

Overview : Camera Calibration :- Shree Nayar \rightarrow First Principles of CV \rightarrow Youtube.
Linear Camera Model

One of the key problems in Computer Vision is recovering the 3 dimensional structure of a scene from its images. Image to full metric reconstruction requires 2 things:-

- 1) Position & Orientation of the camera w.r.t. world co-ordinate frame \rightarrow external parameters.
- 2) How the camera maps the perspective projection points in the world onto its image plane. \rightarrow Internal parameters such as focal length.

Determining the external & internal parameters of the camera is what is referred to as camera calibration.

Method to find a camera's internal & external parameters.

- 1) We need a model \rightarrow Linear Camera Model

Single matrix called Projection Matrix.

- 2) Camera Calibration

- 3) Extracting Intrinsic & Extrinsic Matrices.

- 4) Example Application: Simple Stereo.

Intrinsic Matrix $K = \begin{bmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}$ $f_x, f_y \rightarrow$ focal length in pixels in x & y direction.
 $c_x, c_y \rightarrow$ Image Center in Pixels (principal pt)
 $0s \& 1 \rightarrow$ Homogenous co-ordinates
 \rightarrow Miolth video \rightarrow Youtube

Image Plane

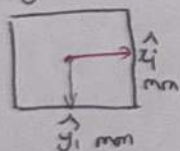
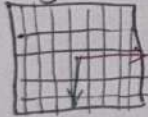


Image Sensor



v (pixels)

$$u = m_x f_x \frac{z_c}{z_c} + c_x$$

$$v = m_y f_y \frac{z_c}{z_c} + c_y$$

$$m_x = \frac{\text{image width (px)}}{\text{sensor width (mm)}}$$

$$m_y = \frac{\text{image height (px)}}{\text{sensor height (mm)}}$$

Camera = iPhone 16 Pro Max, focal length in mm \rightarrow 6.9mm, Image Resolution \Rightarrow

5712 x 4284 px Aperture = f/1.78

24 MP iPhone sensor size \rightarrow 9.6mm x 7.2mm

$f_x = f m_x$ & $f_y = f m_y$ i.e. focal length in pixels. \rightarrow Linear Camera Model \rightarrow YT

$$\therefore f_x = \frac{6.9}{9.6} \times 5712 = 0.71875 \times 5712 = 4108 \text{ pixels}$$

$$f_y = \left(\frac{6.9}{9.6} \right) \times 4284 = 0.71875 \times 4284 = 3077 \text{ pixels}$$

$$c_x = \frac{\text{image width}}{2} = \frac{5712}{2} = 2856$$

$$c_y = \frac{\text{image height}}{2} = \frac{4284}{2} = 2142$$

Theoretical
 \therefore Calculated
 K

$$K = \begin{bmatrix} 4108 & 0 & 2856 \\ 0 & 3077 & 2142 \\ 0 & 0 & 1 \end{bmatrix}$$

\therefore Practical
 K
Observed

$$K = \begin{bmatrix} 3980.8 & 0 & 2785.4 \\ 0 & 3974.4 & 2140.38 \\ 0 & 0 & 1 \end{bmatrix}$$



Add a Caption



Look Up **American Wirehair** >

Wednesday • Jun 18, 2025 • 3:48 PM

[Adjust](#)

