

Artificial Intelligence Lab Report



Submitted by

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Program 1 - Tic Tac toe

Algorithm

Lab - 1
24/10/2021

Week - 1

Tic - Tac - Toe

function minmax (node, depth, isMaximizingPlayer):

if node is a terminal state:

return evaluate (node)

if is MaximizingPlayer:

best value = $-\infty$

for each child in node:

value = minmax (child, depth+1, false)

bestvalue = max (best-value, value)

return bestvalue

else:

bestvalue = $+\infty$

for each child in node:

value = minmax (child, depth+1, true)

bestvalue = min (bestvalue, value)

return bestvalue.

24/10/2021

Code :

```
board={1:' ',2:' ',3:' ',  
        4:' ',5:' ',6:' ',  
        7:' ',8:' ',9:' '  
}
```

```

def printBoard(board):
    print(board[1]+'|'+board[2]+'|'+board[3])
    print('-+-+-')
    print(board[4] + '|' + board[5] + '|' + board[6])
    print('-+-+-')
    print(board[7] + '|' + board[8] + '|' + board[9])
    print('\n')

def spaceFree(pos):
    if(board[pos]==' '):
        return True
    else:
        return False

def checkWin():
    if(board[1]==board[2] and board[1]==board[3] and board[1]!=' '):
        return True
    elif(board[4]==board[5] and board[4]==board[6] and board[4]!=' '):
        return True
    elif(board[7]==board[8] and board[7]==board[9] and board[7]!=' '):
        return True
    elif (board[1] == board[5] and board[1] == board[9] and board[1] != ' '):
        return True
    elif (board[3] == board[5] and board[3] == board[7] and board[3] != ' '):
        return True
    elif (board[1] == board[4] and board[1] == board[7] and board[1] != ' '):
        return True
    elif (board[2] == board[5] and board[2] == board[8] and board[2] != ' '):
        return True
    elif (board[3] == board[6] and board[3] == board[9] and board[3] != ' '):
        return True
    else:
        return False

def checkMoveForWin(move):
    if (board[1]==board[2] and board[1]==board[3] and board[1] ==move):
        return True
    elif (board[4]==board[5] and board[4]==board[6] and board[4] ==move):
        return True
    elif (board[7]==board[8] and board[7]==board[9] and board[7] ==move):
        return True
    elif (board[1]==board[5] and board[1]==board[9] and board[1] ==move):
        return True
    elif (board[3]==board[5] and board[3]==board[7] and board[3] ==move):
        return True

```

```

elif (board[1]==board[4] and board[1]==board[7] and board[1] ==move):
    return True
elif (board[2]==board[5] and board[2]==board[8] and board[2] ==move):
    return True
elif (board[3]==board[6] and board[3]==board[9] and board[3] ==move):
    return True
else:
    return False

def checkDraw():
    for key in board.keys():
        if (board[key]==' '):
            return False
    return True
def insertLetter(letter, position):
    if (spaceFree(position)):
        board[position] = letter
        printBoard(board)

        if (checkDraw()):
            print('Draw!')
        elif (checkWin()):
            if (letter == 'X'):
                print('Bot wins!')
            else:
                print('You win!')
        return

    else:
        print('Position taken, please pick a different position.')
        position = int(input('Enter new position: '))
        insertLetter(letter, position)
        return

player = 'O'
bot ='X'

def playerMove():
    position=int(input('Enter position for O:'))
    insertLetter(player, position)
    return

def compMove():
    bestScore=-1000
    bestMove=0

```

```

for key in board.keys():
    if (board[key]==' '):
        board[key]=bot
        score = minimax(board, False)
        board[key] = ' '
    if (score > bestScore):
        bestScore = score
        bestMove = key

insertLetter(bot, bestMove)
return
def minimax(board, isMaximizing):
    if (checkMoveForWin(bot)):
        return 1
    elif (checkMoveForWin(player)):
        return -1
    elif (checkDraw()):
        return 0

    if isMaximizing:
        bestScore = -1000
        for key in board.keys():
            if board[key] == ' ':
                board[key] = bot
                score = minimax(board, False)
                board[key] = ' '
                if (score > bestScore):
                    bestScore = score
        return bestScore
    else:
        bestScore = 1000

        for key in board.keys():
            if board[key] == ' ':
                board[key] = player
                score = minimax(board, True)
                board[key] = ' '
                if (score < bestScore):
                    bestScore = score
        return bestScore

while not checkWin():
    compMove()
    playerMove()

```

Output :

V Dhanush Reddy

1BM22CS324

```
X| |  
-+-+--  
| |  
-+-+--  
| |
```

Enter position for O: 3

```
X| |O  
-+-+--  
| |  
-+-+--  
| |
```

```
X| |O  
-+-+--  
X| |  
-+-+--  
| |
```

Enter position for O: 9

```
X| |O  
-+-+--  
X| |  
-+-+--  
| |O
```

```
X| |O  
-+-+--  
X| |X  
-+-+--  
| |O
```

```
x| |o
-+-+
x| |x
-+-+
| |o
```

Enter position for O: 2

```
x|o|o
-+-+
x| |x
-+-+
| |o
```

```
x|o|o
-+-+
x|x|x
-+-+
| |o
```

Bot wins!

Program 2: Vacuum Cleaner

Algorithm

Week-2

18/10/2024

Vacuum Cleaner Agent:

FUNCTION vacuum_world()

INITIALIZE goal state as {'A': '0', 'B': '0'}

// 0: clean, 1: Dirty.

SET cost to 0

PROMPT for vacuum location (A/B) as location_input

PROMPT for status of location_input as status_input

SET other_location to 'B' if A else 'A'

PROMPT for status of other_location as status_input_compl

IF location_input is 'A':

IF status_input is '1':

SET goal state ['A'] to '0' // clean A.

INCREMENT cost by 2

IF status_input_compl is '1':

SET goal state ['B'] to '0'

ELSE IF status_input_compl is '1':

INCREMENT cost by 1

SET goal state ['B'] to '0'

ELSE:

IF status_input is '1':

SET goal state ['B'] to '0'

INCREMENT cost by 2

IF status_input_compl is '1':

SET goal state ['A'] to '0'

ELSE-IF status_input_compl is '1':

INCREMENT cost by 1

SET goal state ['A'] to '0'

PRINT goal state and cost.

END FUNCTION

call vacuum_agent() could

18/10/2024

Code:

```
def vacuum_world():
    # Initializing goal_state
    # 0 indicates Clean and 1 indicates Dirty
    goal_state = {'A': '0', 'B': '0'}
    cost = 0

    location_input = input("Enter Location of Vacuum (A or B): ").strip().upper() #
    User input for vacuum location

    status_input = input(f"Enter status of {location_input} (0 for Clean, 1 for Dirty):
    ").strip() # Status of the current location
    other_location = 'B' if location_input == 'A' else 'A'
    status_input_complement = input(f"Enter status of {other_location} (0 for Clean, 1
    for Dirty): ").strip() # Status of the other room

    print("Initial Location Condition: " + str(goal_state))

    # Helper function to clean a location
    def clean(location):
        nonlocal cost
        goal_state[location] = '0'
        cost += 1 # Cost for sucking dirt
        print(f"Location {location} has been Cleaned. Cost: {cost}")

    # Main logic
    if location_input == 'A':
        print("Vacuum is placed in Location A.")
        if status_input == '1':
            print("Location A is Dirty.")
            clean('A')
        if status_input_complement == '1':
            print("Location B is Dirty.")
            print("Moving right to Location B.")
            cost += 1 # Cost for moving right
            print(f"COST for moving RIGHT: {cost}")
```

```

        clean('B')
    else:
        print("Location B is already clean.")
else:
    print("Location A is already clean.")
    if status_input_complement == '1':
        print("Location B is Dirty.")
        print("Moving right to Location B.")
        cost += 1 # Cost for moving right
        print(f"COST for moving RIGHT: {cost}")
        clean('B')
    else:
        print("Location B is already clean.")

else: # Vacuum is placed in Location B
    print("Vacuum is placed in Location B.")
    if status_input == '1':
        print("Location B is Dirty.")
        clean('B')
    if status_input_complement == '1':
        print("Location A is Dirty.")
        print("Moving left to Location A.")
        cost += 1 # Cost for moving left
        print(f"COST for moving LEFT: {cost}")
        clean('A')
    else:
        print("Location A is already clean.")
else:
    print("Location B is already clean.")
    if status_input_complement == '1':
        print("Location A is Dirty.")
        print("Moving left to Location A.")
        cost += 1 # Cost for moving left
        print(f"COST for moving LEFT: {cost}")
        clean('A')

