

**LAPORAN TUGAS KECIL 2**  
**STRATEGI ALGORITMA IF2211 IMPLEMENTASI CONVEX HULL**  
**MENGGUNAKAN ALGORITMA DIVIDE AND CONQUER**



**Pembuat:**  
**13520136 Vincent Christian Siregar**

## I. Algoritma

1. Data yang akan di olah adalah data yang berisi kumpulan titik sebanyak  $n$  (dengan notasi  $(x,y)$ ) pada bidang dua dimensi.
2. Dua titik dengan nilai absis terendah dan tertinggi diambil dari dataset (misalkan titik absis terendah  $p1$  dan titik absis tertinggi  $p2$ ). Titik  $p1$  dan  $p2$  termasuk dalam convex hull.
3. Garis yang dibentuk dari  $p1$  dan  $p2$  membagi titik-titik yang lain menjadi 2 bagian yaitu  $s1$  yang berada di sebelah kiri atas garis dan  $s2$  yang berada di sebelah kanan bawah garis.
4.  $s1$  dan  $s2$  diterapkan algoritma decrease and conquer dengan metode rekursif.
5. Titik-titik pada  $s1$  dan  $s2$  dicari jarak yang terjauh dari garis yang dibentuk antara  $p1$  dan  $p2$ . Titik yang terjauh termasuk dari convex hull (misalkan  $p3$ ). Setelah itu, titik-titik yang berada di luar garis  $p1-p3$ , dan di luar garis  $p3-p2$  dilakukan algoritma yang sama hingga tidak terdapat titik di luar garis yang dibentuk.
6. Hasil titik yang merupakan convex hull di merge dalam satu array yang menyimpan data titik-titik yang termasuk convex hull.

## II. Kode Program

myConvexHull.py

```
import math

class ConvexHull:
    def __init__(self, bucket):
        self.bucket = bucket

    def getVertices(bucket):
        #ubah input menjadi list
        array = bucket.tolist()

        #mencari index letak titik paling kiri dan paling kanan
        x = []
        for item in array:
            x.append(item[0])
        idx_min, idx_max = getMinMax(x)

        #membagi titik titik menjadi s1 dan s2
        matrix = [[1 for i in range(3)] for i in range(3)]
        matrix[0][0] = array[idx_min][0]
        matrix[0][1] = array[idx_min][1]
        matrix[1][0] = array[idx_max][0]
        matrix[1][1] = array[idx_max][1]

        s1 = []
```

```

s2 = []
for i in range(len(array)):
    matrix[2][0] = array[i][0]
    matrix[2][1] = array[i][1]
    det = getDeterminant(matrix)
    if (det > 0):
        s1.append(i)
    elif (det < 0) :
        s2.append(i)

Hull1 = RecConvexHull(idx_min,idx_max, s1, array, True)
Hull2 = RecConvexHull(idx_min,idx_max, s2, array, False)
invertArray(Hull2)

vertices = [idx_min]
for item in Hull1:
    vertices.append(item)
vertices.append(idx_max)
for item in Hull2:
    vertices.append(item)

return vertices

def getSimplices(vertices):
    simplices = []
    for i in range(len(vertices)):
        s = []
        if i != len(vertices)-1:
            s.append(vertices[i])
            s.append(vertices[i+1])
        else:
            s.append(vertices[i])
            s.append(vertices[0])
        simplices.append(s)

    return simplices

#fungsi untuk membalikan urutan array
def invertArray(array):
    for i in range(math.floor(len(array)/2)):
        temp = array[i]
        array[i] = array[len(array)-1-i]
        array[len(array)-1-i] = temp

#fungsi untuk mencari index dengan nilai min dan max pada array