IMG_0837

Apple iPhone 16 Pro Max

HEIF

Fusion Camera — 24 mm $f1.78$

24 MP • 4284 × 5712 • 3.2 MB

STANDARD

ISO800

24mm

0ev

$f1.78$

1/33s

[Add a location...](#)



```

import numpy as np
import cv2
import glob
import os
import matplotlib.pyplot as plt
%matplotlib inline

# Chessboard parameters
chessboard_size = (8, 5)
square_size = 3.0 # Square 3.0 cm

# Prepare object points
objp = np.zeros((chessboard_size[0] * chessboard_size[1], 3),
np.float32)
objp[:, :2] = np.mgrid[0:chessboard_size[0],
0:chessboard_size[1]].T.reshape(-1, 2)
objp *= square_size

# Arrays to store object points and image points
objpoints = []
imgpoints = []

# Image loading
image_path = r'C:\Users\vikra\Downloads\Iphone_Images\newdata\*.jpg'
images = glob.glob(image_path)
print(f"Found {len(images)} image(s).")

plt.figure(figsize=(15, 10))

for idx, fname in enumerate(images):
    print(f"\n[{idx + 1}/{len(images)}] Processing:
{os.path.basename(fname)}")

    img = cv2.imread(fname)
    if img is None:
        print(" x Could not read image.")
        continue

    gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)

    # Detection flags
    flags = cv2.CALIB_CB_ADAPTIVE_THRESH +
cv2.CALIB_CB_NORMALIZE_IMAGE

    try:
        ret, corners = cv2.findChessboardCornersSB(gray,
chessboard_size, flags)
    except:
        ret, corners = cv2.findChessboardCorners(gray,

```



```

chessboard_size, flags)

    if ret:
        print(" ✓ Chessboard detected.")

        objpoints.append(objp)

        # Corner refinement
        corners2 = cv2.cornerSubPix(
            gray, corners, (11, 11), (-1, -1),
            (cv2.TERM_CRITERIA_EPS + cv2.TERM_CRITERIA_MAX_ITER, 30,
0.001)
        )
        imgpoints.append(corners2)

        # Draw corners on image
        img_display = img.copy()
        cv2.drawChessboardCorners(img_display, chessboard_size,
corners2, ret)

    if len(objpoints) >= 1:
        h, w = gray.shape[:2]
        camera_matrix_est = np.array([[w, 0, w/2],
                                      [0, w, h/2],
                                      [0, 0, 1]], dtype=np.float32)
        dist_coeffs_est = np.zeros((4,1))

        # Define 3D points for coordinate axes (in chessboard
coordinate system)
        axis_points = np.float32([[0,0,0], [3,0,0], [0,3,0],
[0,0,-3]]).reshape(-1,3) * square_size

        # Find pose of the chessboard
        success, rvec, tvec = cv2.solvePnP(objp, corners2,
camera_matrix_est, dist_coeffs_est)

        if success:
            # Project 3D axis points to image plane
            axis_img_pts, _ = cv2.projectPoints(axis_points, rvec,
tvec, camera_matrix_est, dist_coeffs_est)
            axis_img_pts = np.int32(axis_img_pts).reshape(-1,2)

            # Draw coordinate axes
            origin = tuple(axis_img_pts[0])