```

```

else:
    print("Location A is already clean.")

# Done cleaning
print("GOAL STATE: ")
print(goal_state)
print("Performance Measurement: " + str(cost))

# Output
print('OUTPUT:')

print(' Vinayak H (1BM22CS328):')
vacuum_world()

```

OUTPUT:

```

Vinayak H (1BM22CS328):
Enter Location of Vacuum (A or B): A
Enter status of A (0 for Clean, 1 for Dirty): 1
Enter status of B (0 for Clean, 1 for Dirty): 1
Initial Location Condition: {'A': '0', 'B': '0'}
Vacuum is placed in Location A.
Location A is Dirty.
Location A has been Cleaned. Cost: 1
Location B is Dirty.
Moving right to Location B.
COST for moving RIGHT: 2
Location B has been Cleaned. Cost: 3
GOAL STATE:
{'A': '0', 'B': '0'}
Performance Measurement: 3

```

Program 3 - 8 Puzzle Using BFS and DFS

Algorithm

Weeks -3
18/10/24

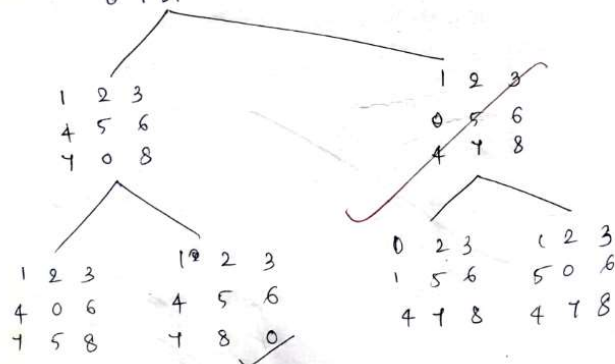
② 8-Puzzle Game:

① BFS \Rightarrow
 Let fringe be the list containing the initial state

Loop
 If fringe is empty then return failure
 Node \leftarrow remove-first (fringe)
 If node is a goal
 then return the path from initial state to node
 else generate all successors of Node, and
 add generated node to the back of fringe

End loop

Input: 1 2 3
4 5 6
0 7 8



BFS moves to solve the puzzle : 2

② DFS \Rightarrow

Let fringe be the list containing the initial state

Loop

If fringe is empty then return failure

Node \leftarrow remove-first (fringe)

If Node is a goal

then return the path from initial state to first Node

else generate all successors of Node, and
 add generated node to the back of fringe

End loop

Output:

1 2 3

4 5 6

0 7 8

1 2 3

4 5 6

7 0 8

1 2 3

4 0 6

7 8 0

DFS moves to solve the puzzle : 2

Code(BFS) :

8 puzzle problem using BFS technique

prompt: solve 8-puzzle problem using BFS

```
from collections import deque
```

```
def solve_8puzzle_bfs(initial_state):
```

```
    def find_blank(state):
```

```
        """Finds the row and column of the blank tile."""
```

```
        for row in range(3):
```

```
            for col in range(3):
```

```
                if state[row][col] == 0:
```

```
                    return row, col
```

```
    def get_neighbors(state):
```

```
        """Generates possible neighbor states by moving the blank tile."""
```

```
        row, col = find_blank(state)
```

```
        neighbors = []
```

```
        if row > 0:
```

```
            new_state = [row[:] for row in state]
```

```
            new_state[row][col], new_state[row - 1][col] = new_state[row - 1][col],
```

```
            new_state[row][col]
```

```
            neighbors.append(new_state)
```

```
        if row < 2:
```

```
            new_state = [row[:] for row in state]
```

```
            new_state[row][col], new_state[row + 1][col] = new_state[row + 1][col],
```

```
            new_state[row][col]
```

```
            neighbors.append(new_state)
```

```
        if col > 0:
```

```
            new_state = [row[:] for row in state]
```

```
            new_state[row][col], new_state[row][col - 1] = new_state[row][col - 1],
```

```
            new_state[row][col]
```

```

        neighbors.append(new_state)
    if col < 2:
        new_state = [row[:] for row in state]
        new_state[row][col], new_state[row][col + 1] = new_state[row][col + 1],
new_state[row][col]
        neighbors.append(new_state)
    return neighbors

goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]
queue = deque([(initial_state, [])])
visited = set()

while queue:
    current_state, path = queue.popleft()
    if current_state == goal_state:
        return path + [current_state]

    visited.add(tuple(map(tuple, current_state)))
    for neighbor in get_neighbors(current_state):
        if tuple(map(tuple, neighbor)) not in visited:
            queue.append((neighbor, path + [current_state]))

return None # No solution found

# Example usage:
initial_state = [[1, 2, 3], [4, 0, 6], [7, 5, 8]]
solution = solve_8puzzle_bfs(initial_state)

if solution:
    print("Solution found:")
    for state in solution:
        for row in state:
            print(row)
        print()
else:
    print("No solution found.")

```

Output Snapshot

Solution found:

[1, 2, 3]

[4, 0, 6]

[7, 5, 8]

[1, 2, 3]

[4, 5, 6]

[7, 0, 8]

[1, 2, 3]

[4, 5, 6]

[7, 8, 0]

Code(DFS):

```
from collections import deque
```

```
def solve_8puzzle_dfs(initial_state):
```

```
    def find_blank(state):
```

```
        """Finds the row and column of the blank tile."""
```

```
        for row in range(3):
```

```
            for col in range(3):
```

```
                if state[row][col] == 0:
```

```
                    return row, col
```

```
    def get_neighbors(state):
```

```
        """Generates possible neighbor states by moving the blank tile."""
```

```
        row, col = find_blank(state)
```

```
        neighbors = []
```

```
        directions = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Up, Down, Left, Right
```

```
        for dr, dc in directions:
```

```
            new_row, new_col = row + dr, col + dc
```

```
            if 0 <= new_row < 3 and 0 <= new_col < 3:
```

```
                new_state = [r[:] for r in state]
```

```
                new_state[row][col], new_state[new_row][new_col] =
```

```
new_state[new_row][new_col], new_state[row][col]
```



```

        neighbors.append(new_state)
    return neighbors

goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]
stack = [(initial_state, [])]
visited = set()

while stack:
    current_state, path = stack.pop()
    state_tuple = tuple(map(tuple, current_state)) # Convert to tuple for set
    if state_tuple in visited:
        continue
    visited.add(state_tuple)

    if current_state == goal_state:
        return path + [current_state]

    for neighbor in get_neighbors(current_state):
        stack.append((neighbor, path + [current_state]))

return None # No solution found

# Example usage:
initial_state = [[1, 2, 3], [4, 5, 6], [0, 7, 8]]
solution = solve_8puzzle_dfs(initial_state)

if solution:
    print("Solution found:")
    for state in solution:
        for row in state:
            print(row)
        print()
else:
    print("No solution found.")

