



# Today's Agenda

## **Last time:**

- Central Limit Theorem
- Moment generating functions

...we finished the course material!

## **Today (Lec 36, 07/26):**

- Practice
- Course evaluation

## Question 1

Suppose  $X \sim \text{Bernoulli}(p)$  for some  $p \in (0, 1)$ . Compute the mgf of  $X$  and use it to compute  $E(X)$  and  $\text{Var}(X)$ .



## Question 2

Let  $X, Y$  be arbitrary random variables, which of the following is always correct?

- If  $X$  and  $Y$  are independent, they are uncorrelated.
- If  $X$  and  $Y$  are uncorrelated, they are independent.
- If  $X$  and  $Y$  are dependent, they are correlated.

## Question 3

In a laboratory, the temperature of an object is measured independently with two thermometers  $A$  and  $B$ . Let  $X$  and  $Y$  show the temperatures of the object measured by thermometers  $A$  and  $B$ , respectively. We decide to combine the two measurements as a weighted average of  $X$  and  $Y$  to report the temperature of the object, i.e. the reported temperature  $T$  is  $T = \alpha X + (1 - \alpha)Y$  where  $\alpha \in (0, 1)$ . For what value of  $\alpha$  is the variance of the random variable  $T$  minimized?



## Question 4

Let  $X$  be a continuous random variable with pdf

$$f(x) = e^{-x}, \quad x \geq 0$$

and 0 otherwise. Compute the median of  $X$ .





## Question 5

It is known that 8% of the world's population has blue eyes. Suppose you would like to estimate this proportion by asking  $n$  people whether they have blue eyes. You would use as an estimate  $X/n$  where  $X$  is the number of people having blue eyes in a sample of  $n$  people. How many people do you need to ask so that with probability 95%, the estimate will be within 0.01 of its true value 0.08?



## Question 6

Suppose that  $X_1, \dots, X_{50}$  are independent Geometric random variables with parameter 0.5. Estimate the probability that  $\sum_{i=1}^{50} X_i > 55$ .



## Question 7

Let  $X$  be a continuous rv with pdf

$$f(x) = \lambda x^{\lambda-1}, \quad 0 < x < 1,$$

and 0 otherwise.

- a) Compute  $E(X^k)$  for  $k \in \mathbb{N}$ .
- b) Let  $Y = -\lambda \log(X)$ . Determine the pdf of  $Y$ .







# Course Perceptions

Please go to <https://perceptions.uwaterloo.ca> and fill out the survey.

when it's almost course evaluation time & my teacher starts trying me

