VECTORS

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What is a vector?

Vector is a quantity which has both the magnitude and direction.

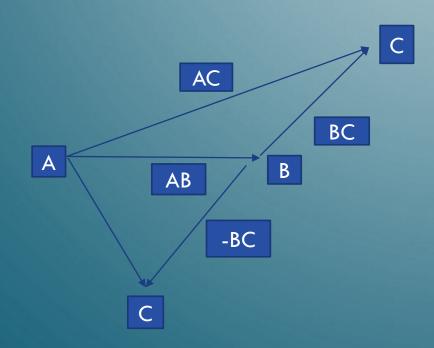




- 1) Unit Vector: Vector having magnitude equals to 1.
- 2) Co-initial Vectors: Vectors having same initial point are called as co-initial vectors.
- 3) Collinear Vectors: Vectors parallel to each other are called collinear vectors.
- 4)Equal Vectors: Vectors having equal magnitude and same direction.
- 5) Negative Vectors: Vectors having equal magnitude but exactly in opposite direction.

Addition of 2 Vectors

$$\cdot$$
 \overrightarrow{AB} $+\overrightarrow{BC}$ $=$ \overrightarrow{AC}



Multiplying a Vector by a Scalar

Dot Product of 2 Vectors

- Dot Product of $\mathbf{v} = a_1 \mathbf{i} + b_1 \mathbf{j}$ and $\mathbf{w} = a_2 \mathbf{i} + b_2 \mathbf{j}$ $\mathbf{v} \bullet \mathbf{w} = a_1 a_2 + b_1 b_2$ OR $\mathbf{v} \bullet \mathbf{w} = \|\mathbf{v}\| \|\mathbf{w}\| \cos \theta$
- Angle between two vectors (θ is the smallest non-negative angle between the two vectors)

$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|} \quad \text{and} \quad \theta = \cos^{-1} \left(\frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|} \right)$$

Cross Product of 2 vectors

$$\mathbf{A} = a_1 \mathbf{i} + a_2 \mathbf{j} + a_3 \mathbf{k}$$

$$\mathbf{B} = b_1 \mathbf{i} + b_2 \mathbf{j} + b_3 \mathbf{k}$$

$$\mathbf{A} \times \mathbf{B} = \det \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = \mathbf{i}(a_2b_3 - a_3b_2) + \mathbf{j}(a_3b_1 - a_1b_3) + \mathbf{k}(a_1b_2 - a_2b_1)$$

Example:

$$A=i-j$$

$$B=i+k$$

$$\mathbf{A} \times \mathbf{B} = \mathbf{i}(-1-0) + \mathbf{j}(0-1) + \mathbf{k}(0-(-1)) = -\mathbf{i} - \mathbf{j} + \mathbf{k}$$



Equation of Straight Line

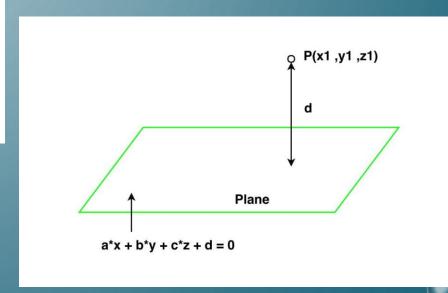
 $m \rightarrow Slope$

 $C \rightarrow$ Intercept of line on Y axis.

Distance b/w a point from plane

The distance D between a point $P_0(x_0,y_0,z_0)$ and the plane ax + by + cz + d = 0 is

$$D = \frac{|ax_0 + by_0 + cz_0 + d|}{\sqrt{a^2 + b^2 + c^2}}$$





Equation of a plane

• IF ANY PLANE P PASSES THROUGH THE POINT (X1,Y1,Z1) AND THE VECTOR NORMAL TO IT IS AI^+BJ^+CK^

THEN ITS EQUATION IS GIVEN BY,

$$P:A(X-X1)+B(Y-Y1)+C(Z-Z1)=0$$