```

OUTPUT:

Solution found:

[1, 2, 3]

[4, 5, 6]

[0, 7, 8]

[1, 2, 3]

[4, 5, 6]

[7, 0, 8]

[1, 2, 3]

[4, 5, 6]

[7, 8, 0]

Program 4 - A* Algorithm

Algorithm

Week - 4
25/10/2024

② A* Algorithm:

function A* search (problem) returns a solution or failure
 node \leftarrow a node n with $n.state = problem.initial_state$, $n.g = 0$.
 frontier \leftarrow a priority queue ordered by ascending g , only element n .

loop do
 if empty? (frontier) then return failure
 $n \leftarrow \text{pop}(\text{frontier})$
 if problem.goalTest($n.state$) then return solution(n)
 for each action a in problem.actions($n.state$) do
 $n' \leftarrow \text{child_state}(\text{problem}, n, a)$
 insert(n' , $g(n') + h(n')$, frontier).

State space Tree: ① Manhattan.

initial

1	2	3
4	5	6
0	7	8

goal

1	2	3
4	5	6
7	8	0

State space tree diagram showing nodes and their Manhattan distances (h values). The root node has h=2. Its children have h=4 and h=4. The child with h=4 has children with h=2 and h=4. The child with h=2 is the goal state.

① M8 placed:

State space tree diagram showing nodes and their Manhattan distances (h values). The root node has h=2. Its children have h=4 and h=4. The child with h=4 has children with h=2 and h=4. The child with h=2 is the goal state.

Code:

Manhattan Distance

#Manhattan Distance

import heapq

class PuzzleState:

def __init__(self, board, g=0):

self.board = board

self.g = g # Cost from start to this state

self.zero_pos = board.index(0) # Position of the empty space

```

def h(self):
    # Calculate the Manhattan distance
    distance = 0
    for i in range(9):
        if self.board[i] != 0:
            target_x, target_y = divmod(self.board[i] - 1, 3)
            current_x, current_y = divmod(i, 3)
            distance += abs(target_x - current_x) + abs(target_y - current_y)
    return distance

def f(self):
    return self.g + self.h()

def get_neighbors(self):
    neighbors = []
    x, y = divmod(self.zero_pos, 3)
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Up, Down, Left, Right
    for dx, dy in directions:
        new_x, new_y = x + dx, y + dy
        if 0 <= new_x < 3 and 0 <= new_y < 3:
            new_zero_pos = new_x * 3 + new_y
            new_board = self.board[:]
            # Swap zero with the neighboring tile
            new_board[self.zero_pos], new_board[new_zero_pos] =
new_board[new_zero_pos], new_board[self.zero_pos]
            neighbors.append(PuzzleState(new_board, self.g + 1))
    return neighbors

def a_star(initial_state, goal_state):
    open_set = []
    heapq.heappush(open_set, (initial_state.f(), 0, initial_state)) # Push (f, unique_id, state)
    came_from = {}
    g_score = {tuple(initial_state.board): 0}

    while open_set:

```

```

current_f, _, current = heapq.heappop(open_set)

if current.board == goal_state:
    return reconstruct_path(came_from, current)

for neighbor in current.get_neighbors():
    neighbor_tuple = tuple(neighbor.board)
    tentative_g_score = g_score[tuple(current.board)] + 1

    if neighbor_tuple not in g_score or tentative_g_score < g_score[neighbor_tuple]:
        came_from[neighbor_tuple] = current
        g_score[neighbor_tuple] = tentative_g_score
        # Push (f, unique_id, state)
        heapq.heappush(open_set, (neighbor.f(), neighbor.g, neighbor)) # Using g as a
tie-breaker

return None # If no solution is found

def reconstruct_path(came_from, current):
    path = []
    while current is not None:
        path.append(current.board)
        current = came_from.get(tuple(current.board), None)
    return path[::-1]

# Example usage
initial_state = PuzzleState([1, 2, 3, 4, 5, 6, 0, 7, 8])
goal_state = [1, 2, 3, 4, 5, 6, 7, 8, 0]

solution = a_star(initial_state, goal_state)
if solution:
    for step in solution:
        print(step)
else:

```

```
print("No solution found")
```

Output:

```
[1, 2, 3, 4, 5, 6, 0, 7, 8]
```

```
[1, 2, 3, 4, 5, 6, 7, 0, 8]
```

```
[1, 2, 3, 4, 5, 6, 7, 8, 0]
```

CODE:

Number of Misplaced tiles

```
import heapq
```

```
def misplaced_tiles(state, goal):
```

```
    return sum(1 for i in range(len(state)) if state[i] != 0 and state[i] != goal[i])
```

```
def get_neighbors(state):
```

```
    neighbors = []
```

```
    zero_idx = state.index(0) # Find the empty tile (represented as 0)
```

```
    row, col = divmod(zero_idx, 3)
```

```
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Up, Down, Left, Right
```

```
    for dr, dc in directions:
```

```
        new_row, new_col = row + dr, col + dc
```

```
        if 0 <= new_row < 3 and 0 <= new_col < 3:
```

```
            new_idx = new_row * 3 + new_col
```

```
            new_state = state[:]
```

```
            # Swap 0 with the neighbor
```

```
            new_state[zero_idx], new_state[new_idx] = new_state[new_idx],
```

```
            new_state[zero_idx]
```

```
            neighbors.append(new_state)
```

```
    return neighbors
```

```
def a_star(initial_state, goal_state):
```

```
    # Priority queue for A* (min-heap)
```

```
    open_set = []
```

```

heapq.heappush(open_set, (0, initial_state)) # (priority, state)

# Dictionaries to store the cost and parent of each state
g_cost = {tuple(initial_state): 0} # Cost from start to current state
parent = {tuple(initial_state): None} # To reconstruct the path

while open_set:
    # Get the state with the lowest  $f(n) = g(n) + h(n)$ 
    _, current = heapq.heappop(open_set)

    # If we reach the goal, reconstruct the path
    if current == goal_state:
        return reconstruct_path(parent, current)

    for neighbor in get_neighbors(current):
        neighbor_tuple = tuple(neighbor)
        tentative_g_cost = g_cost[tuple(current)] + 1

        # If this path is better, update costs and add to open set
        if neighbor_tuple not in g_cost or tentative_g_cost < g_cost[neighbor_tuple]:
            g_cost[neighbor_tuple] = tentative_g_cost
            f_cost = tentative_g_cost + misplaced_tiles(neighbor, goal_state)
            heapq.heappush(open_set, (f_cost, neighbor))
            parent[neighbor_tuple] = current

return None # No solution found

# Helper function to reconstruct the path from start to goal
def reconstruct_path(parent, state):
    path = []
    while state is not None:
        path.append(state)
        state = parent[tuple(state)]
    return path[::-1] # Reverse the path

# Main function

```

```

if __name__ == "__main__":
    # Define the initial state and goal state
    initial_state = [1, 2, 3, 0, 4, 6, 7, 5, 8] # 0 represents the empty tile
    goal_state = [1, 2, 3, 4, 5, 6, 7, 8, 0]
    solution = a_star(initial_state, goal_state)

    if solution:
        print("Solution found:")
        for step in solution:
            print_board(step)
            print()
    else:
        print("No solution exists.")
# Helper function to print the 8-puzzle board
def print_board(state):
    for i in range(0, 9, 3):
        print(state[i:i + 3])

```

OUTPUT:

Solution found:

[1, 2, 3]

[0, 4, 6]

[7, 5, 8]

[1, 2, 3]

[4, 0, 6]

[7, 5, 8]

[1, 2, 3]

[4, 5, 6]

[7, 0, 8]

[1, 2, 3]

[4, 5, 6]

[7, 8, 0]

PROGRAM 5:HILL CLIMBING(N-QUEENS)

Algorithm

Week-4
8/11/2024

Lab-5

Implement Hill Climbing Algo to solve N-Queens Problem

N-Queens Problem: In a $n \times n$ grid, place a queen such that there should be only one queen in the row and only one queen in a column, and one queen in the diagonal.

function hillclimbing (problem) returns a state that is least maximum

current \leftarrow makeNode (problem, initial_state)

loop do

 neighbours \leftarrow A highest value successor of current

 if neighbours := VALUE \leq current.value then return

 current_state

 current-neighbours

Steps :-

- (i) Initial state
- (ii) Evaluation function
- (iii) Generate Neighbours
- (iv) Select Best solution
- (v) Move to next neighbour
- (vi) Repeat.

