

# Discrete Structures

IIIT Hyderabad

Monsoon 2020

*Tutorial 3*

September 23, 2020

## 1 Instructions

## 2 Questions

- Question 0
- Question 1
- Question 2

We will be having a test quiz to increase your familiarity with Moodle. This is NOT GRADED. You don't need to mail them to sir in case you have not submitted.

- 1 Go to the "Tutorial 3 Submission" under the **Tutorials** Section on Moodle.
- 2 A pdf named "Tutorial 3" would be there in the portal.
- 3 Please download it and solve the questions **1, 2.1 and 2.2** . You **may not** submit Question 0.
- 4 Upload your scanned answers by **1:25PM**. We would start discussing their solutions by then.

# Question 0

**0.1** In the following condition, when is it equal?

$$(A \times B) \cup (C \times D) \subseteq (A \cup C) \times (B \cup D)$$

**0.2** Find the number of primes between 40 - 100 using PRT.

# Question 1

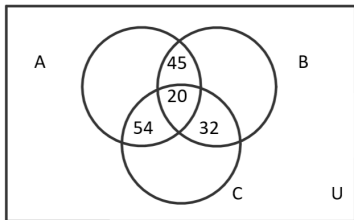
Simplify the following -

①  $(A - (B \cup C)) \cap ((B \cap C) - A)$

②  $(A \cap B') \cup (A' \cap B) \cup (A' \cap B')$

## Question 2

**2.1**  $A$  is the set of people who go to resort area for vacation,  $B$  is the set of people who take cruise for vacation,  $C$  is the set of people who go to national park for vacation. Suppose  $|A| = 150$ ,  $|B| = 100$  and  $|C| = 300$



- a. How many people only go to a resort area for vacation?
- b. How many people only take a cruise for vacation?
- c. How many people only go to national park for vacation?
- d. How many people either go to a resort area or take a cruise for vacation but not national park?
- e. How many people use any of the 3 methods to take a vacation?

## Question 2 (contd.)

**2.2** Observe the values of the table and find the number of students who:

		Pudding		
		Chocolate	Tapioca	Neither
Ice Cream	Vanilla	68	53	12
	Strawberry	59	48	9
	Neither	23	21	7
	Total	150	122	28

**a.** Like strawberry ice cream and tapioca pudding

**b.** Do not like pudding

**c.** Like at least one of the ice cream flavours

**d.** Like neither ice cream nor pudding

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**2.3** Mark the following as true or false:

**a.**  $26 \in \mathbb{Z}$

**b.**  $-5 \in \mathbb{N}$

**c.**  $\sqrt{2} \notin \mathbb{Q} \cap \mathbb{R}$

**d.**  $\mathbb{Z} \cup \mathbb{Q} = \mathbb{R}$

**e.**  $\mathbb{R} \cap \mathbb{C} = \mathbb{R}$

Any doubts ?

- ① If  $B$  is finite set and  $A \subseteq B$  such that  $|A| = |B|$ , then prove, without using Venn-Euler's diagram, that  $A = B$ .
- ② In a hostly fought battle at least 70% of the combatants lost an eye, at least 75% an ear, at least 80% an arm and at least 85% a leg. What is the least number of combatants who lost all four members?