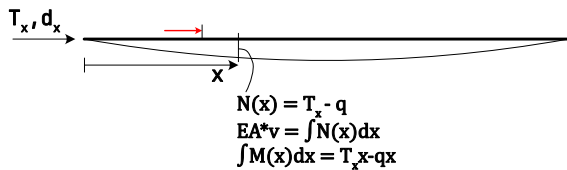


Venymän laskenta integroimalla normaalivoiman funktio

Ville PekkaLa, 25.2.2025

Pistekuorma

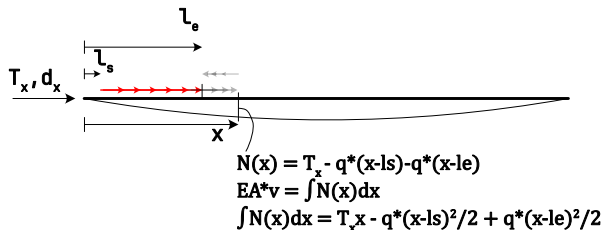


Venymän arvo pisteessä x

$$EI \cdot v'(x) = N(x)$$

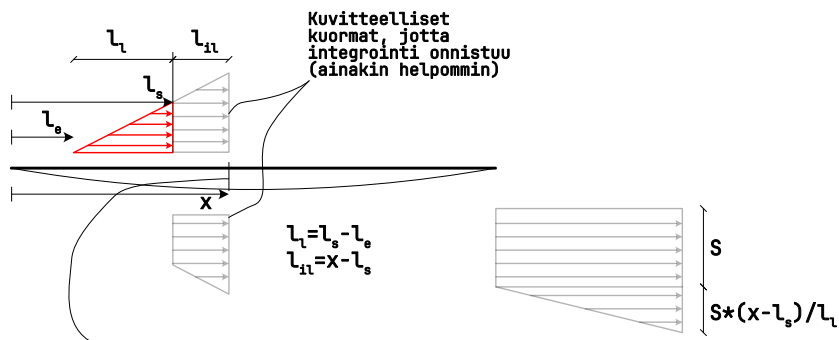
$$EI \cdot v = \int M(x) dx \quad (C_1 = \text{siirtymä } d_x \cdot EA)$$

Viivakuorma



Kolmiokuorma, kuorma kasvaa x-suuntaan

$$\begin{aligned}
 N(x) &= T_x - \\
 &\quad \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \cdot \frac{1}{2} + \\
 &\quad S^* (x - l_s) + \\
 &\quad \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \cdot \frac{1}{2} \\
 EI \cdot v &= \int N(x) dx \\
 \int N(x) dx &= T_x x - \\
 &\quad \frac{S}{l_1} (x - l_s)^3 \cdot \frac{1}{6} + \\
 &\quad S^* (x - l_s)^2 / 2 + \\
 &\quad \frac{S}{l_1} (x - l_s)^3 \cdot \frac{1}{6}
 \end{aligned}$$



Kolmiokuorma, kuorma pienenee x-suuntaan

Kuorma, joka loppuu ennen pistettä x

$$\begin{aligned}
 N(x) &= T_x - \\
 &\quad \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \cdot \frac{1}{2} - \\
 &\quad \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \cdot \frac{1}{2} + \\
 &\quad S^* (x - l_s) - \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \\
 EI \cdot v &= \int N(x) dx \\
 \int N(x) dx &= T_x x - \\
 &\quad \frac{S}{l_1} (x - l_s)^3 \cdot \frac{1}{6} - \\
 &\quad \frac{S}{l_1} (x - l_s)^3 \cdot \frac{1}{6} + \\
 &\quad S^* (x - l_s)^2 / 2 - \\
 &\quad \frac{S}{l_1} (x - l_s)^3 / 3
 \end{aligned}$$

$$\begin{aligned}
 N(x) &= T_x - \\
 &\quad \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \cdot \frac{1}{2} - \\
 &\quad S^* (x - l_s) - \\
 &\quad \frac{S}{l_1} (x - l_s) \cdot (x - l_s) \\
 EI \cdot v &= \int N(x) dx \\
 \int N(x) dx &= T_x x - \\
 &\quad \frac{S}{l_1} (x - l_s)^3 \cdot \frac{1}{6} + \\
 &\quad S^* (x - l_s)^2 / 2 - \\
 &\quad \frac{S}{l_1} (x - l_s)^3 / 3
 \end{aligned}$$