\Rightarrow State Space Tree

CODE:

```
def count_conflicts(state):
    conflicts = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j]:
                conflicts += 1
            if abs(state[i] - state[j]) == abs(i - j):
                conflicts += 1
```

```
return conflicts
```

```
def generate_neighbors(state):  
    neighbors = []  
    n = len(state)  
    for i in range(n):  
        for j in range(i + 1, n):  
            neighbor = state[:]   
            neighbor[i], neighbor[j] = neighbor[j], neighbor[i] # Swap positions of queens i  
            and j  
            neighbors.append(neighbor)  
    return neighbors
```

```
def hill_climbing(n, initial_state):  
    state = initial_state  
    while True:  
        current_conflicts = count_conflicts(state)  
        if current_conflicts == 0:  
            return state  
        neighbors = generate_neighbors(state)  
        best_neighbor = None  
        best_conflicts = float('inf')  
        for neighbor in neighbors:  
            conflicts = count_conflicts(neighbor)  
            if conflicts < best_conflicts:  
                best_conflicts = conflicts  
                best_neighbor = neighbor  
        if best_conflicts < current_conflicts:  
            state = best_neighbor  
        else:  
            return None  
print('Vinayak H (1BM22CS328):')
```

```
def get_user_input(n):  
    while True:
```

```

try:
    user_input = input(f"Enter the row positions for the queens (space-separated
integers between 0 and {n-1}): ")
    initial_state = list(map(int, user_input.split()))
    if len(initial_state) != n or any(x < 0 or x >= n for x in initial_state):
        print(f"Invalid input. Please enter exactly {n} integers between 0 and {n-1}.")
        continue
    return initial_state
except ValueError:
    print(f"Invalid input. Please enter a list of {n} integers.")

```

```
n = 4
```

```
initial_state = get_user_input(n)
```

```
solution = hill_climbing(n, initial_state)
```

```
if solution:
```

```
    print("Solution found!")
```

```
    for row in range(n):
```

```
        board = ['Q' if col == solution[row] else '.' for col in range(n)]
```

```
        print(' '.join(board))
```

```
else:
```

```
    print("No solution found (stuck in local minimum).")
```

OUTPUT :

Vinayak H (1BM22CS328):

Enter the row positions for the queens (space-separated integers between 0 and 3): 3 1 2 0

Solution found!

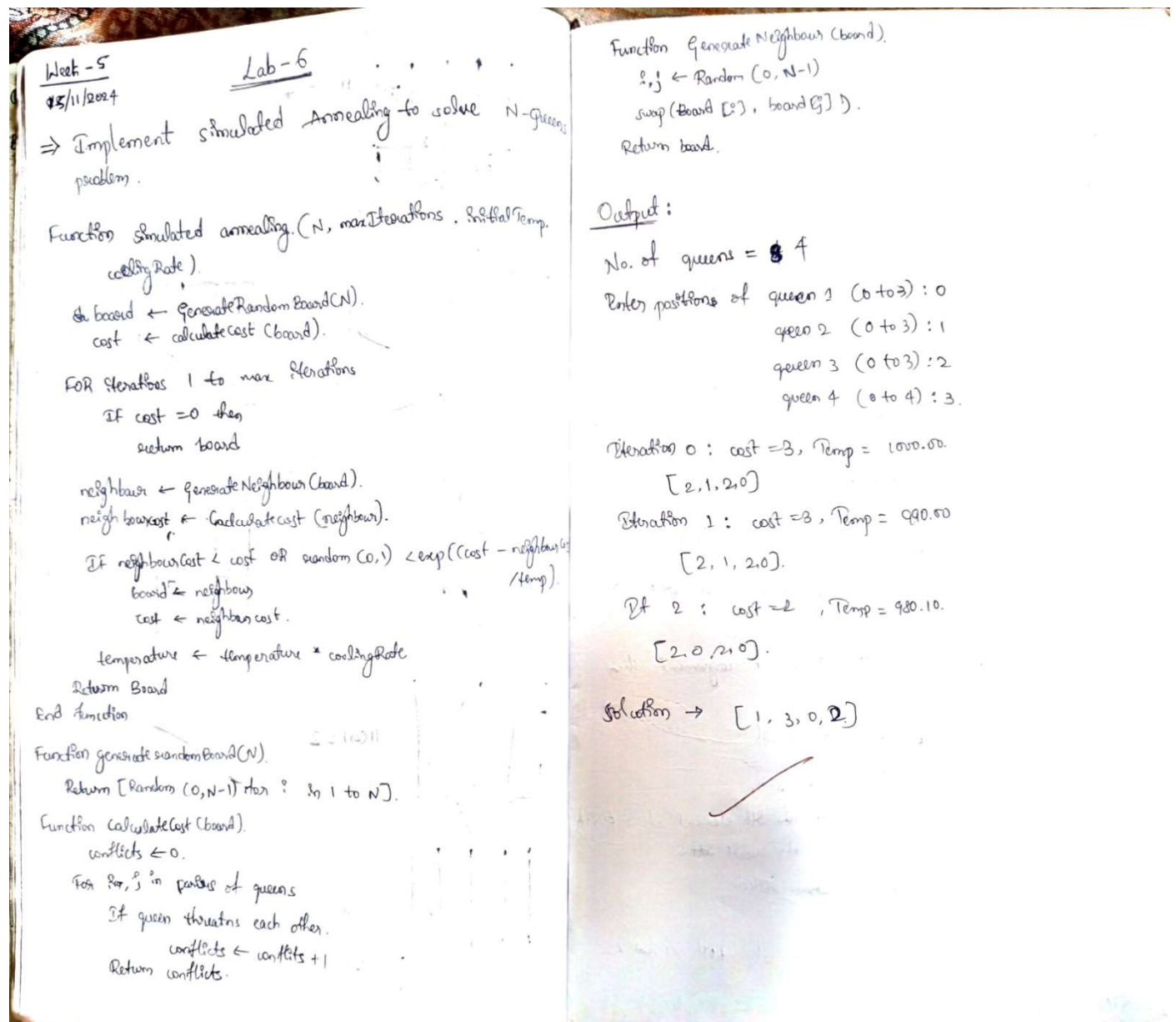
```
. Q . .
```

```
. . . Q
```

```
Q . . .
```

```
. . Q .
```

PROGRAM 6:SIMULATED ANNEALING ALGORITHM



CODE:

```
import random
```

```
import math
```

```
def calculate_conflicts(board):
```

```
    conflicts = 0
```

```
    n = len(board)
```

```

for i in range(n):
    for j in range(i + 1, n):
        if board[i] == board[j]:
            conflicts += 1
        elif abs(board[i] - board[j]) == abs(i - j):
            conflicts += 1
return conflicts

```

```

def generate_neighbor(board):

```

```

    n = len(board)
    new_board = board[:]

    col = random.randint(0, n - 1)

    current_row = new_board[col]
    possible_rows = set(range(n)) - {current_row}

```

```

    valid_rows = set()
    for row in possible_rows:
        valid = True
        for c in range(n):
            if c != col and abs(row - new_board[c]) == abs(col - c):
                valid = False
                break
        if valid:
            valid_rows.add(row)

```

```

    if valid_rows:
        new_board[col] = random.choice(list(valid_rows))
    return new_board

```

```

def simulated_annealing(n, initial_state, max_iterations=10000, initial_temp=1000,
cooling_rate=0.99):

