



$arr[] = \{ 5, 10, 3, 2, 50, 80 \}$

$B = 78$

Brute force

```
for(int i=0; i<n; i++)  
{  
    for(int j=i+1; j<n; j++)  
    {  
        if (arr[i] - arr[j] == B)  
            return true;  
        if (arr[j] - arr[i] == B)  
            return true;  
    }  
}
```

TC: $O(N^2)$
SC: $O(1)$

$arr[] = \{5, 10, 3, 2, 50, 80\}$

~~$B = 78$~~

Sorting

$arr[] = \{2, 3, 5, 10, 50, 80\}$

$B = 45$

$\uparrow \quad \uparrow$
 $ei \quad si$

if _____

if ($arr[ei] - arr[si] > B$)

$ei--;$

else

$si++;$

←
X
←

$$\text{arr}[] = \{ \textcircled{5}, 10, 3, 2, 50, 80 \} \quad B = 78$$

TC: $O(N)$
SC: $O(N)$

(x, y)

$$\boxed{x - y = B}$$

let $x = 80$
 $y = 80 - 78 = \textcircled{2}$

$(80, 2)$

let $10 = x$
 $y = 10 - 78 = \underline{\underline{-68}}$

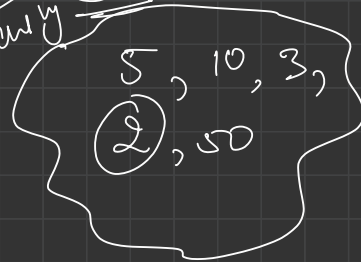
let $10 = y$
 $x = 78 + 10 = 88$

let $5 = x$
 $y = 5 - 78 = \boxed{-73}$

→ $O(1)$ searching

$y = x - B, \quad x = B + y$

insertion search



let $3 = x$
 $y = 3 - 78 = -75$

let $3 = y$
 $x = 78 + 3 = 81$

let $5 = y$
 $x = 78 + 5 = 83$

let $x = 50$
 $y = -28$
let $y = 50$
 $x = 128$

let $2 = x, y = -76$
 $2 = y, x = 80$

```
HashSet<Integer> mySet = new HashSet<>();
```

```
for (int ele : A) {
```

```
    // case 1
```

```
    int x = ele;
```

```
    int y = x - B;
```

```
    if (mySet.contains(y) == true) {
```

```
        return 1;
```

```
    }
```

```
    // case 2
```

```
    y = ele;
```

```
    x = B + y;
```

```
    if (mySet.contains(x) == true) {
```

```
        return 1;
```

```
    }
```

```
    // add myself for further reference of x, y  
    mySet.add(ele);
```

```
}
```

```
return 0;
```

$arr[] = \{ 5, 10, 3, 2, 50, 80 \}$

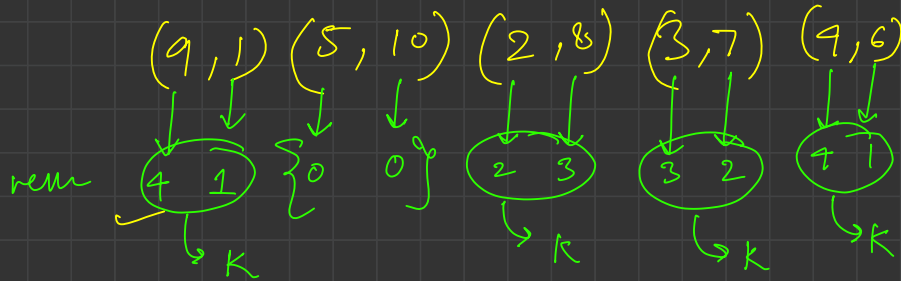
$B = 78$

5, 10, 3, 2,
50

TC: $O(N)$
sc: $O(N)$

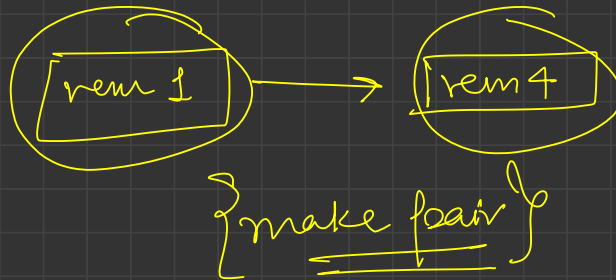
Array Pair divisible by k.

