

MIT Machine Learning notes

Vincent Courtois

Linear Classifiers

Perceptron Algorithm $\theta = \theta_0 = 0$. if $y_i(\theta \cdot x_i) \leq 0$ then $\theta = \theta + y_i x_i, \theta_0 = \theta_0 + y_i$

Large Margin Optimization

signed distance to boundary $\frac{y^{(i)}(\theta \cdot x^{(i)} + \theta_0)}{\|\theta\|}$. Margins are $\frac{1}{\|\theta\|}$ away from boundary.

hinge loss $Loss_h(y^{(i)}(\theta \cdot x^{(i)} + \theta_0)) = Loss_h(z) = 0$ if $z \geq 1$, $1 - z$ if $z < 1$

objective function $J(\theta, \theta_0) = \frac{1}{n} \sum_{i=1}^n Loss_h(y^{(i)}(\theta \cdot x^{(i)} + \theta_0)) + \frac{\lambda}{2} \|\theta\|^2$

Optimization algorithms

Stochastic gradient descent $\theta \leftarrow \theta - \eta_t \nabla_{\theta} [Loss_h(y^{(i)} \theta \cdot x^{(i)}) + \frac{\lambda}{2} \|\theta\|^2]$