## School of Computer Science (BICA) Monash University



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## Improving cooperative pathfinding using a path oracle

Phillip Wong

Supervisors: Daniel Harabor,

Pierre Le Bodic

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