arr[] = { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 } k = 5



④
(K-rem)

rem	freq
1	1 2
2	1 2
3	1 2
4	1 2
0	1 2



neutralize each
comp. rem.

```

for (int rem : remFreqMap.keySet()) {
    // edge case of rem = 0
    if (rem == 0) {
        // no need to neutralize
        continue;
    }

    int compRem = k - rem;
    if (remFreqMap.containsKey(compRem) == false) {
        return false;
    } else if (remFreqMap.get(rem) != remFreqMap.get(compRem)) {
        return false;
    }
}

return true;

```

rem	freq
0	4
2	2
1	4
3	2
4	1

$k = 5$

$$\left\{ \begin{array}{l} \text{TC: } O(N) + O(N) = O(N) \\ \text{SC: } O(K) \end{array} \right.$$

$$\xrightarrow{\text{}} \{ \text{remFreqMap} \}$$

Largest Subarray with zero Sum

arr[] = { 15, -2, 2, -8, 1, 7, 10, 23 }

Brute force

↳ get each sub-array with sum

↳ maxlen

{ TC: $O(N^2)$
SC: $O(1)$

arr[] = { 0, 1, 2, 3, 4, 5, 6, 7 }

15, -2, 2, -8, 1, 7, 10, 23

0, 15, 13, 15, 7, 8, 15, 25, 40

first occ.
index

len = 5

15 → 0
13 → 1
7 → 3
8 → 4

2 - 0 = 2
5 - 0 = 5

subarray with zero sum

0, 1, 2, 3, 4, 5

2, -2, 2, -2, 2, -2

0, 2, 0, 2, 0, 2, 0

5 - (-1) = 6

Equilibrium Index

arr[] = { 9, 3, 7, 6, 8, 1, 10 }

$$\text{totalSum} = 44$$

$$\text{lsum} = \frac{9}{19}$$

$$\begin{aligned} \text{lsum} + \text{val} + \text{rsum} &= \text{totalSum} \\ \text{rsum} &= \text{total} - \text{val} - \text{lsum} \end{aligned}$$

$$= 44 - 6 - 19$$

$$= \underline{\underline{19}}$$

Sc! OCl)

Subarray Sum equal to K

arr[]: {10, 2, -2, -20, 10} , K = 10

3 subarrays

Brute-Force

{ get all subarray and check sum == K ;

{ TC: $O(N^2)$
SC: $O(1)$

$$\text{curr}[i] = \begin{matrix} & 0 & 1 & 2 & 3 & 4 \\ \begin{matrix} 0 \\ 0 \\ 10 \\ 12 \\ 10 \\ -10 \\ 0 \end{matrix} & 0 & 0 & 10 & 2 & -2 & -20 & 10 \end{matrix}, \quad k=10$$

① Map (currsum, index)

$$\text{currsum} = (\text{currsum} - k)$$

```

class Solution {
    static int solve(int N, int[] Arr, int K) {
        // Write your code here
        int result = 0;

        // runningSum, freq
        HashMap<Integer, Integer> map = new HashMap<>();
        map.put(key: 0, value: 1);

        int runningSum = 0;
        for (int num : Arr) {
            runningSum += num;

            int x = runningSum;
            int y = runningSum - K;

            if (map.containsKey(y) == true) {
                result += map.get(y);
            }

            map.put(runningSum, map.getOrDefault(runningSum, defaultValue: 0) + 1);
        }

        return result;
    }
}

```

$TC: O(N)$
 $SC: O(N)$

$K = 10$
 -1 0 1 2 3 4 5 6 7
 } 0, 0, 10, 2, -2, 0, -20, 10 }
 0 0 10 12 10 10 -10 0

runningSum	freq
0	1 3 3 4
10	1 3 3
12	1
-10	1

$3 + 3 + 3 + 1$
 $= 10$