```

```

def getMinMax(array):
    min = array[0]
    max = array[0]
    idx_min = 0
    idx_max = 0
    for i in range(1, len(array)):
        if array[i] < min:
            min = array[i]
            idx_min = i
        elif array[i] > max:
            max = array[i]
            idx_max = i
    return idx_min, idx_max

#fungsi untuk mencari determinan dengan menggunakan ekspansi kofaktor
def getDeterminant(matrix):
    if len(matrix) == 1:
        return matrix[0][0]
    elif len(matrix) > 1:
        sign = 1
        det = 0
        for i in range(len(matrix)):
            a = matrix[i][0]
            m = []
            for j in range(len(matrix)):
                m1 = []
                for k in range(len(matrix[0])):
                    if j != i and k != 0:
                        m1.append(matrix[j][k])
                if (len(m1) != 0):
                    m.append(m1)
            det += sign * (a * getDeterminant(m))
            sign *= -1
        return det

def DividePoint(idx1, idx2, si, bucket, isLeft):
    # inisiasi matrix untuk mencari determinan
    mat = [[1 for i in range(3)] for i in range(3)]
    mat[0][0] = bucket[idx1][0]
    mat[0][1] = bucket[idx1][1]
    mat[1][0] = bucket[idx2][0]
    mat[1][1] = bucket[idx2][1]

    s = []
    if isLeft:

```

```

        for i in si:
            mat[2][0] = bucket[int(i)][0]
            mat[2][1] = bucket[int(i)][1]
            det = getDeterminant(mat)
            if (det > 0):
                s.append(i)
        return s
    else:
        for i in si:
            mat[2][0] = bucket[int(i)][0]
            mat[2][1] = bucket[int(i)][1]
            det = getDeterminant(mat)
            if (det < 0):
                s.append(i)
        return s

def PointToLine(x1,x2,y1,y2):
    distx = x2 - x1
    disty = y2 - y1
    a = disty
    b = -distx
    c = (distx*y1) - (disty*x1)
    return (a,b,c)

def Distance(x1, y1, Line):
    d = abs((Line[0] * x1 + Line[1] * y1 + Line[2])) / (math.sqrt(Line[0]
* Line[0] + Line[1] * Line[1]))
    return d

def RecConvexHull(idx1, idx2, s, bucket, isLeft):
    if len(s) == 0:
        return []
    elif len(s) == 1:
        return s
    else:
        max = 0
        Line =
PointToLine(bucket[idx1][0],bucket[idx2][0],bucket[idx1][1],bucket[idx2][1])
        for i in s:
            idx = int(i)
            distance = Distance(bucket[idx][0], bucket[idx][1], Line)
            if (max < distance):
                max = distance
                id = idx

```

```

        s1 = DividePoint(idx1, id, s, bucket, isLeft)
        arr1 = RecConvexHull(idx1, id, s1, bucket, isLeft)
        s2 = DividePoint(id, idx2, s, bucket, isLeft)
        arr2 = RecConvexHull(id, idx2, s2, bucket, isLeft)

        arr1.append(id)
        for item in arr2:
            arr1.append(item)

        return arr1

self.vertices = getVertices(self.bucket)
self.simplices = getSimplices(self.vertices)

```

## II. Tes Program

Import code:

```

import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from myConvexHull import ConvexHull
from sklearn import datasets

