ML Assignment 4

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Section A

M & Assignment 4

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Section B

(a)

1. Initialization:

The initial centroids were set as:

u1=(3.0,3.0), u2=(2.0,2.0)

These centroids serve as starting points for clustering.

2. Assignment:

Each data point was assigned to the nearest centroid using the Euclidean distance:

Distance=
$$(x1-c1)2+(x2-c2)2$$
 {Distance} = $sqrt\{(x_1 - c_1)^2 + (x_2 - c_2)^2\}$ Distance= $(x1-c1)2+(x2-c2)2$

The algorithm iteratively recalculated the distances and assigned the data points to the clusters defined by the closest centroids.

3. Update:

After each assignment, the centroids were updated by computing the mean of the points in each cluster:

$$uj=1Nj\sum_{i=1}^{i=1}Njxi \cdot \{u\}_{i} = \frac{1}{N_{i}} \cdot \sup_{i=1}^{N_{i}} \cdot \{x\}_{i} = \frac{1}{N_{i}}$$

where NjN_jNj is the number of points in cluster jjj.

4. Convergence Check:

The algorithm terminated when the centroids' change was smaller than the threshold tol=10-4text{tol} = 10^{-4} tol=10-4 or after 100 iterations.

(b)

Final Centroids:

After convergence, the centroids were:

```
u1=[5.8,2.125],u2=[4.2,-0.0556]\{u\}_1 = [5.8, 2.125], \quad \{u\}_2 = [4.2,-0.0556]u1=[5.8,2.125],u2=[4.2,-0.0556]
```

Cluster Assignments:

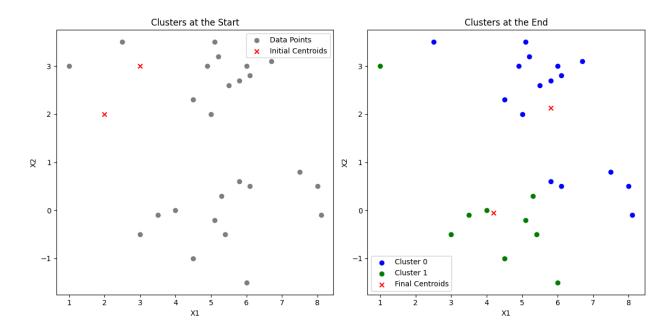
The data points were divided into two clusters as follows:

- Cluster 0: Points closer to u1\mathbf{u} 1u1
- Cluster 1: Points closer to u2\mathbf{u}_2u2

Visualization:

- The left plot shows the data points with the initial centroids.
- The right plot illustrates the final clusters with the updated centroids after convergence.

Plots:



(c)

Provided Initialization:

Using the given initial centroids:

```
u1=[3.0,3.0],u2=[2.0,2.0]\mathbf{u}_1 = [3.0, 3.0], \quad \mathbf{u}_2 = [2.0, 2.0]u1=[3.0,3.0],u2=[2.0,2.0]
```

• Final centroids after convergence:

```
 u1=[5.8,2.125], u2=[4.2,-0.0556] \\  wathbf{u}_1 = [5.8,2.125], \\  \quad \\  \mbox{mathbf}{u}_2 = [4.2,-0.0556] \\  \quad \\  \mbox{mathbf}{u}_2 = [4.2,-0.0556] \\  \quad \\  \q
```

• The data points were assigned to clusters based on proximity to these centroids.

Random Initialization:

With randomly initialized centroids:

Random initial centroids depend on the specific run.\text{Random initial centroids depend on the specific run.} Random initial centroids depend on the specific run.

