

Homework3

2022年12月9日 上午 11:09

- Find the projection of the vector \mathbf{v} onto the subspace S .
 $S = \text{span}\{[0 \ 0 \ -1 \ 1]^T, [0 \ 1 \ 1 \ 1]^T\}$
 $\mathbf{v} = [1 \ 0 \ 1 \ 1]^T$
- Find the least squares solution of the system $\mathbf{Ax} = \mathbf{b}$.
 $\mathbf{A}_{3 \times 2} = [2 \ 1; 1 \ 2; 1 \ 1], \mathbf{b} = [2 \ 0 \ -3]^T$
 $\mathbf{B}_{4 \times 3} = [1 \ 0 \ 1; 1 \ 1 \ 1; 0 \ 1 \ 1; 1 \ 1 \ 0], \mathbf{b} = [4 \ -1 \ 0 \ 1]^T$
- Find the least squares regression line ($y = ax + b$) for the data points:
 $(-1, 1), (1, 0), (3, -3)$
- Find the least squares regression quadratic polynomial ($y = ax^2 + bx + c$) for the data points:
 $(-2, 0), (-1, 0), (0, 1), (1, 2), (2, 5)$
- Find a unit vector orthogonal to both $\mathbf{u} = [1 \ -4 \ 1]^T$ and $\mathbf{v} = [2 \ 3 \ 0]^T$.
- Find the area of a parallelogram that has $\mathbf{u} = [-3 \ 4 \ 1]^T$ and $\mathbf{v} = [0 \ -2 \ 6]^T$ as adjacent sides.
- Apply the Gram Schmidt process to $B = \{[0 \ 3 \ 4]^T, [1 \ 0 \ 0]^T, [1 \ 1 \ 0]^T\}$ (according to this order).
- $\mathbf{C}_{3 \times 3} = \mathbf{QR}$ using the Gram Schmidt process.
 \mathbf{C} 's 1st column is $[0 \ 0 \ 1]^T$, 2nd column is $[0 \ 1 \ 1]^T$, 3rd column is $[1 \ 1 \ 1]^T$.
- Find the determinant of
 $\mathbf{D}_{5 \times 5} = [2 \ 0 \ 1 \ 3 \ -2; -2 \ 1 \ 3 \ 2 \ -1; 1 \ 0 \ -1 \ 2 \ 3; 3 \ -1 \ 2 \ 4 \ -3; 1 \ 1 \ 3 \ 2 \ 0]$
- Find an equation of the plane passing through $(0, 1, 0), (-1, 3, 2), (-2, 0, 1)$.
- Find the determinant of $\mathbf{E}_{n \times n}$ (The values on the diagonal are $(1-n)$ and others are 1).
$$\begin{bmatrix} 1-n & 1 & 1 & \dots & 1 \\ 1 & 1-n & 1 & \dots & 1 \\ 1 & 1 & 1-n & \dots & 1 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & 1 & 1 & \dots & 1-n \end{bmatrix}$$
- Use the Cramer's rule to solve x, y and z .
 $2x + 3y + 3z = 3$
 $6x + 6y + 12z = 13$
 $12x + 9y - z = 2$

13. Let D_n be the determinant of the 1, 1, -1 tridiagonal matrix ($n \times n$), that is

$$D_n = \det \begin{bmatrix} 1 & -1 & & \\ & 1 & -1 & \\ & & \ddots & \ddots \\ & & & 1 & -1 \\ & & & & 1 \end{bmatrix}$$

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Calculate D^{15} .