

# Circular Queue and Deque in C++

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## Part 1: Circular Queue

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### ✓ 1. Definition

- A **Circular Queue** is a **linear data structure** that follows the **FIFO** principle (First-In-First-Out).
  - Unlike a normal queue, it **wraps around** when the end of the array is reached.
  - This helps to **reuse the empty spaces** left after deletions.
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### ✓ 2. Real-Life Example

Imagine people standing in a **circular line** for a roller coaster ride — when someone leaves the front, the space can be reused from the rear without shifting everyone.

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### ✓ 3. Circular Queue Structure

```
#define SIZE 5
int queue[SIZE];
int front = -1, rear = -1;
```

- **front**: Points to the first element
  - **rear**: Points to the last inserted element
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### ✓ 4. Full Conditions

- **Empty**: `front == -1`
- **Full**: `(rear + 1) % SIZE == front`

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## ✓ 5. Operations in Circular Queue

### ♦ Enqueue (Insert)

```
void enqueue(int value) {
    if ((rear + 1) % SIZE == front)
        cout << "Queue is Full\n";
    else {
        if (front == -1)
            front = rear = 0;
        else
            rear = (rear + 1) % SIZE;
        queue[rear] = value;
    }
}
```

### ♦ Dequeue (Delete)

```
void dequeue() {
    if (front == -1)
        cout << "Queue is Empty\n";
    else {
        cout << "Deleted: " << queue[front] << endl;
        if (front == rear)
            front = rear = -1;
        else
            front = (front + 1) % SIZE;
    }
}
```

### ♦ Display Queue

```
void display() {
    if (front == -1)
        cout << "Queue is Empty\n";
    else {
        int i = front;
        cout << "Queue: ";
        while (true) {
            cout << queue[i] << " ";
            if (i == rear) break;
            i = (i + 1) % SIZE;
        }
    }
}
```

```
    }  
    cout << endl;  
}  
}
```

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## Dry Run Example

Operations:

```
enqueue(10); enqueue(20); enqueue(30); enqueue(40); enqueue(50); //  
Full  
dequeue(); dequeue();  
enqueue(60); enqueue(70); // Wraps around  
display();
```

Result:

Queue: 30 40 50 60 70

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## Summary of Circular Queue

Operation	Time Complexity
Enqueue	O(1)
Dequeue	O(1)
Display	O(n)
Space Used	Fixed, reused

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## Part 2: Deque (Double-Ended Queue)

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### ✓ 1. Definition

- A **Deque** is a **double-ended queue** where we can insert and delete from both **front** and **rear**.
  - It is more flexible than both a queue and a stack.
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### ✓ 2. Real-Life Analogy

Think of a **bus** with doors at both front and back. Passengers can **enter and exit from either side**.

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### ✓ 3. Types of Deques

Type	Insertion	Deletion
Input Restricted	Only at rear	Both front and rear
Output Restricted	Both front and rear	Only at front
General Deque	Both ends	Both ends

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### ✓ 4. Deque Structure

```
#define SIZE 5
int deque[SIZE];
int front = -1, rear = -1;
```

- `front` and `rear` are used for both insertion and deletion.
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### ✓ 5. Conditions

- **Empty:** `front == -1`
- **Full:** `(front == (rear + 1) % SIZE)`

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## ✓ 6. Operations in Deque

### + Insert at Front

```
void insertFront(int value) {
    if ((front == (rear + 1) % SIZE))
        cout << "Deque is Full\n";
    else {
        if (front == -1)
            front = rear = 0;
        else
            front = (front - 1 + SIZE) % SIZE;
        deque[front] = value;
    }
}
```

### + Insert at Rear

```
void insertRear(int value) {
    if ((front == (rear + 1) % SIZE))
        cout << "Deque is Full\n";
    else {
        if (front == -1)
            front = rear = 0;
        else
            rear = (rear + 1) % SIZE;
        deque[rear] = value;
    }
}
```

### — Delete from Front

```
void deleteFront() {
    if (front == -1)
        cout << "Deque is Empty\n";
    else {
        cout << "Deleted: " << deque[front] << endl;
        if (front == rear)
            front = rear = -1;
        else
            front = (front + 1) % SIZE;
    }
}
```

```
        front = (front + 1) % SIZE;
    }
}
```

#### — Delete from Rear

cpp

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```
void deleteRear() {
    if (front == -1)
        cout << "Deque is Empty\n";
    else {
        cout << "Deleted: " << deque[rear] << endl;
        if (front == rear)
            front = rear = -1;
        else
            rear = (rear - 1 + SIZE) % SIZE;
    }
}
```

#### 🖨 Display

```
void display() {
    if (front == -1)
        cout << "Deque is Empty\n";
    else {
        int i = front;
        cout << "Deque: ";
        while (true) {
            cout << deque[i] << " ";
            if (i == rear) break;
            i = (i + 1) % SIZE;
        }
        cout << endl;
    }
}
```

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#### 🧠 Dry Run Example

Operations:

```
insertRear(10);
```

```
insertRear(20);
insertFront(5);
deleteRear();
deleteFront();
display();
```

**Deque Status:**

Deque: 10

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### Summary of Deque

Operation	Description	Time Complexity
insertFront()	Insert element at front	O(1)
insertRear()	Insert element at rear	O(1)
deleteFront()	Delete from front	O(1)
deleteRear()	Delete from rear	O(1)

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### Quiz (Quick Recap)

**Q1.** What is the condition for a circular queue to be full?

✓ `(rear + 1) % SIZE == front`

**Q2.** What is the advantage of a circular queue over a normal queue?

✓ Space is reused after deletion

**Q3.** What does a deque allow?

✓ Insertion and deletion from both ends

**Q4.** In input-restricted deque, from where can we delete?

✓ From both front and rear