```

### A. Data Iris

#### a. sepal length vs sepal width

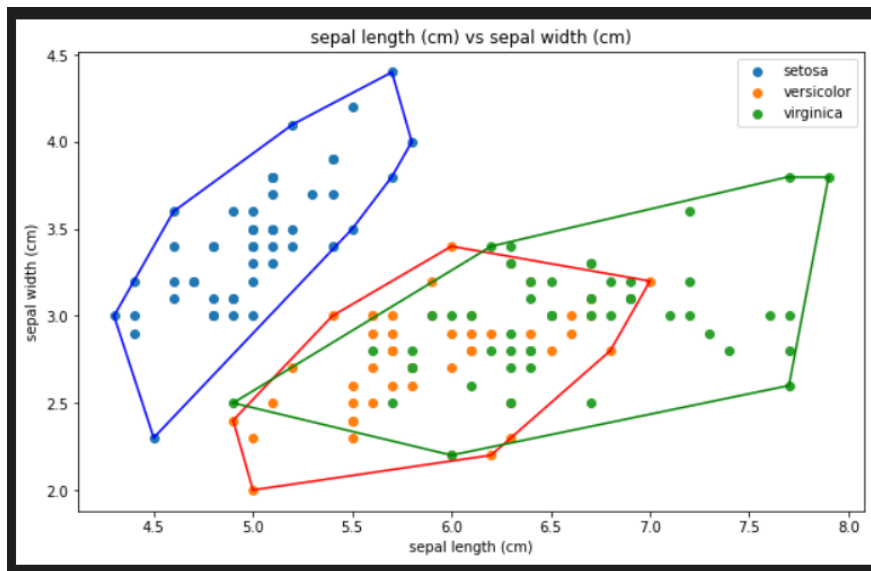
Input:

```

data = datasets.load_iris()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 0
y = 1
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[x,y]].values
    hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull.simplices:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()

```

Output:

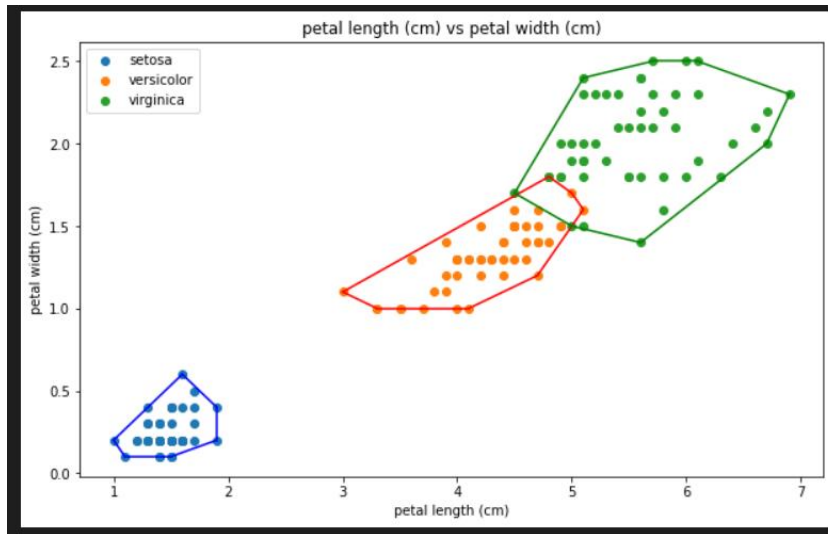


b. petal length vs petal width

Input:

```
data = datasets.load_iris()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 2
y = 3
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[x,y]].values
    hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull.simplices:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

Output:



## B. Data Wine

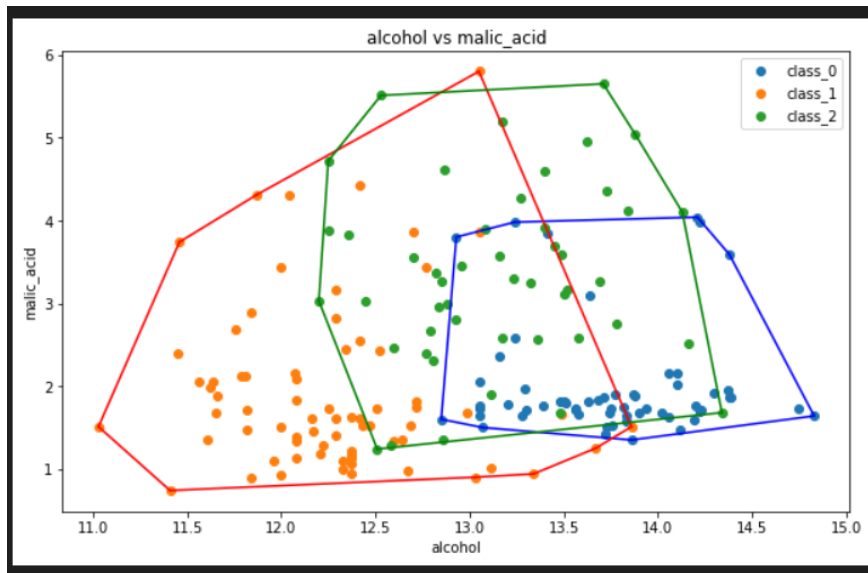
### a. alcoholic vs malic\_acid

Input:

```
data = datasets.load_wine()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 0
y = 1
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[x,y]].values
    hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull.simplices:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

Output:



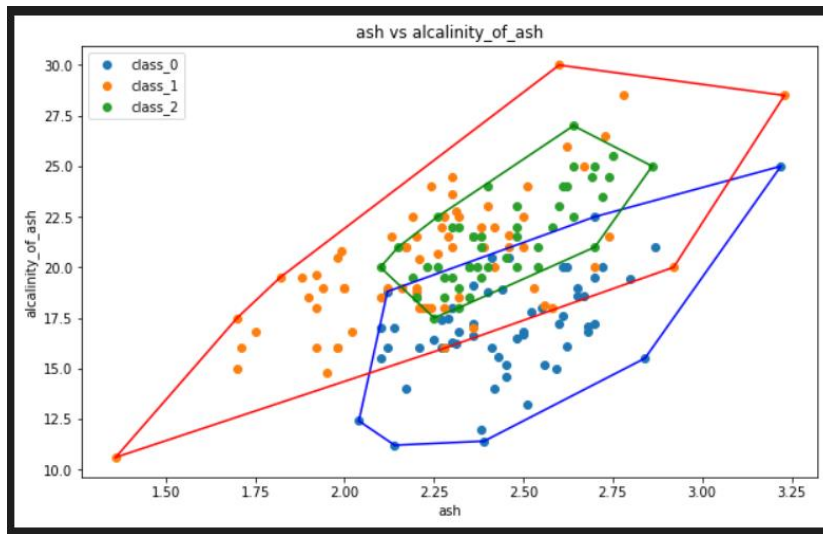


b. ash vs alcalinity\_of\_ash

Input:

```
data = datasets.load_wine()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 2
y = 3
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[x,y]].values
    hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull.simplices:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

Output:

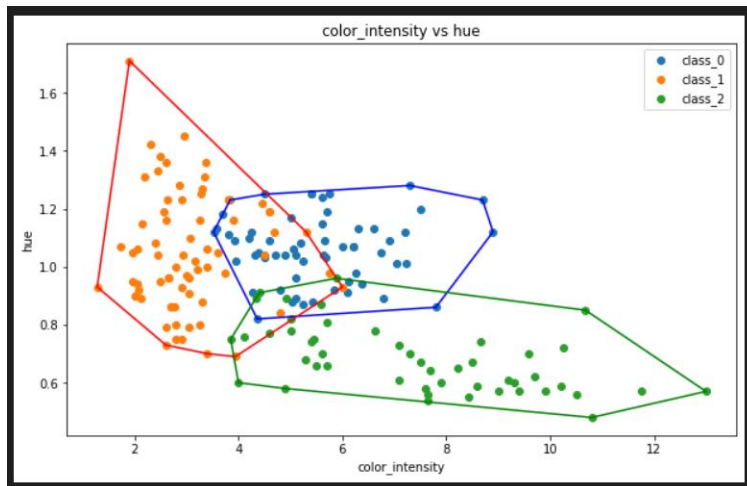


c. color\_intensity vs hue

Input:

```
data = datasets.load_wine()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 9
y = 10
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    ... bucket = df[df['Target'] == i]
    ... bucket = bucket.iloc[:,[x,y]].values
    ... hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    ... plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    ... for simplex in hull.simplices:
    ...     plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

Output:



