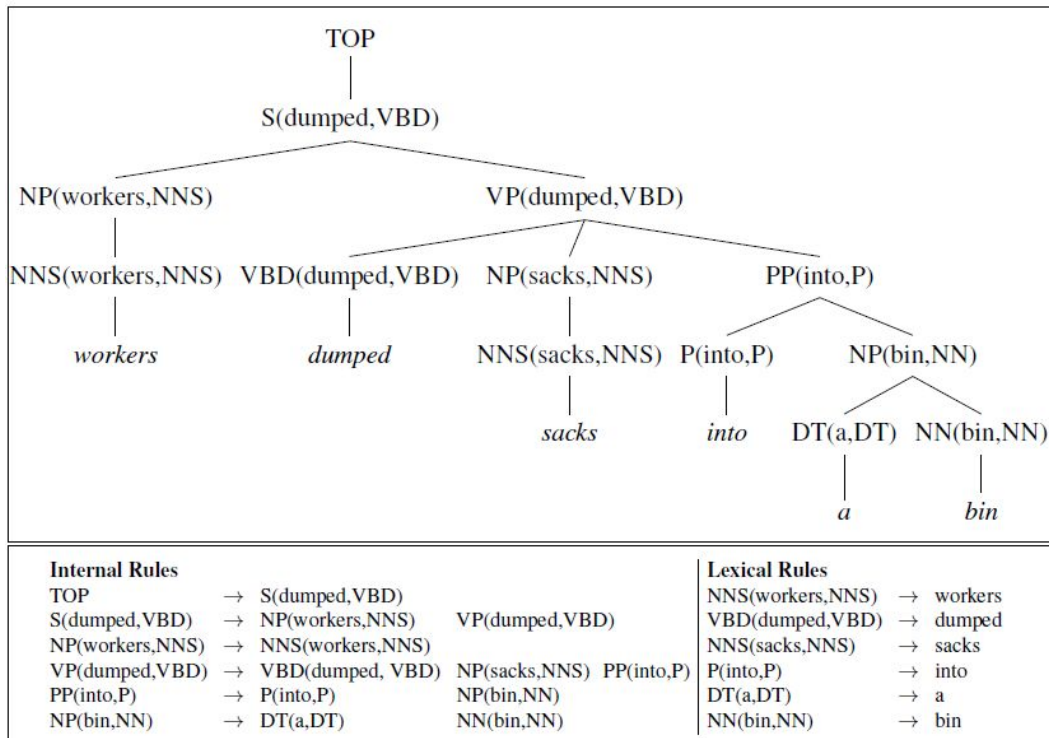


Two possible parse trees for a **PP attachment ambiguity**

- The left parse is the sensible one where "into a bin" describes the resulting location of the sacks
- In the right incorrect parse, the sacks to be dumped are the ones which are already "into a bin"

# Probabilistic Lexicalised CFG

- Each non-terminal grammar in the tree is annotated
  - With **Lexical head** and **Part-of-speech tags of the head word**
- Parsing Method
  - Collins Parser



# Parser Evaluation

- Precision

$$\text{labeled precision} = \frac{\# \text{ of correct constituents in hypothesis parse of } s}{\# \text{ of total constituents in hypothesis parse of } s}$$

- Recall

$$\text{labeled recall} = \frac{\# \text{ of correct constituents in hypothesis parse of } s}{\# \text{ of correct constituents in reference parse of } s}$$