```

```

"""
Simulated Annealing to solve the N-Queens problem.
"""

current_state = initial_state
current_conflicts = calculate_conflicts(current_state)
temperature = initial_temp

for iteration in range(max_iterations):
    if current_conflicts == 0:
        return current_state

    neighbor = generate_neighbor(current_state)
    neighbor_conflicts = calculate_conflicts(neighbor)

    delta = current_conflicts - neighbor_conflicts

    if delta > 0 or random.random() < math.exp(delta / temperature):
        current_state = neighbor
        current_conflicts = neighbor_conflicts

    temperature *= cooling_rate

return None

def print_solution(board):
    """
    Prints the solution board in a human-readable format.
    """
    n = len(board)
    for row in range(n):
        board_row = ['Q' if col == board[row] else '.' for col in range(n)]
        print(' '.join(board_row))

print('Vinayak H (1BM22CS328):
')

```

```

n = int(input("Enter the number of queens: "))
initial_state_input = input(f"Enter the initial state (a list of {n} integers representing the
row positions of queens in each column): ")

initial_state = list(map(int, initial_state_input.strip('[]').split(',')))

if len(initial_state) != n or any(queen < 0 or queen >= n for queen in initial_state):
    print("Invalid initial state! Please make sure it's a list of integers between 0 and n-1.")
else:
    solution = simulated_annealing(n, initial_state)

    if solution:
        print("Solution found:")
        print_solution(solution)
    else:
        print("No solution found.")

```

OUTPUT :

Vinayak H (1BM22CS328):

Enter the number of queens: 8

Enter the initial state (a list of 8 integers representing the row positions of queens in each column): 0,1,2,3,4,5,6,7

Solution found:

```

.....Q..
...Q....
.....Q.
Q.....
.....Q
.Q.....
....Q...
..Q.....

```

// Output:

for 8 queens by taking random inputs

Initial state Board:

.	Q	.	.
.	Q	.
.	●	.	.	.	Q	.	.	.
.	.	.	Q
.	Q
Q
.	Q
.	.	Q

solution found!

.	.	Q
.	Q	.	.
.	Q
.	Q	.
.	.	.	.	Q
Q
.	Q
.	.	.	Q

Date _____
Page _____

PROGRAM 7: UNIFICATION IN FOL

ALGORITHM

Week-6
02/11/24

Lab-7

Unification Algorithm

Algorithm: $\text{Unify}(\Psi_1, \Psi_2)$.

Step 1: If Ψ_1 & Ψ_2 are is a variable or constant, then:

a) If Ψ_1 or Ψ_2 are identical, then return NIL

b) else return $\{\Psi_1/\Psi_2\}$.

Else if Ψ_1 is a variable.

a. then if Ψ_1 occur in Ψ_2 , then return Failure

b. Else return $\{\Psi_2/\Psi_1\}$.

c) Else if Ψ_2 is a variable,

a. If Ψ_2 occurs in Ψ_1 , then return Failure

b. Else return $\{\Psi_1/\Psi_2\}$.

d) else return failure.

Step 2: If the predicate symbol in Ψ_1 and Ψ_2 are not same, then return Failure

Step 3: If Ψ_1 & Ψ_2 have different no. of arguments then return failure

Step 4: set substitutions set (SUBST) to nil.

Step 5: For $i=1$ to np . of elements in Ψ_1 ,

a) Call unify function with the i th element of Ψ_1 & i th element of Ψ_2 , and put the result into S .

b) If $S = \text{failure}$ then return failure

c) If $S \neq \text{NIL}$ then do.

a. Apply S to the remainder of both Ψ_1 and Ψ_2

b. SUBST = $\text{append}(S, \text{SUBST})$.

Step 6: Return SUBST.

Output:

Expression $a = \text{"Eats}(x, \text{Apple})"$

Expression $b = \text{"Eats}(Riya, y)"}$

2/p

Unification Successful:

$\{x: \text{"Riya"}, y: \text{"Apple"}\}$

Sum
22/11/24

CODE:

#Implement unification in First Order Logic

```
def is_variable(x):
```

```
    """Checks if x is a variable (assuming variables are single lowercase letters)."""
```

```
    return isinstance(x, str) and x.islower() and len(x) == 1
```

```
def occurs_check(var, term):
```

```
    """Checks if a variable occurs in a term (used to avoid circular unification)."""
```

```
    if var == term:
```

```
        return True
```

```
    if isinstance(term, tuple): # If term is a function (tuple), check its arguments.
```

```
        return any(occurs_check(var, t) for t in term)
```

```
    return False
```

```
def unify(x, y, substitution=None):
```

```
    """Unifies two terms x and y, applying substitutions."""
```

```
    if substitution is None:
```

```
        substitution = {}
```

```
    # Case 1: If both terms are the same, no unification needed
```

```
    if x == y:
```

```
        return substitution
```

```
    # Case 2: If x is a variable, try to unify
```

```
    elif is_variable(x):
```

```
        if x in substitution:
```

```
            return unify(substitution[x], y, substitution)
```

```
        elif occurs_check(x, y):
```

```
            raise ValueError(f"Unification fails due to occurs check for {x} in {y}")
```

```

else:
    substitution[x] = y
    return substitution

# Case 3: If y is a variable, try to unify
elif is_variable(y):
    return unify(y, x, substitution)

# Case 4: If both terms are compound (functions), unify their components
elif isinstance(x, tuple) and isinstance(y, tuple):
    if x[0] != y[0]:
        raise ValueError(f"Unification fails: {x[0]} != {y[0]}")
    # Recursively unify arguments
    for a, b in zip(x[1:], y[1:]):
        substitution = unify(a, b, substitution)
    return substitution

# Case 5: Unification fails if x and y have no other cases
else:
    raise ValueError(f"Unification fails: {x} cannot be unified with {y}")

def apply_substitution(term, substitution):
    """Applies the substitution to the term."""
    if isinstance(term, str):
        return substitution.get(term, term)
    elif isinstance(term, tuple):
        return (term[0], *[apply_substitution(t, substitution) for t in term[1:]])
    return term

def parse_term(term_str):
    """Parses a string representation of a term into a Python data structure."""
    term_str = term_str.strip()

    # Case 1: If it's a variable (single lowercase letter)
    if term_str.islower() and len(term_str) == 1:

```

```

    return term_str

# Case 2: If it's a constant (any non-empty string, for example 'apple')
if term_str.isalpha():
    return term_str

# Case 3: If it's a function, e.g., 'f(x, y)'
if term_str.startswith('f(') and term_str.endswith(')'):
    func_str = term_str[2:-1] # Remove 'f(' and ')'
    parts = func_str.split(',')
    return ('f', *[parse_term(p.strip()) for p in parts]) # Function name, arguments

# If none of these, raise an error
raise ValueError(f"Invalid term format: {term_str}")
print(Vinayak H (1BM22CS328):)

def main():
    print("Enter two terms to unify (e.g., f(x, y), f(a, b)):")
    term1_str = input("Enter first term: ")
    term2_str = input("Enter second term: ")

    try:
        term1 = parse_term(term1_str)
        term2 = parse_term(term2_str)

        print(f"Unifying terms: {term1} and {term2}")
        substitution = unify(term1, term2)

        # Apply substitution to both terms to get the unified expression
        unified_term1 = apply_substitution(term1, substitution)
        unified_term2 = apply_substitution(term2, substitution)

        print("Unification successful!")
        print("Substitution:", substitution)
        print("Unified expression:")

```

```
print(f"Term 1 after substitution: {unified_term1}")
```

```
print(f"Term 2 after substitution: {unified_term2}")
```

```
except ValueError as e:
```

```
    print("Unification failed:", e)
```

```
# Run the program
```

```
if __name__ == "__main__":
```

```
    main()
```

OUTPUT :

Vinayak H(1BM22CS328):

Enter two terms to unify (e.g., f(x, y), f(a, b)):

Enter first term: f(x,car)

Enter second term: f(bike,y)