Example from one run:

```
 u1=[4.03,0.3], u2=[6.02,2.033] $$  u1=[4.03,0.3], \quad \mathbf{u}_2 = [6.02,2.033] u1=[4.03,0.3], u2=[6.02,2.033] $$  u1=[4.03,0.3], u2=[6.02,2.03], u1=[4.03,0.3], u1
```

Final centroids after convergence:

 $u1=[4.03,0.3], u2=[6.02,2.033] $$ u1=[4.03,0.3], \quad \mathbf{u}_2 = [6.02,2.033] u1=[4.03,0.3], u2=[6.02,2.033] $$ u1=[4.03,0.3], u2=[6.02,2.03], u1=[4.03,0.3], u1$

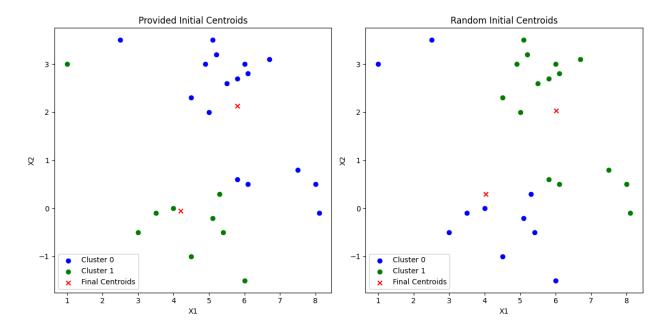
Key Observations:

- 1. The final cluster configurations depend significantly on the initialization of centroids.
- 2. With provided initialization, clustering follows the bias introduced by the given starting centroids, yielding consistent results.
- 3. Random initialization introduces variability in clustering, potentially leading to different outcomes, as seen in the random initialization plot.

Visualization:

- The left plot shows clustering with provided centroids.
- The right plot illustrates clustering with random initialization.

Plots:



(d)

Method:

To determine the optimal number of clusters (MMM), the **Elbow Method** was used. This involved:

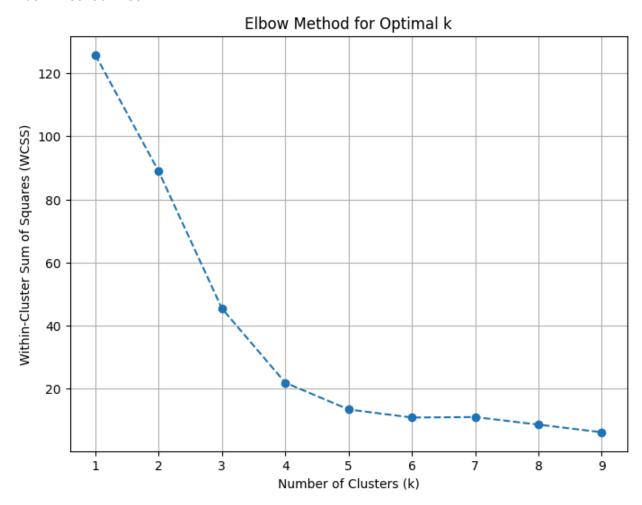
- 1. Calculating the **Within-Cluster Sum of Squares (WCSS)** for different values of kkk (number of clusters).
- 2. Plotting kkk against WCSS and identifying the "elbow point," where the rate of decrease slows significantly.

Results:

• The elbow point was observed at k=3k = 3k=3, indicating that three clusters best represent the data.

Visualization:

• Elbow Method Plot:

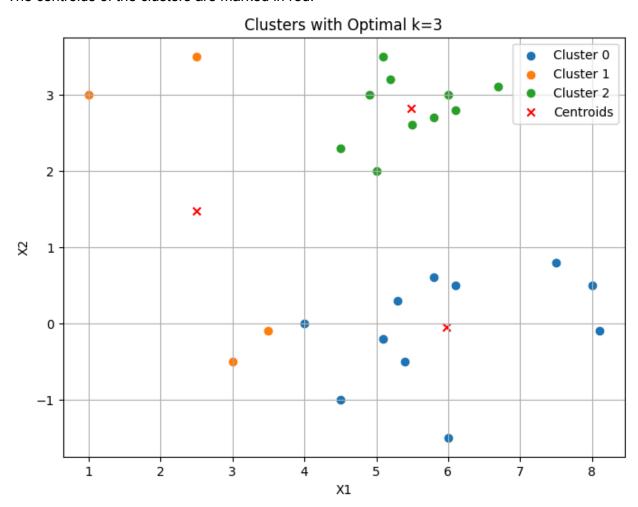


• The plot below shows WCSS values for k=1k=1 to k=9k=9k=9, with the elbow point at k=3k=3k=3.

