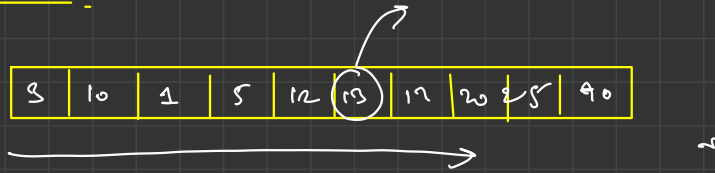




Hashing

A technique useful for searching purpose.

① Linear Search



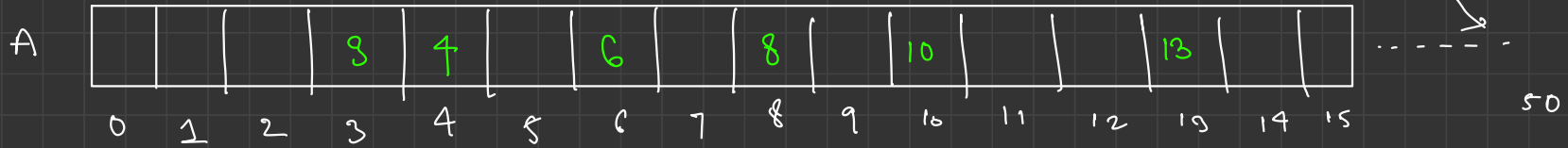
TC: $O(N)$ Searching.

② Binary Search \longrightarrow sorted Array.

{ TC: $O(\log N)$ Searching }

③ Hashing \rightarrow TC $O(1)$ Searching!

{ 8, 3, 13, 6, 4, 10 }, 50

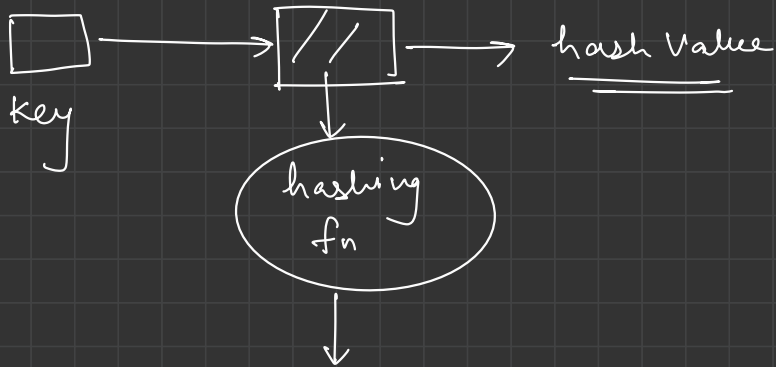


key \rightarrow 3

if $(A[key] \neq \text{null})$
true; // present

TC $O(1)$

high Memory is required,
hence we introduced hashing.

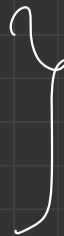


step 1

$$g(x) = K$$

key

integer value.