Unifying terms: ('f', 'x', 'car') and ('f', 'bike', 'y')

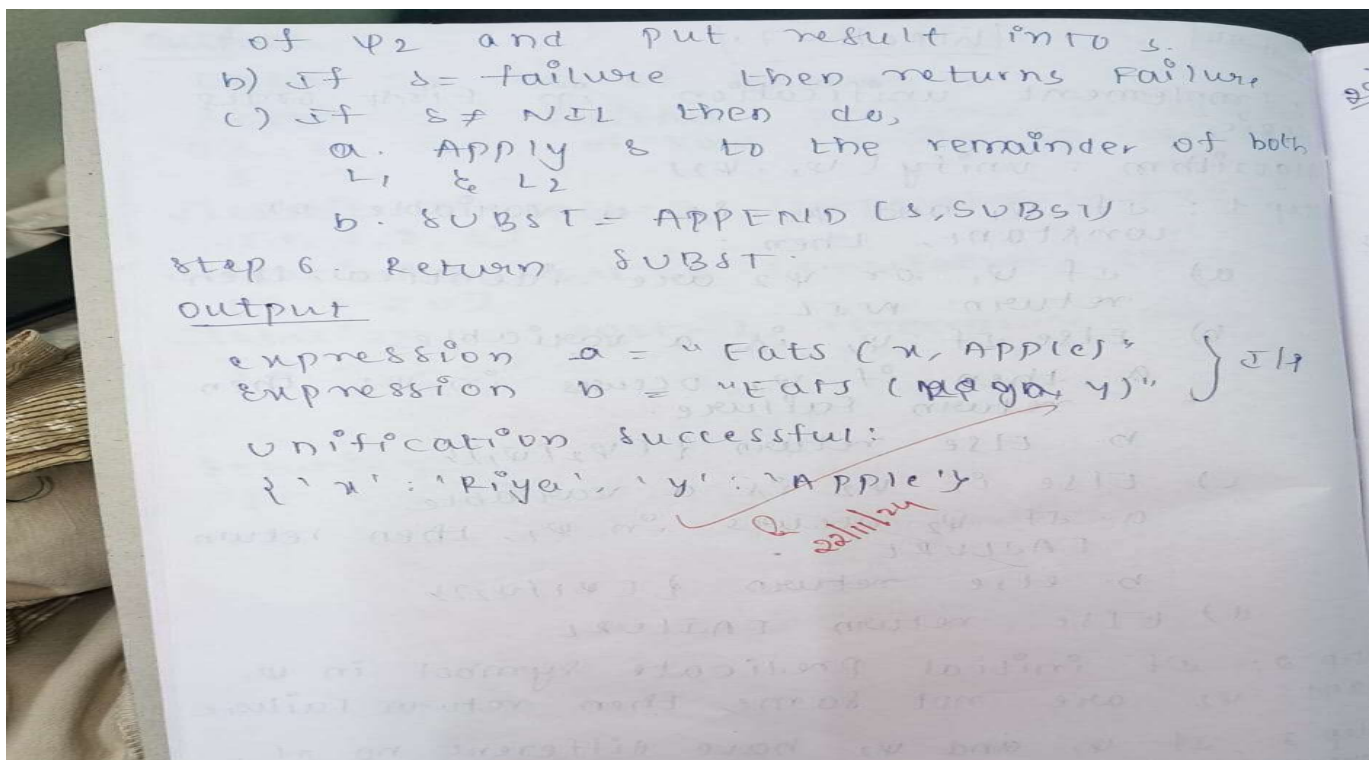
Unification successful!

Substitution: {'x': 'bike', 'y': 'car'}

Unified expression:

Term 1 after substitution: ('f', 'bike', 'car')

Term 2 after substitution: ('f', 'bike', 'car')



PROGRAM 8: FORWARD CHAINING ALGORITHM

Week-4
29/11/2024

Lab-8

Forward Reasoning Algorithm:

function FOR-FC-ASK (KB, α) returns a substitution or false
Inputs: KB, the Knowledgebase, a set of first order definite clauses α , the query, an atomic sentence

Local variables: new, the new sentences integrated on each iteration.

repeat until new is empty.

new $\leftarrow \{ \}$.

for each rule in KB do

$(p_1 \wedge \dots \wedge p_n \rightarrow q) \leftarrow$ standardize variables (rule)

for each θ such that SUBST($\theta, p_1 \wedge \dots \wedge p_n$) =

SUBST($\theta, p_1' \wedge \dots \wedge p_n'$)

for some $p_1' \dots p_n'$ in KB.

$q' \leftarrow$ SUBST(θ, q).

if q' does not unify with some sentence already in KB or new then add q' to new.

$\phi \leftarrow$ unify(q', α)

if ϕ is not fail then return ϕ .

add new to KB.

return false

Output:

Rule applied: { 'conditions': { 'cough', 'fever' }

'conclusion': 'flu' }

New fact entered: flu

Final facts = { 'cough', 'flu', 'fever' }

inferred facts = { 'flu' }.

a) Occupation (Emily, Surgeon) \vee Occupation (Emily, Lawyer)

b) Occupation (Joe, Doctor) $\wedge \exists o (o \neq \text{Joe} \wedge \text{Occupation}(\text{Joe}, o))$

c) $\forall P (\text{Occupation}(P, \text{surgeon}) \rightarrow \neg \text{Occupation}(P, \text{Doctor}))$

d) $\neg \exists P (\text{Occupation}(P, \text{layer}) \wedge \text{customer}(\text{Joe}, P))$

e) $\exists P (\text{Occupation}(P, \text{Lawyer}) \wedge \text{Buss}(P, \text{Emily}))$

f) $\exists P (\text{Occupation}(P, \text{Lawyer}) \wedge \forall C (\text{customer}(C, P) \rightarrow \text{Occupation}(C, \text{Doctor})))$

g) $\forall P (\text{Occupation}(P, \text{surgeon}) \rightarrow \exists C (\text{Occupation}(C, \text{Lawyer}) \wedge \text{customer}(P, C)))$

9/11/24

CODE:

```
knowledge_base = {
    "facts": {
        "American(Robert)": True,
        "Enemy(A, America)": True,
        "Owns(A, T1)": True,
        "Missile(T1)": True,
    },
    "rules": [
        {"if": ["Missile(x)", "then": ["Weapon(x)"]},
        {"if": ["Enemy(x, America)", "then": ["Hostile(x)"]},
        {"if": ["Missile(x)", "Owns(A, x)", "then": ["Sells(Robert, x, A)"]},
        {
            "if": ["American(p)", "Weapon(q)", "Sells(p, q, r)", "Hostile(r)",
            "then": ["Criminal(p)"],
        },
    ],
}
```

```
def forward_chaining(kb):
    facts = kb["facts"].copy()
    rules = kb["rules"]

    inferred = set()

    while True:
```

```
new_inferences = set()
```

```
for rule in rules:
```

```
    if_conditions = rule["if"]
```

```
    then_conditions = rule["then"]
```

```
    substitutions = {}
```

```
    all_conditions_met = True
```

```
    for condition in if_conditions:
```

```
        predicate, args = condition.split("(")
```

```
        args = args[:-1].split(",")
```

```
        matched = False
```

```
        for fact in facts:
```

```
            fact_predicate, fact_args = fact.split("(")
```

```
            fact_args = fact_args[:-1].split(",")
```

```
            if predicate == fact_predicate and len(args) == len(fact_args):
```

```
                temp_subs = {}
```

```
                for var, val in zip(args, fact_args):
```

```
                    if var.islower():
```

```
                        if var in temp_subs and temp_subs[var] != val:
```

```
                            break
```

```
                        temp_subs[var] = val
```

```
                    elif var != val:
```

```
                        break
```

```
            else:
```

```
                matched = True
```

```
                substitutions.update(temp_subs)
```

```
                break
```

```
    if not matched:
```

```
        all_conditions_met = False
```

```
        break
```



```

    if all_conditions_met:
        for condition in then_conditions:
            predicate, args = condition.split("(")
            args = args[:-1].split(",")
            new_fact = predicate + "(" + ",".join(substitutions.get(arg, arg) for arg in args)
+ ")"

            new_inferences.add(new_fact)

    if new_inferences - inferred:
        inferred.update(new_inferences)
        facts.update({fact: True for fact in new_inferences})
    else:
        break

return inferred

result = forward_chaining(knowledge_base)
print(' (1BM22CS328):')

if "Criminal(Robert)" in result:
    print("Proved: Robert is a criminal.")
else:
    print("Could not prove that Robert is a criminal.")