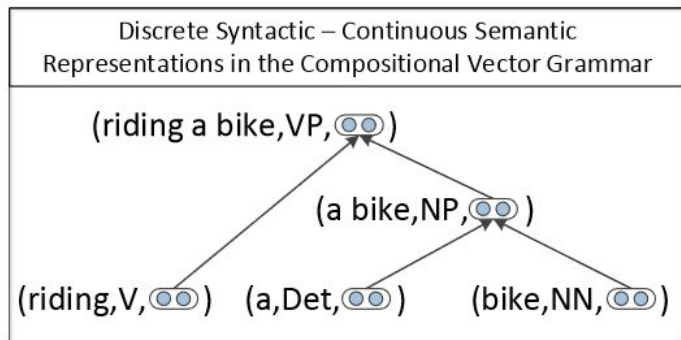
- F-Measure

$$F_{\beta} = \frac{(\beta^2 + 1)PR}{\beta^2 P + R}$$

- $\beta > 1$  favor recall
- $\beta < 1$  favor precision



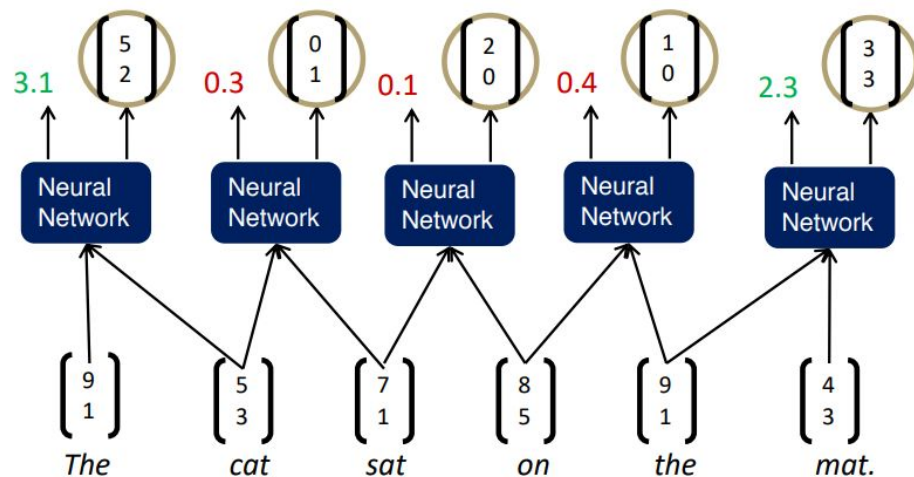
# Scoring and selecting the constituents



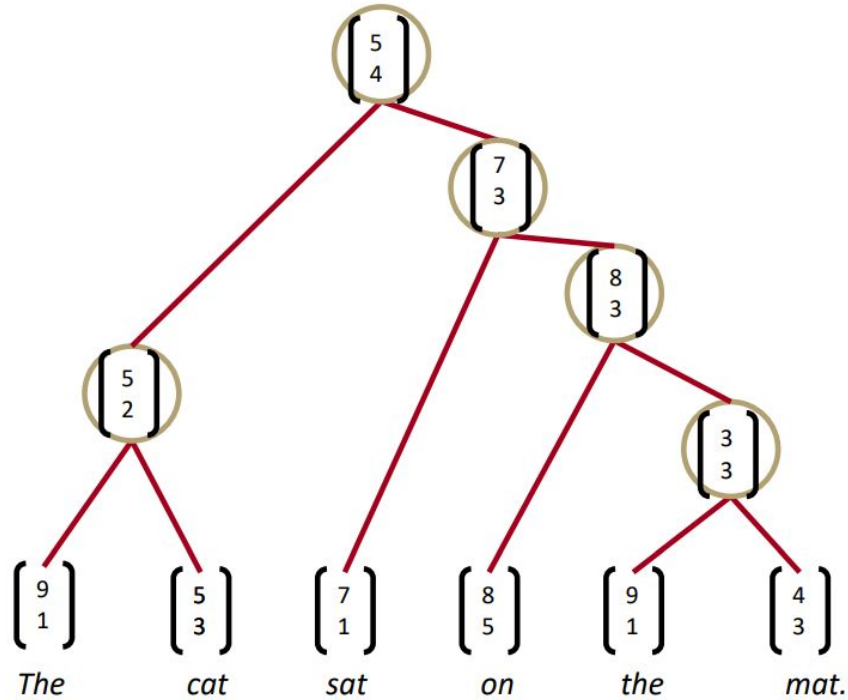
Dimensionality of  $W_{A,B}$ ?

- Parse tree construction in recursive manner
- The next two nodes to be combined is decided based on greedy choice
  - For each pair of consecutive nodes, find a score
  - Pick the pair with highest score
  - Merge them and replace the two constituent nodes with this merged nodes
- Scoring
  - Based on the representations of the nodes, their labels and PCFG probability
- Score
  - $p_{X,a,b} = f \left( W_{A,B} \begin{bmatrix} a \\ b \end{bmatrix} + bias_{A,B} \right) + P(X \rightarrow AB)$

# Parsing with Recursive NN (greedily)



# Parsing with Recursive NN (greedily)



# Partial Parsing : Chunking

- Not all tasks require complete parse trees
  - Information extraction
- **Chunking** is the process of identifying and classifying the **flat, non-overlapping segments** of a sentence
- Objective of Chunking
  - **Segmentation**
    - Finding the non-overlapping extents of the chunks
    - Some input words may not be part of any chunk
  - **Labeling**
    - Assigning the correct tag to the discovered chunks
- Example
  - [NP The old gentleman] from [NP the neighboring village] is an amazing [NP artist ].

# More examples of chunking

- The morning flight from Denver has arrived

\_\_\_\_\_

NP PP NP VP

- The morning flight from Denver has arrived

B\_NP I\_NP I\_NP B\_PP B\_NP B\_VP I\_VP

- Let the equation of the circle be  $ax^2 + by^2 = c$ .

\_\_\_\_\_

M

- The *sigmoid* activation is applied on the output  $y = Wx + b$  of the final layer

O\_M B\_M O\_M O\_M O\_M O\_M O\_M O\_M B\_M I\_M I\_M I\_M I\_M O\_M O\_M O\_M O\_M

# Chunking Model

- IOB Tagging
  - **B** : Beginning of a chunk
  - **I** : Inside of a chunk
  - **O** : Outside of any chunk
- Chunking reduces to tagging task
  - Can use any supervised classification model from ML
- Example features:
  - $w_i, w_{i-1}, w_{i+1}, \text{POS}(w_i), \text{POS}(w_{i-1}), \text{POS}(w_{i+1}),$  punctuations, beginning-of-sentence?, end-of-sentence? Etc.