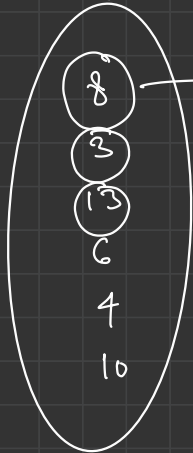
step 2

$$f(K) = y$$



hashing fn

Key Space

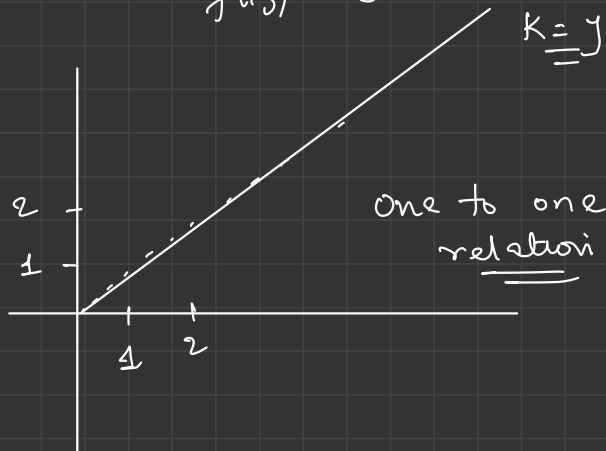


$$f(k) = y$$

$$f(8) = 8$$

$$f(13) = 3$$

$$f(13) = 13$$

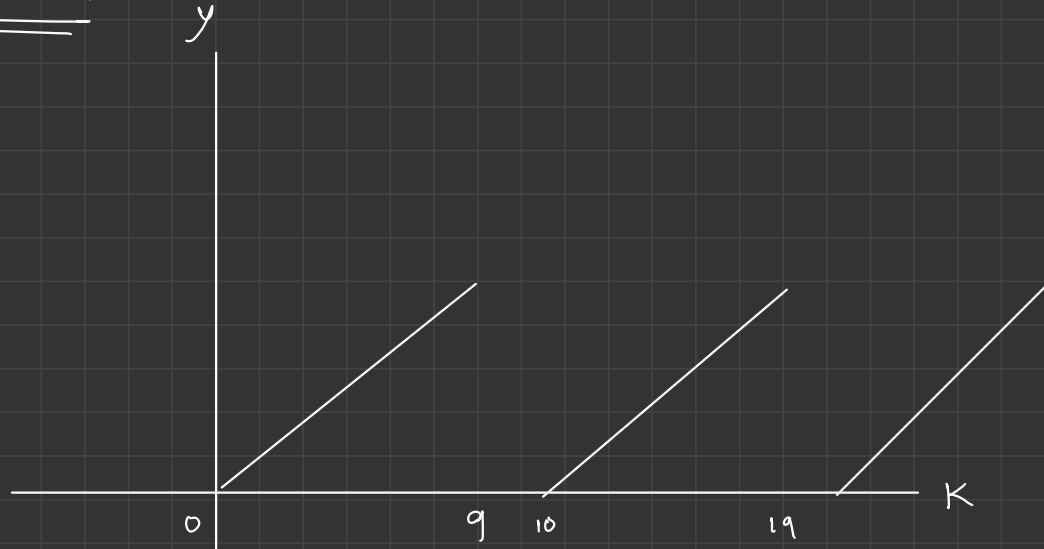


	0
	1
	2
3	3
	4
8	5
13	6
	...

HashTable

Many to One Relation

$$\underline{\underline{y = K \% 10}}$$



Hash Table

Key Space

- 8
- 3
- 13
- 6
- 4
- 10

hashing f^h

(0-9)