```

OUTPUT:

```

(1BM22CS328):
Proved: Robert is a criminal.

```

PROGRAM 9:ALPHA BETA PRUNING ALGORITHM

Week-8

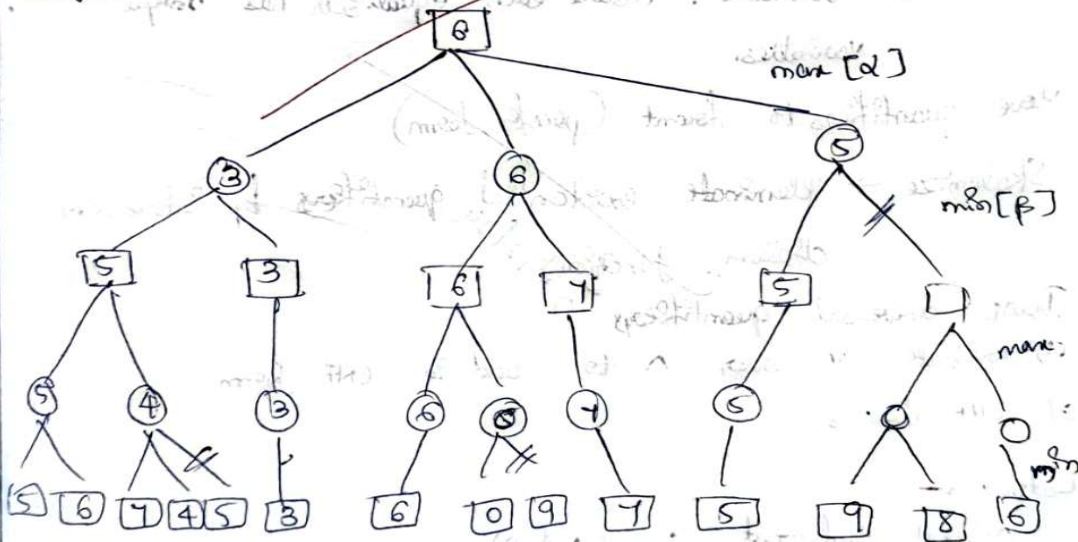
Lab - 10

Alpha - Beta Pruning :

Algorithm:

- 1) Alpha - Beta proposes to compute find the optimal selection without finding looking at the every node in the given tree.
- 2) Max contains α (alpha), min contains β . bound during calculation.
- 3) In both min and max node we return when $\alpha \geq \beta$ which computes with its parent node only.
- 4) Both min-max and α - β cutoff gives same path.
- 5) α - β - gives optimal path as it takes less time to get the value of the root node.

Output \Rightarrow



CODE:

```
import math
```

```
def alpha_beta_pruning(depth, node_index, is_maximizing_player, values, alpha, beta,
max_depth):
```

```
    # Base case: when the maximum depth is reached
```

```
    if depth == max_depth:
```

```
        return values[node_index]
```

```
    if is_maximizing_player:
```

```
        best = -math.inf
```

```
        # Recur for left and right children
```

```
        for i in range(2):
```

```
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, False, values, alpha, beta,
max_depth)
```

```
            best = max(best, val)
```

```
            alpha = max(alpha, best)
```

```
        # Prune the remaining nodes
```

```
        if beta <= alpha:
```

```
            break
```

```
        return best
```

```
    else:
```

```
        best = math.inf
```

```
        # Recur for left and right children
```

```
        for i in range(2):
```

```
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, True, values, alpha, beta,
max_depth)
```

```
            best = min(best, val)
```

```
            beta = min(beta, best)
```

```

# Prune the remaining nodes
if beta <= alpha:
    break
return best

```

Example usage

```
if __name__ == "__main__":
```

```
    # Example tree represented as a list of leaf node values
```

```
    values = [3, 5, 6, 9, 1, 2, 0, -1]
```

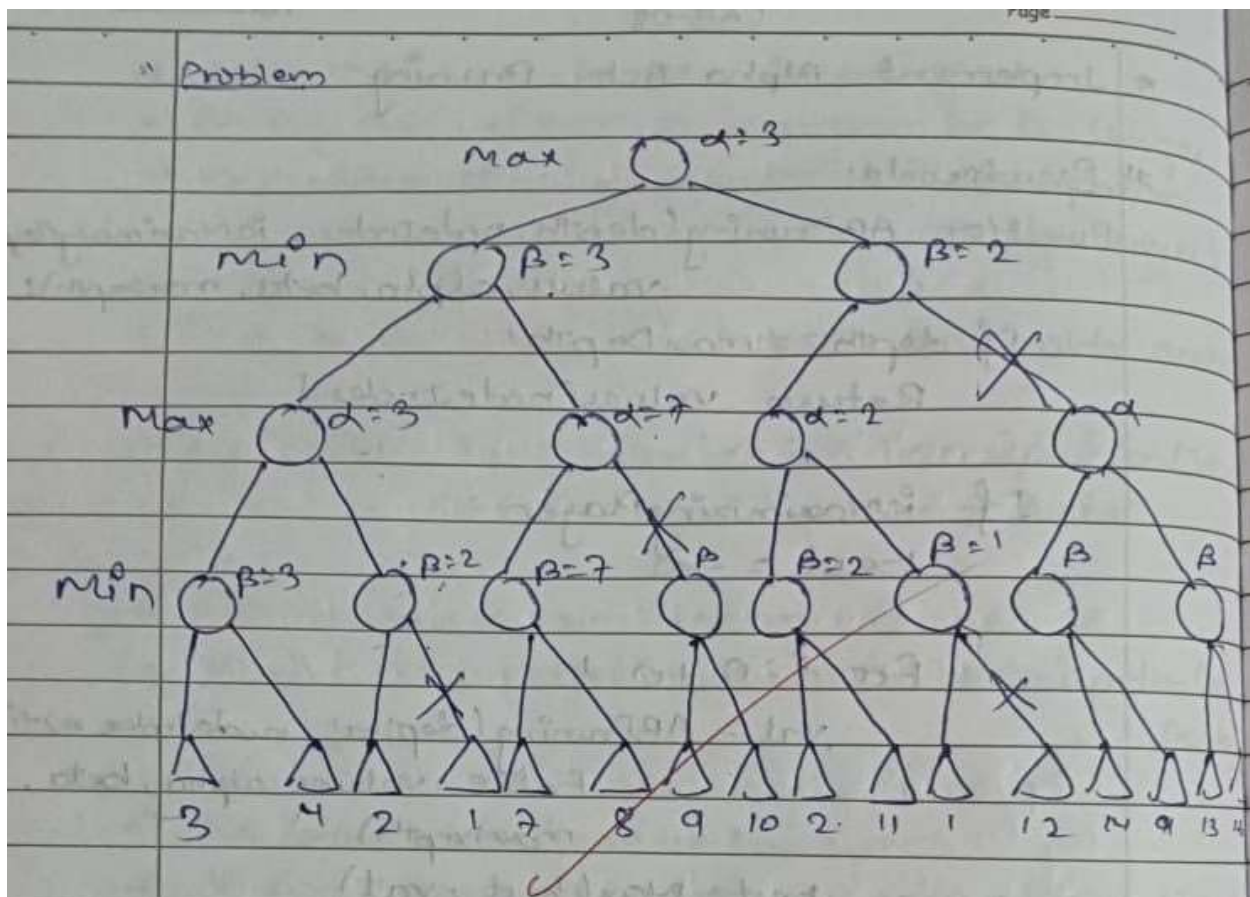
```
    max_depth = 3 # Height of the tree
```

```
    result = alpha_beta_pruning(0, 0, True, values, -math.inf, math.inf, max_depth)
```

```
    print("The optimal value is:", result)
```

