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Improving cooperative pathfinding using a path oracle

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Abstract

The order picking process is the number one expense in the operating cost of warehouse systems. This project will look at *part-to-picker*, a method of order picking where orders are retrieved and delivered to a number of picking areas located around the warehouse. Previous research has improved on multi-agent path finding (MAPF) algorithms but mostly overlooked the potential benefits gained by configuring the warehouse layout. Here, we will be exploring Kiva systems a part-to-picker system which uses autonomous vehicles and mobile storage. Our focus is to explore a number of adjustments and additions which we expect will greatly affect how we design warehouse layouts. These include: introducing an intermediate dropping zone, optimizing order processing and adding the capability for robots to maneuver under storage pods. The results of this project will help identify how we should position storage and picking stations in a warehouse. Additionally, we will be looking at developing a MAPF method which uses a pre-computed path oracle.

Keywords

Cooperative Multi-agent pathfinding, Kiva systems

1 Introduction

Order picking is a process in warehouse systems whereby products are retrieved from storage to satisfy incoming customer orders. This process has been identified by [De Koster et al. \(2007\)](#) as the most expensive process in operating a warehouse, estimated to take 55% of the warehouse operating cost.

Here we look at a method of order picking known as part-to-picker systems. Part-to-picker systems contain multiple picking stations located around the warehouse. Products are brought to picking stations where workers will manually pick and process the product. One of the disadvantages of part-to-picker systems is that there will be some downtime at the picking stations while waiting for an order to be delivered. To solve this, these systems often use an automated storage and retrieval system (AS/RS). [AutoStore \(2015\)](#) is a recent part-to-picker system where products are organized in a grid of stacked bins. Robots move around the top of the grid, lifting bins and delivering them to picking areas. Benefits of the AutoStore system include high storage density and expansion capability. While not much literature is published about the specifics of AutoStore, we suspect the major downsides are: slow, expensive order retrieval as well as high infrastructure and maintenance costs.

In this project, we look at Kiva Systems (now known as Amazon Robotics). In Kiva systems, products are stored in mobile shelves known as storage pods. Robots known as drive units are responsible for retrieving and delivering storage pods to picking stations. A human worker is stationed at each picking station who picks the item off the pod before processing it (Fig ??). Once the pod has been processed, the drive unit will return the pod to an appropriate location in the warehouse.

Kiva systems do not require a complex infrastructure to operate, a warehouse needs only a suitable number of storage pods, picking stations and drive units to operate. As long as the warehouse has space, more robots, pods or stations can be easily be added to the system to satisfy the incoming flow of customer orders. When a drive unit malfunctions it can be easily accessed and replaced. In summary, the main benefits of Kiva systems are their low initial and maintenance costs and their rapid deployment and flexibility ([Wurman et al. \(2008\)](#)).

1.1 Research questions

We aim to explore two areas of Kiva systems, the layout and MAPF. These can be summarized in the following questions:

1. How will the adjustments and additions below affect our decision when it comes to configuring the warehouse layout?
 - Adding an intermediate zone where drive units may drop off storage pods
 - Adding the capability for drive units to maneuver under storage pods
 - Implementing an optimized order process
2. How much faster will the MAPF search run by pre-computing paths and storing them in a path oracle?

2 Background

In Kiva systems, we face a multi-agent pathfinding (MAPF) problem. MAPF aims to find a path for each agent to their goal while ensuring that no path conflicts with another. MAPF has usage in video games, robotics (Bennewitz et al. (2002)), search and rescue (Konolige et al. (2006)) and warehouse applications. When analyzing the efficiency of a MAPF algorithm we generally aim to reduce the makespan of the system. Additionally, in Kiva systems we want to reduce the downtime of picking stations.

Finding an optimal solution in MAPF is an NP-hard problem (Yu and LaValle (2013)) and mostly has found usage in systems containing a small number agents. This is not an option as Kiva systems deal with hundreds of agents, for example the Office Supply company, Staples uses 500 robots in their $30000m^2$ center (Guizzo (2008)). Here we look at finding a bounded suboptimal solution and this has been explored in Kiva systems by (Cohen and Koenig (2016)).

To improve MAPF, generally methods are created to simplify the problem, Cohen and Koenig (2016) define user-provided highways to help guide agents towards a specific direction, greatly reducing the chance of path collisions. Wilt and Botea (2014) identifies bottlenecks in the environment and assigns a controller which handles agents who want to pass through the bottleneck, simplifying agent behaviour in high collision zones. Another common technique is grouping agents into teams. Ma and Koenig (2016) splits agents into teams of 5 and presents a Conflict-Based Min-Cost-Flow algorithm which and shows that they can achieve a correct, complete and optimal solution.

Specific to the process of order picking, we will look at the method of order processing. Take an example where products of the same type are grouped together in a warehouse. If a large order of one product comes in, the agents will all try to find a path to this one area and create many collisions in the MAPF. We want the goal locations for our drive units to be spread evenly around the warehouse and order processing allows this by looking at two areas. Firstly, by evenly distributing products around the warehouse. If we place products of the same type across many different row around the warehouse, a large order of one product will be no issue. Secondly, is sequencing of incoming orders. Instead of processing the large orders of one product sequentially, we have some flexibility to interlace this large order with other orders which we know we will need to process. Essentially, we can move the mobile storage pods as well adjust the incoming ordering sequence to benefit the MAPF. Boysen et al. (2017) looks at both these aspects in unison and found that with optimized order processing, only half the units are required to provide the supply given by a non-optimized system.

2.1 Comparing search algorithms

- Completeness
- Solution quality - Optimal, bounded suboptimal, suboptimal
- Centralized - **A centralised method incorporates a global decision maker to plan paths for all units simultaneously**
- Time complexity
- Anonymous - In TAPF we put agents in groups. The group may have n agents moving to n targets, anonymous means we don't care which agent moves to which target
 - Non-Polynomial (NP) / Intractable
 - Polynomial / Tractable

Centralized - Complete

Decentralized - Incomplete.

2.2 tractable

QUOTES

- In global search approaches, the entire set of agents is treated as a single entity and paths are found for all agents simultaneously. Alternatively, in decoupled approaches paths are found for each agent one at a time, and information about the paths of other agents is used to ensure that no paths conflict

END QUOTES

2.3 Cooperative Multi-agent pathfinding

When looking at multi-agent pathfinding, we will be first considering whether it is centralized. A centralized search usually indicates

2.3.1 WHCA*

Windowed Hierarchical Cooperative A* uses a Reservation table

2.3.2 FAR

[Wang et al. \(2008\)](#)

2.3.3 MAPP

For each problem instance, MAPP systematically identifies a set of units, which can contain all units in the instance, that are guaranteed to be solved within low-polynomial time

Based on sliding tile puzzle. Always tries to keep a blank on an alternative path.

[Wang and Botea \(2011\)](#)

2.3.4 CBS

2.4 Summary

2.5 Further research

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