            x_axis = tuple(axis_img_pts[1])
            y_axis = tuple(axis_img_pts[2])
            z_axis = tuple(axis_img_pts[3])

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        # Draw axes
        cv2.arrowsLine(img_display, origin, x_axis,
(0,0,255), 8) # X-axis: Red
        cv2.arrowsLine(img_display, origin, y_axis,
(0,255,0), 8) # Y-axis: Green
        cv2.arrowsLine(img_display, origin, z_axis,
(255,0,0), 8) # Z-axis: Blue

        cv2.putText(img_display, 'X', x_axis,
cv2.FONT_HERSHEY_SIMPLEX, 1, (0,0,255), 3)
        cv2.putText(img_display, 'Y', y_axis,
cv2.FONT_HERSHEY_SIMPLEX, 1, (0,255,0), 3)
        cv2.putText(img_display, 'Z', z_axis,
cv2.FONT_HERSHEY_SIMPLEX, 1, (255,0,0), 3)

        # Enhance corner visibility
        for corner in corners2:
            center = tuple(corner.ravel().astype(int))
            cv2.circle(img_display, center, 8, (255,255,0), -1) #
Yellow filled circles
            cv2.circle(img_display, center, 10, (0,0,0), 2)      #
Black outline

        # Convert BGR to RGB
        img_display_rgb = cv2.cvtColor(img_display, cv2.COLOR_BGR2RGB)

        plt.subplot(2, 3, (idx % 6) + 1)
        plt.imshow(img_display_rgb)
        plt.title(f'Image {idx+1}: Corners + XYZ Axes\
n{os.path.basename(fname)}', fontsize=10)
        plt.axis('off')

        # Show plot every 6 images
        if (idx + 1) % 6 == 0 or idx == len(images) - 1:
            plt.tight_layout()
            plt.show()
            if idx < len(images) - 1:
                plt.figure(figsize=(15, 10))
        else:
            print(" Chessboard NOT detected.")

# === Calibration ===
if len(objpoints) >= 3:
    ret, mtx, dist, rvecs, tvecs = cv2.calibrateCamera(
        objpoints, imgpoints, gray.shape[:: -1], None, None
    )

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print("\n Calibration complete!")
print("Camera Matrix:\n", mtx)
print("Distortion Coefficients:\n", dist)

# Save calibration data
np.savez('iphone_calibration_data.npz', mtx=mtx, dist=dist,
rvecs=rvecs, tvecs=tvecs)
print("Calibration data saved as 'iphone_calibration_data.npz'")

# Display calibration results
print(f"\nCalibration Results:")
print(f"- Used {len(objpoints)} images for calibration")
print(f"- Reprojection error: {ret:.4f} pixels")

else:
    print(f"\n Not enough valid images to calibrate. Found
{len(objpoints)} valid images, need at least 3.")

Found 26 image(s).

[1/26] Processing: IMG_0961.JPG
✓ Chessboard detected.

[2/26] Processing: IMG_0962.JPG
✓ Chessboard detected.

[3/26] Processing: IMG_0963.JPG
✓ Chessboard detected.

[4/26] Processing: IMG_0964.JPG
✓ Chessboard detected.

[5/26] Processing: IMG_0965.JPG
✓ Chessboard detected.

[6/26] Processing: IMG_0966.JPG
✓ Chessboard detected.