Clustering with k=3k = 3k=3:

After identifying k=3k=3k=3 as the optimal number of clusters, clustering was performed with random initialization. The results are illustrated in the plot below:

- Three distinct clusters are shown, each marked with a unique color.
- The centroids of the clusters are marked in red.

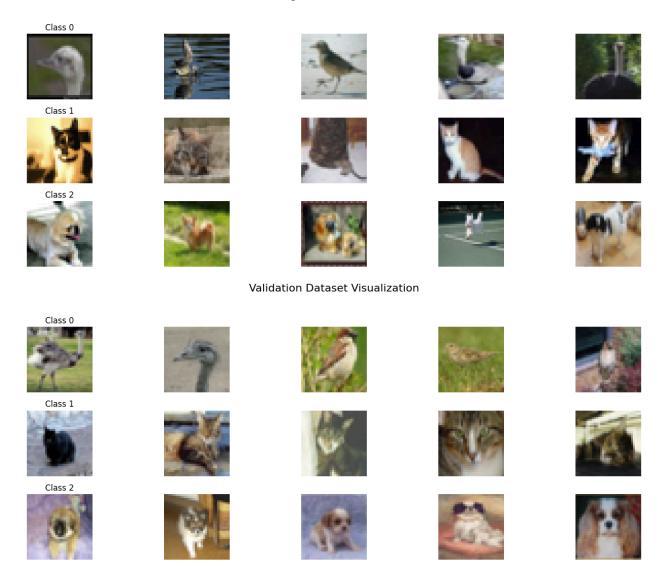


Key Observations:

- 1. Increasing the number of clusters (kkk) reduces WCSS but leads to diminishing returns after k=3k=3k=3.
- 2. The clustering results effectively group similar data points, with each cluster representing a distinct region in the feature space.

Section C

Training Dataset Visualization



3. Convolutional Layer 1:

Kernel size: 5×55 \times 55×5

• Number of filters: 16

Stride: 1Padding: 1

Max-Pooling Layer 1:

• Kernel size: 3×33 \times 33×3

• Stride: 2

Convolutional Layer 2:

Kernel size: 3×33 \times 33×3

• Number of filters: 32

Stride: 1Padding: 0

Max-Pooling Layer 2:

Kernel size: 3×33 \times 33×3

• Stride: 3

Fully Connected Layers:

FC1: 512→16512 \to 16512→16 neurons with ReLU activation.

• FC2: 16→316 \to 316→3 neurons for classification (3 classes).

4.

1. Training Progress:

- Training loss decreased steadily from 0.98320.98320.9832 in epoch 1 to 0.57460.5746 in epoch 15.
- Training accuracy improved from 50.59%50.59\%50.59% to 75.82%75.82\%75.82% over 15 epochs.

2. Validation Progress:

- Validation loss initially decreased, stabilizing in later epochs. This indicates the model was generalizing well.
- Validation accuracy improved from 59.23%59.23\%59.23\% in epoch 1 to 70.90\%70.90\%70.90\% by epoch 15.

3. Final Model:

 The trained model achieved good generalization performance, as evidenced by the close gap between training and validation metrics.

Output Logs

The training logs provide a detailed view of the model's performance over each epoch:

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Using device: cpu

Epoch 1/15

Train Loss: 0.9832, Train Accuracy: 0.5059

Val Loss: 0.8917, Val Accuracy: 0.5923

Epoch 2/15

Train Loss: 0.8733, Train Accuracy: 0.5982

Val Loss: 0.8191, Val Accuracy: 0.6247

Epoch 3/15

Train Loss: 0.8231, Train Accuracy: 0.6211

Val Loss: 0.7826, Val Accuracy: 0.6500

Epoch 4/15

Train Loss: 0.7918, Train Accuracy: 0.6398

Val Loss: 0.7597, Val Accuracy: 0.6620

Epoch 5/15

Train Loss: 0.7597, Train Accuracy: 0.6581

Val Loss: 0.7328, Val Accuracy: 0.6727

Epoch 6/15

Train Loss: 0.7330, Train Accuracy: 0.6768

Val Loss: 0.7214, Val Accuracy: 0.6810

Epoch 7/15

Train Loss: 0.7040, Train Accuracy: 0.6949

Val Loss: 0.6968, Val Accuracy: 0.6910

Epoch 8/15

Train Loss: 0.6822, Train Accuracy: 0.7042

Val Loss: 0.6941, Val Accuracy: 0.6860

Epoch 9/15

Train Loss: 0.6649, Train Accuracy: 0.7115

Val Loss: 0.6976, Val Accuracy: 0.6960

Epoch 10/15

Train Loss: 0.6504, Train Accuracy: 0.7174

Val Loss: 0.6916, Val Accuracy: 0.6933

Epoch 11/15

Train Loss: 0.6260, Train Accuracy: 0.7307

Val Loss: 0.6688, Val Accuracy: 0.7037

Epoch 12/15

Train Loss: 0.6138, Train Accuracy: 0.7388

Val Loss: 0.7192, Val Accuracy: 0.6863

Epoch 13/15

Train Loss: 0.5926, Train Accuracy: 0.7479

Val Loss: 0.6789, Val Accuracy: 0.7010

Epoch 14/15

Train Loss: 0.5847, Train Accuracy: 0.7543

Val Loss: 0.6934, Val Accuracy: 0.7053

Epoch 15/15

Train Loss: 0.5746, Train Accuracy: 0.7582

Val Loss: 0.6784, Val Accuracy: 0.7090

Model saved as 'simple_cnn_model.pth'

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Training and Validation Loss Plot



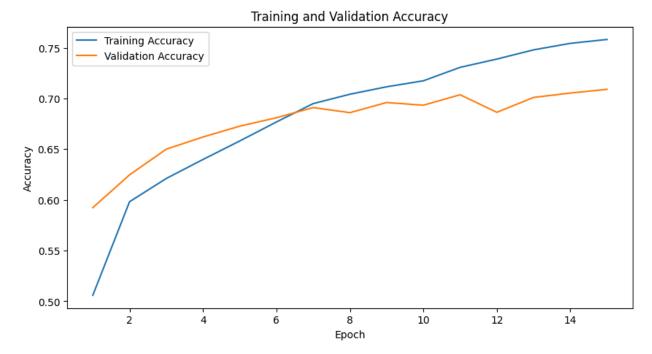
• Trend:

- Both training and validation loss consistently decreased during the 15 epochs.
- Training loss shows a smooth decline, suggesting that the model effectively learned from the data.
- Validation loss stabilizes and fluctuates slightly after epoch 10, indicating the model's generalization capability.

• Interpretation:

- The model avoids overfitting as validation loss does not significantly diverge from training loss.
- Slight fluctuations in validation loss are expected due to the nature of mini-batch training.

Training and Validation Accuracy Plot



Trend:

- Training accuracy steadily increases from 50.59%50.59\%50.59% in epoch 1 to 75.82%75.82\%75.82% in epoch 15.
- Validation accuracy improves from 59.23%59.23%59.23% in epoch 1 to 70.90%70.90%70.90%, closely tracking training accuracy.

• Interpretation:

- The small gap between training and validation accuracy indicates good generalization.
- The model has sufficient capacity to capture patterns in the data without overfitting.

6.

Training Progress

The model was trained for 15 epochs. Key observations include:

1. Training Loss:

- Decreased steadily from 0.97000.97000.9700 in epoch 1 to 0.57230.57230.5723 in epoch 15.
- o Indicates the model successfully minimized the loss during training.

2. Training Accuracy:

 Improved from 52.25%52.25\%52.25\% to 76.64\%76.64\%76.64\%, demonstrating the model's ability to learn from the training data.