$$\underline{f(K) = K \% 10}$$

$$f(8) = 8 \% 10 = 8$$

$$f(3) = 3 \% 10 = 3$$

$$f(13) = 13 \% 10 = 3$$

Collision

	0
	1
	2
3	3
	4
	5
	6
	7
8	8
	9
	10
	11
	12

$$f(k) = k \% \textcircled{20}$$

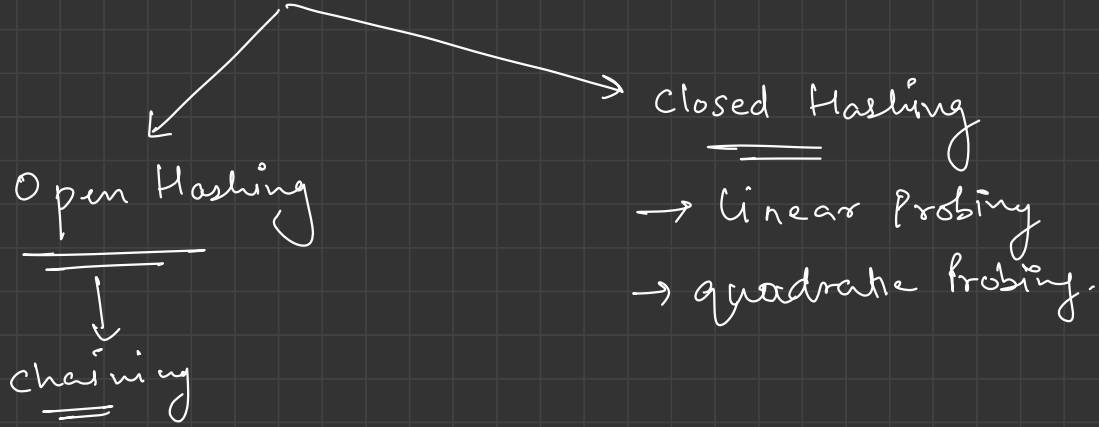
size of hashtable

If hashtable size = 1000

✓

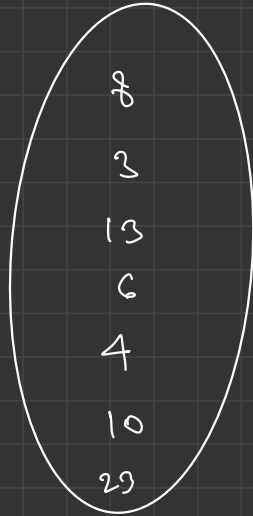
$f(k) = k \% \textcircled{1000}$

Methods to Remove Collision.



Chaining

Key Space



hashing f^h

(0-9)

$$\underline{f(K) = K \% 10}$$

$f(8) = 8$
 $f(3) = 3$
 $f(13) = 3$
 $f(6) = 6$
 $f(4) = 4$
 $f(10) = 0$
 $f(29) = 9$

Hash Table

10	0
	1
	2
3	3
4	4
	5
6	6
	7
8	8
	9

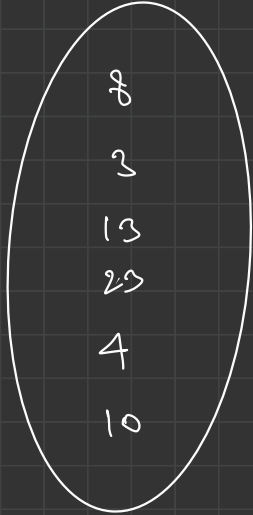
$13 \rightarrow 23$
 $T(13) = 23$

find (13)

3

Linear Probing

Key Space



hashing f^h

$$\underline{f(K) = K \% 10}$$

$$f'(K) = [f(K) + \overset{1}{f(h(i))}] \% 10$$

$$h(i) = i, \quad i = 0, 1, 2, \dots$$

$$f'(8) = [f(8) + h(0)] \% 10 = (8 + 0) \% 10 = 8$$

$$f'(3) = [f(3) + h(1)] \% 10 = (3 + 0) \% 10 = 3$$

$$\rightarrow f'(13) = [f(13) + \underline{h(2)}] \% 10 = (3 + 0) \% 10 = 3$$

Hash Table

10	0
	1
	2
2	3
13	4
23	5
4	6
	7
8	8
	9

$$\begin{aligned} f'(13) &= [f(13) + \underline{h(1)}] \% 10 \\ &= (3 + 1) \% 10 = 4 \end{aligned}$$

find(4)