```

Image 1: Corners + XYZ Axes
IMG_0961.JPG

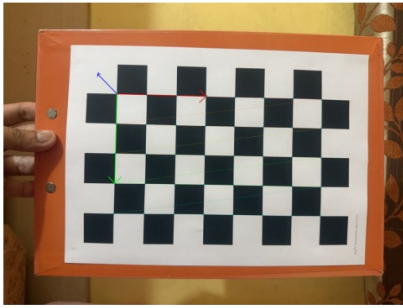


Image 2: Corners + XYZ Axes
IMG_0962.JPG

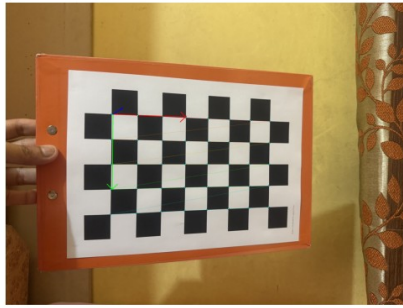


Image 3: Corners + XYZ Axes
IMG_0963.JPG

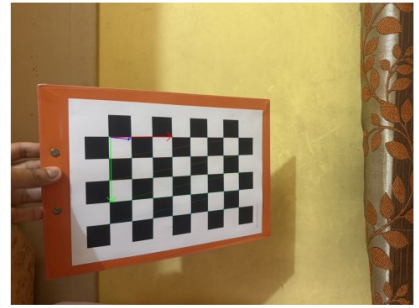


Image 4: Corners + XYZ Axes
IMG_0964.JPG

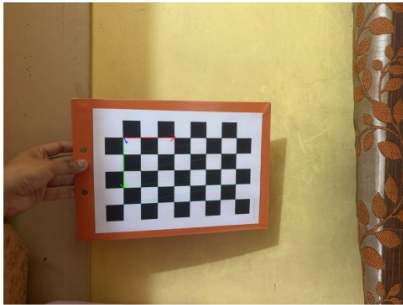


Image 5: Corners + XYZ Axes
IMG_0965.JPG

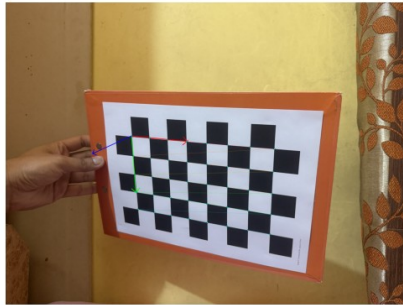
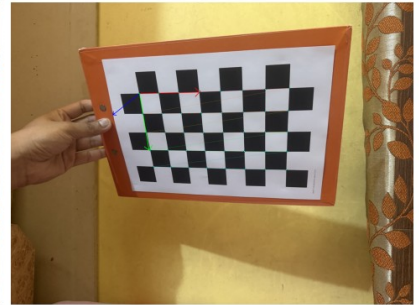


Image 6: Corners + XYZ Axes
IMG_0966.JPG



[7/26] Processing: IMG_0967.JPG
x Chessboard NOT detected.

[8/26] Processing: IMG_0968.JPG
✓ Chessboard detected.

[9/26] Processing: IMG_0969.JPG
✓ Chessboard detected.

[10/26] Processing: IMG_0970.JPG
✓ Chessboard detected.

[11/26] Processing: IMG_0971.JPG
✓ Chessboard detected.

[12/26] Processing: IMG_0972.JPG
x Chessboard NOT detected.

[13/26] Processing: IMG_0973.JPG
✓ Chessboard detected.

[14/26] Processing: IMG_0974.JPG
✓ Chessboard detected.

[15/26] Processing: IMG_0975.JPG
✓ Chessboard detected.

[16/26] Processing: IMG_0976.JPG
✓ Chessboard detected.

[17/26] Processing: IMG_0977.JPG
✗ Chessboard NOT detected.

[18/26] Processing: IMG_0978.JPG
✗ Chessboard NOT detected.

[19/26] Processing: IMG_0979.JPG
✓ Chessboard detected.

[20/26] Processing: IMG_0980.JPG
✗ Chessboard NOT detected.

[21/26] Processing: IMG_0981.JPG
✓ Chessboard detected.

[22/26] Processing: IMG_0982.JPG
✓ Chessboard detected.

[23/26] Processing: IMG_0983.JPG
✓ Chessboard detected.

[24/26] Processing: IMG_0984.JPG
✓ Chessboard detected.