Validation Progress

1 Validation Loss:

- Decreased initially but started increasing from epoch 6 (0.90580.90580.9058) to epoch 15 (1.09241.09241.0924).
- Suggests overfitting, as the model struggled to generalize to validation data.

2. Validation Accuracy:

- Peaked at 59.37%59.37%59.37% (epoch 9) but fluctuated and eventually dropped to 57.07%57.07%57.07% (epoch 15).
- Indicates the model failed to generalize effectively compared to CNN.

7.

Training and Validation Loss

CNN Observations:

- The **training loss** steadily decreases from 0.9832 to 0.5746 over 15 epochs, indicating consistent improvement during training.
- The **validation loss** initially decreases but stabilizes around epoch 11, indicating that the model is beginning to generalize well.
- Final Validation Loss: 0.6784

MLP Observations:

- The **training loss** decreases more gradually from 0.9700 to 0.5723.
- The **validation loss** decreases initially but starts increasing after epoch 6, which could indicate overfitting.
- Final Validation Loss: 1.0924

Inference:

- CNN outperforms MLP in terms of loss reduction.
- MLP shows signs of overfitting as the validation loss diverges from the training loss in later epochs.

Training and Validation Accuracy

CNN Observations:

• The **training accuracy** improves consistently, reaching **75.82%** by epoch 15.

- The validation accuracy also improves, stabilizing at 70.90%.
- The close gap between training and validation accuracy suggests good generalization.

MLP Observations:

- The **training accuracy** improves to **76.64%**, slightly higher than CNN.
- The **validation accuracy**, however, stagnates around **57%** in the later epochs, showing poor generalization.

Inference:

 CNN achieves better validation accuracy and generalizes well to unseen data, whereas MLP overfits and struggles to generalize.

Test Dataset Performance

CNN Observations:

- Test Accuracy: 70.23%
- **F1-Score**: Balanced across classes, with an average of **70%**.
 - o Class 0: F1 = 0.78
 - o Class 1: F1 = 0.62
 - Class 2: F1 = 0.70

MLP Observations:

- Test Accuracy: 55.90%
- **F1-Score**: Weaker and imbalanced, with an average of **56%**.
 - o Class 0: F1 = 0.64
 - o Class 1: F1 = 0.51
 - Class 2: F1 = 0.52

Inference:

 CNN significantly outperforms MLP in both accuracy and F1-score, particularly for complex classes (Class 1 and Class 2).

Confusion Matrices

Training Confusion Matrix

- CNN: Strong diagonal dominance, indicating excellent classification during training.
- **MLP**: Moderate diagonal dominance with more misclassifications.

Validation Confusion Matrix

- **CNN**: Better performance with fewer off-diagonal elements compared to MLP.
- MLP: Higher confusion between similar classes (e.g., Class 1 and Class 2).

Test Confusion Matrix

- **CNN**: More balanced predictions across all classes.
 - o E.g., Class 0: 802/1000, Class 1: 548/1000, Class 2: 757/1000.
- **MLP**: Higher misclassifications, especially for Class 2.
 - E.g., Class 0: 682/1000, Class 1: 501/1000, Class 2: 494/1000.

Inference:

• CNN shows stronger classification ability across all datasets, while MLP struggles, particularly for the more complex test dataset.

Key Takeaways

1. Model Performance:

- CNN is better suited for image classification tasks because of its ability to capture spatial features using convolutional layers.
- MLP, lacking convolutional layers, treats all pixels independently, making it less effective for image data.

2. Generalization:

- CNN generalizes well to unseen data, as seen in the small gap between training, validation, and test metrics.
- MLP shows poor generalization, with validation and test accuracy significantly lower than training accuracy.

3. Class-Specific Performance:

- CNN handles all classes relatively well, with balanced F1-scores.
- MLP struggles, especially for Class 1 and Class 2, which likely have more complex patterns.

4. Confusion Matrices:

- o CNN shows better diagonal dominance, reflecting fewer misclassifications.
- MLP confusion matrices show more errors, especially for similar or complex classes.