Quadratic Probing

$$f(k) = k \% \text{size}$$

$$f'(k) = [f(k) + h(i)] \% \text{size}$$

$$h(i) = i^2, \quad i = 0, 1, 2, 3, \dots$$

8

size = 10

3

$$f'(8) = [8 + 0] \% 10 = 8 \checkmark$$

13

$$f'(3) = [3 + 0] \% 10 = 3 \checkmark$$

25

$$f'(25) = [3 + 4] \% 10 = 7 \checkmark$$

1

$$= 7 \% 10 = 7 \checkmark$$

10

$$f'(10) = [3 + 1] \% 10 = 4 \checkmark$$

HashMap, HashSet



{ Hashing Algo }

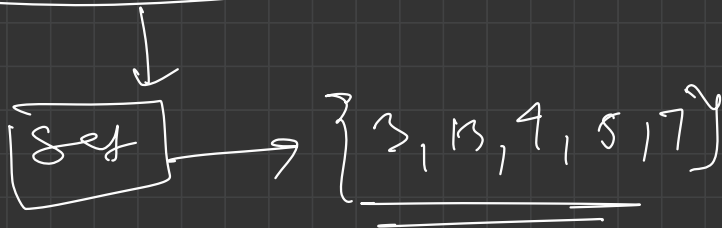
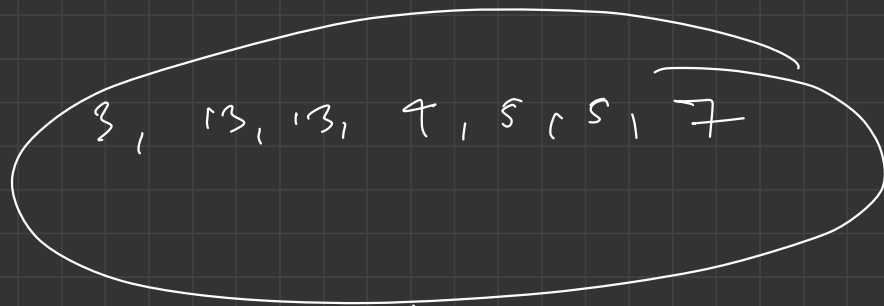
TreeMap, TreeSet



{ Red-Black trees }

Sets

Collection of unique entities



Searching
insertion

$O(1)$

HashSet

Values will be in
Random order

TreeSet

Values are sorted
in asc. order

Searching
insertion
 $O(\log N)$

HashMap

→ Key - value pairs

```
HashMap<Integer, String> map = new HashMap();
```

key	Value
1	Rishi
2	Aca'o
1	

→ Keys are in Random Order

→ offers $O(1)$ searching, $O(1)$ insertion.

TREEMAP

→ stores keys in asc. order.

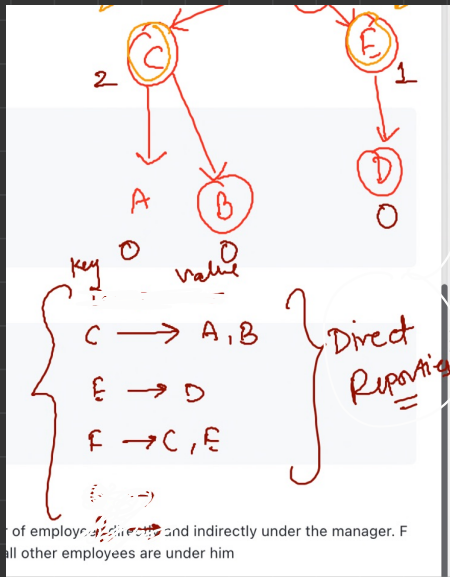
→ offers $O(\log N)$ search, $O(\log N)$ insertion.

↓ ↓ ↓ ↓
[1, 7, 4, 3, 4, 8, 7] K=2

```
public void firstElementToOccurKTimes(int[] nums, int n, int k) {  
    // Your code here  
    HashMap<Integer, Integer> mymap = new HashMap<>();  
  
    for (int num : nums) {  
        // if (mymap.containsKey(num)) {  
        //     mymap.put(num, mymap.get(num) + 1);  
        // } else {  
        //     mymap.put(num, 1);  
        // }  
  
        mymap.put(num, mymap.getOrDefault(num, defaultValue: 0) + 1);  
  
        if (mymap.get(num) == k) {  
            System.out.println(num);  
            return;  
        }  
    }  
  
    System.out.println(-1);  
}
```

key	value
1	1
7	1
4	2
3	1

TC = O(N)



```

2 import java.util.*;
3
4 class Solution {
5     int rec (String ceo, HashMap<String, ArrayList<String>> mngrAndDirect
6         // base case the emp is not a manager
7         if (mngrAndDirect.containsKey(ceo) == false) {
8             ans.put(ceo, 0);
9             return 1;
10        }
11
12        int cnt = 0;
13        for (String emp : mngrAndDirect.get(ceo)) {
14            cnt += rec(emp, mngrAndDirect, ans);
15        }
16
17        ans.put(ceo, cnt);
18        return cnt + 1;
19    }
20
21    public void EmpUnderManager(Map<String, String> emp)
22    {
23        HashMap<String, ArrayList<String>> mngrAndDirect = new HashMap<>();
24        String ceo = "";
25    }

```

A → 0
 B → 0
 C → 2
 D → 0
 E → 1
 F → 5