OUTPUT :

The optimal value is: 5



PROGRAM 10: PROVE A QUERY USING RESOLUTION ALGORITHM

Week - 8
20/12/24

Lab - 9

Convert FOL to Resolution:

Algorithm -

- 1) Convert all sentences to ~~the~~ CNF
 - 2) Negate conclusion S and convert result to CNF
 - 3) Add negated conclusion S to the premise clauses.
 - 4) Repeat until contradiction or no progress is made
 - a) Select two clauses (call them parent clauses).
 - b) Resolve them together, performing all required unification.
 - c) If resolvent is the empty clause a contradiction has been found (i.e. S follows from the premises).
 - d) If not - add resolvent to the premises.
- If we succeed in step 4 we have proved the conclusion.

Eg \Rightarrow Given F.B. or premises.

- a: John likes all kinds of food
- b: Apple and vegetables are food
- c: Anything anyone eats and not dies is a food
- d: Ann likes peanuts & is still alive
- e: Larry eats everything that Ann eats.

f: Prove by resolution that John likes food.

\Rightarrow The conclusion can be proved by Resolution
Hence proved

CODE:

Example propositional logic statements in CNF

kb = [{"¬B", "¬C", "A"}, "# ¬B ∨ ¬C ∨ A

```

{"B"}, # B
{"¬D", "¬E", "C"}, #  $\neg D \vee \neg E \vee C$ 
{"E", "F"}, #  $E \vee F$ 
{"D"}, #D
{"¬F"}, #¬F

```

```
]
```

Negate the query: If the query is "A", we negate it to "¬A"

```
def negate_query(query):
```

```
    if "¬" in query:
```

```
        return query.replace("¬", "") # If it's negated, remove the negation
```

```
    else:
```

```
        return f"¬{query}" # Otherwise, add negation in front
```

Function to perform resolution on two clauses

```
def resolve(clause1, clause2):
```

```
    resolved_clauses = []
```

Try to find complementary literals

```
    for literal1 in clause1:
```

```
        for literal2 in clause2:
```

```
            # If literals are complementary (e.g., "A" and "¬A"), resolve them
```

```
            if literal1 == f"¬{literal2}" or f"¬{literal1}" == literal2:
```

```
                new_clause = (clause1 | clause2) - {literal1, literal2}
```

```
                resolved_clauses.append(new_clause)
```

```
    return resolved_clauses
```

Perform resolution-based proof

```
def resolution(kb, query):
```

```
    # Step 1: Negate the query and add it to the knowledge base
```

```
    negated_query = negate_query(query)
```

```
    kb.append({negated_query})
```

Step 2: Initialize the set of clauses

```
    new_clauses = set(frozenset(clause) for clause in kb)
```

```

while True:
    resolved_this_round = set()
    clauses_list = list(new_clauses)

    # Try to resolve every pair of clauses
    for i in range(len(clauses_list)):
        for j in range(i + 1, len(clauses_list)):
            clause1 = clauses_list[i]
            clause2 = clauses_list[j]

            # Apply resolution to the two clauses
            resolved = resolve(clause1, clause2)
            if frozenset() in resolved:
                return True # Found an empty clause (contradiction), query is provable
            resolved_this_round.update(resolved)

    # If no new clauses were added, stop
    if resolved_this_round.issubset(new_clauses):
        return False # No new clauses, query is not provable
    # Add new resolved clauses to the set
    new_clauses.update(resolved_this_round)

# Query to prove: "A"
query = (input("Enter the query:"))
result = resolution(kb, query)
print("OUTPUT:(1BM22CS328)")
print("Using Resolution to prove a query")
print(f"Is the query '{query}' provable? {'Yes' if result else 'No'}")

```

OUTPUT :

```

Enter the query:A
OUTPUT:(1BM22CS328)
Using Resolution to prove a query
Is the query 'A' provable? Yes

```


PROGRAM 11: FOL TO CNF

ALGORITHM

Propositional Logic :

Objective \rightarrow Create a KB using propositional logic and show that the given query entails the knowledge or not

Algorithm:

Function: Π -Entails (KB, α)

Lab - 11

Convert FOL to CNF.

Input First-order logic statement.

Eliminate implications : Replace $(A \rightarrow B)$ with $(\neg A \vee B)$.

Move \neg Inwards using De Morgan's Law.

Standardize variables : Ensure each equalizer has unique variables

Move quantifiers to front (prefix form)

Skolemize \rightarrow Eliminate existential quantifiers by introducing chosen function

Drop universal quantifiers

Distribute \vee over \wedge to add in CNF form

of CNF clauses

Output \rightarrow

Original Statement : $(A \wedge B) \rightarrow C$

CNF form : $\neg A / \neg B / C$.

CODE:

```
from sympy import symbols, Not, Or, And, Implies, Equivalent
from sympy.logic.boolalg import to_cnf
```

```
def fol_to_cnf(fol_expr):
```



```
"""
```

Converts a First-Order Logic (FOL) statement to Conjunctive Normal Form (CNF).

Arguments:

fol_expr: A sympy logical expression representing the FOL statement.

Returns:

The CNF equivalent of the input expression.

```
"""
```

```
# Step 1: Eliminate equivalences ( $A \leftrightarrow B$ ) using  $(A \rightarrow B) \wedge (B \rightarrow A)$ 
```

```
fol_expr = fol_expr.replace(Equivalent, lambda a, b: And(Implies(a, b), Implies(b, a)))
```

```
# Step 2: Eliminate implications ( $A \rightarrow B$ ) using  $(\neg A \vee B)$  fol_expr
```

```
= fol_expr.replace(Implies, lambda a, b: Or(Not(a), b))
```

```
# Step 3: Convert to CNF
```

```
cnf_form = to_cnf(fol_expr, simplify=True)
```

```
return cnf_form
```

```
def main():
```

```
    # Define propositional symbols instead of first-order predicates
```

```
    P = symbols("P")
```

```
    Q = symbols("Q")
```

```
    R = symbols("R")
```

```
    # Example 1:  $P \rightarrow Q$ 
```

```
    fol_expr1 = Implies(P, Q)
```

```
    print("Example 1:  $P \rightarrow Q$ ")
```

```
    print("Original FOL Expression:")
```

```
    print(fol_expr1)
```

```
    # Convert to CNF
```

```
    cnf1 = fol_to_cnf(fol_expr1)
```

```
    print("\nCNF Form:")
```

```
    print(cnf1)
```

```

# Example 2:  $(P \vee \neg Q) \rightarrow (Q \vee R)$  fol_expr2
= Implies(Or(P, Not(Q)), Or(Q, R))
print("\nExample 2:  $(P \vee \neg Q) \rightarrow (Q \vee R)$ ")
print("Original FOL Expression:")
print(fol_expr2)

# Convert to CNF
cnf2 = fol_to_cnf(fol_expr2)
print("\nCNF Form:")
print(cnf2)

if __name__ == "__main__":
    main()

```

OUTPUT:

Example 1: $P \rightarrow Q$

Original FOL Expression:

Implies(P, Q)

CNF Form:

$Q \mid \sim P$

Example 2: $(P \vee \neg Q) \rightarrow (Q \vee R)$

Original FOL Expression:

Implies($P \mid \sim Q$, $Q \mid R$)

CNF Form:

$Q \mid R$