Image 19: Corners + XYZ Axes
IMG_0979.JPG

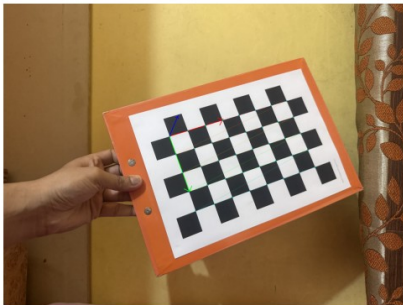


Image 14: Corners + XYZ Axes
IMG_0974.JPG

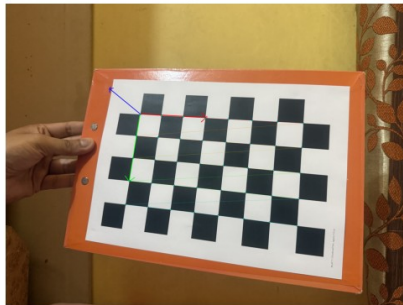


Image 21: Corners + XYZ Axes
IMG_0981.JPG

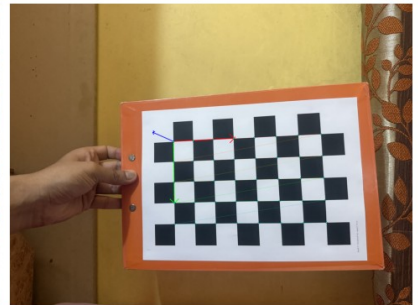


Image 22: Corners + XYZ Axes
IMG_0982.JPG

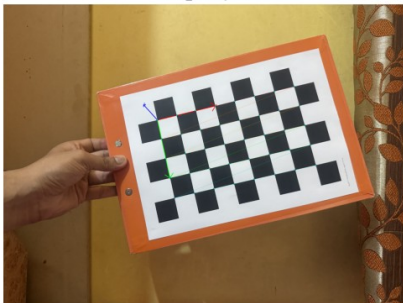


Image 23: Corners + XYZ Axes
IMG_0983.JPG

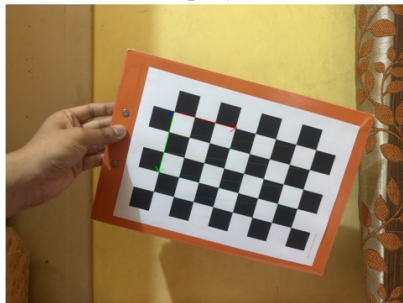
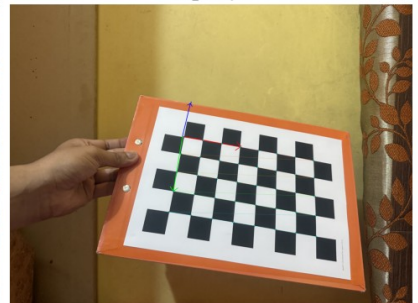


Image 24: Corners + XYZ Axes
IMG_0984.JPG



[25/26] Processing: IMG_0985.JPG
✓ Chessboard detected.

[26/26] Processing: IMG_0986.JPG
✓ Chessboard detected.

Image 25: Corners + XYZ Axes
IMG_0985.JPG

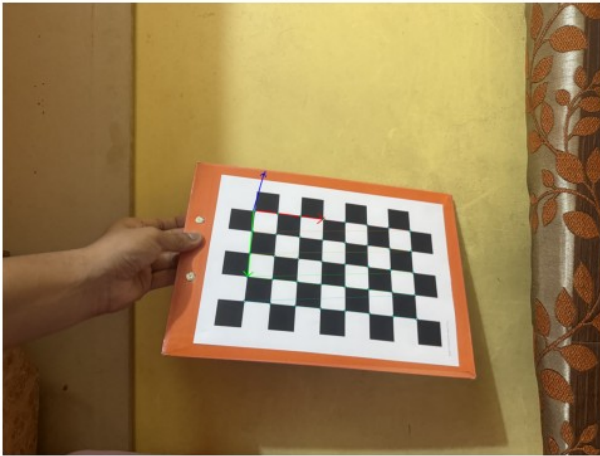
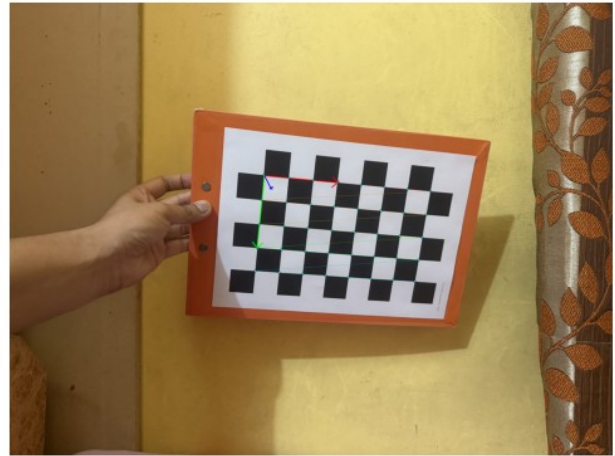


Image 26: Corners + XYZ Axes
IMG_0986.JPG



✓ Calibration complete!

Camera Matrix:

```
[[3.96468132e+03 0.00000000e+00 2.79612355e+03]
 [0.00000000e+00 3.95918955e+03 2.15585899e+03]
 [0.00000000e+00 0.00000000e+00 1.00000000e+00]]
```

Distortion Coefficients:

```
[[ 0.12295367 -0.19094559 0.00111336 -0.00547174 -0.65125816]]
```

Calibration data saved as 'iphone_calibration_data.npz'

Calibration Results:

- Used 21 images for calibration
- Reprojection error: 1.5126 pixels