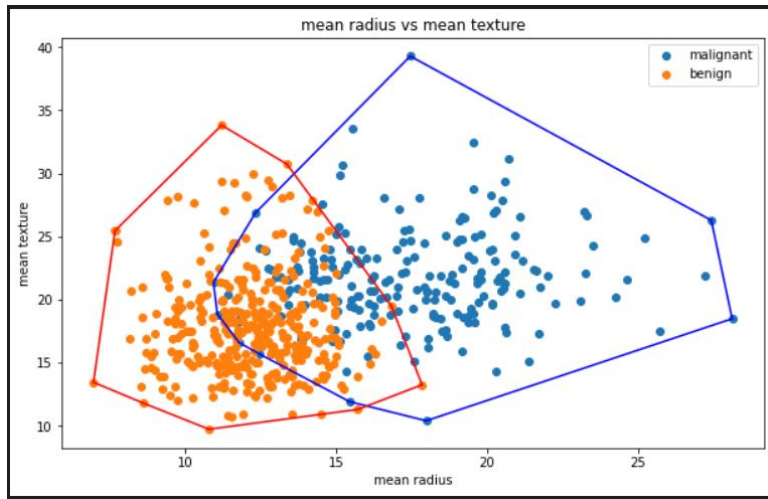
### C. Data Breast Cancer

#### a. mean radius vs mean texture

Input:

```
data = datasets.load_breast_cancer()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 0
y = 1
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[x,y]].values
    hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull.simplices:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

Output:

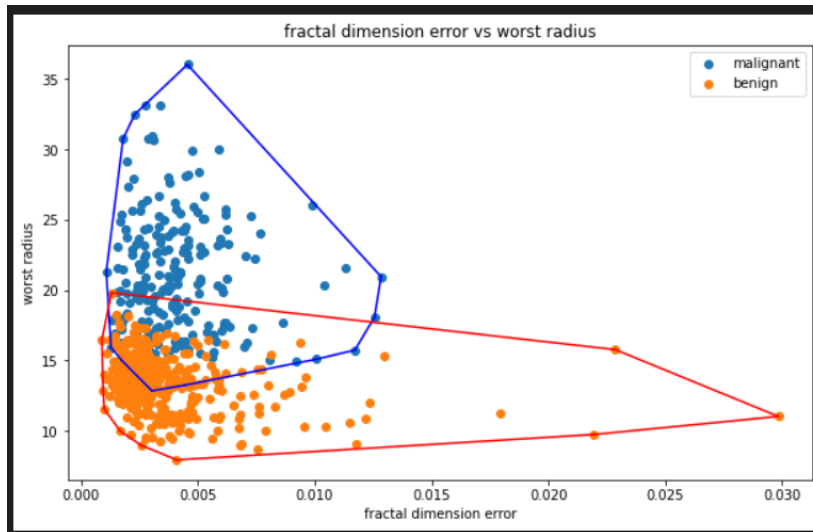


b. fractal dimension error vs worst radius

Input:

```
data = datasets.load_breast_cancer()
#create a DataFrame
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
display(df)
x = 19
y = 20
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
string = data.feature_names[x] + ' vs ' + data.feature_names[y]
plt.title(string)
plt.xlabel(data.feature_names[x])
plt.ylabel(data.feature_names[y])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[x,y]].values
    hull = ConvexHull(bucket) #bagian ini diganti dengan hasil implementasi ConvexHull Divide & Conquer
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull.simplices:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

Output:



#### IV. Git Hub Link

<https://github.com/Vincent136/Tucil-2-ConvexHull>

#### V. Tabel

Poin	Ya	Tidak
Pustaka <i>myConvexHull</i> berhasil dibuat dan tidak ada kesalahan	<input checked="" type="checkbox"/>	<input type="checkbox"/>
<i>Convex hull</i> yang dihasilkan sudah benar	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Pustaka <i>myConvexHull</i> dapat digunakan untuk menampilkan <i>convex hull</i> setiap label dengan warna yang berbeda.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
<b>Bonus:</b> program dapat menerima input dan menuliskan output untuk dataset lainnya.	<input checked="" type="checkbox"/>	<input type="checkbox"/>