

HW10

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Question 1

a.

i. How many recommendations does each bundle have? **ANSWER** : 6 recommendation per bundle(IOS).

ii. Use intuition to recommend 5 bundles! **ANSWER** : I chose Maroon5v first, then my recommendation are as follows: 1.beatsmusic 2. MonsterHigh 3. RetroSummer 4. New Years Party 5. xoxo

b.

```
library(data.table)
library(lsa)
```

```
## Loading required package: SnowballC
```

```
ac_bundles_dt <- fread("piccollage_accounts_bundles.csv")
ac_bundles_matrix <- as.matrix(ac_bundles_dt[, -1, with=FALSE])
```

i. Create cosine similarities for all bundles

```
similiar_matrix <- cosine(ac_bundles_matrix)
diag(similiar_matrix) <- 0 # won't be considered
recommend <- data.frame()
for(bundle in row.names(similiar_matrix)){
  recommend <- rbind(recommend, names(similiar_matrix[bundle, order(similiar_matrix[bundle, ], decreasing = TRUE)]))
}
row.names(recommend) <- row.names(similiar_matrix)
colnames(recommend) <- c(1:ncol(similiar_matrix))
top5_recom <- recommend[, 1:5]
head(top5_recom, 3)
```

1. Create top 5 recommend matrix or df

```
##           1           2   3           4           5
## Maroon5V      OddAnatomy beatsmusic xoxo      alien      word
## between      BlingStickerPack      xoxo gwen OddAnatomy AccessoriesStickerPack
## pellington      springrose      8bit2 mmlm julyfourth      tropicalparadise
```

```
mk_recom5 <- function(ac_bundles_matrix){
  similiar_matrix <- cosine(ac_bundles_matrix)
  diag(similiar_matrix) <- 0 # won't be considered
  recommend <- data.frame()
  for(bundle in row.names(similiar_matrix)){
    recommend <- rbind(recommend, names(similiar_matrix[bundle, order(similiar_matrix[bundle, ], decreasing = TRUE)]))
  }
  row.names(recommend) <- row.names(similiar_matrix)
  colnames(recommend) <- c(1:ncol(similiar_matrix))
  top5_recom <- recommend[, 1:5]
  return (top5_recom)
}
head(mk_recom5(ac_bundles_matrix), 3)
```

2. Create a function to create top 5 recommend matrix

```
##           1           2   3           4           5
## Maroon5V      OddAnatomy beatsmusic xoxo      alien      word
## between      BlingStickerPack      xoxo gwen OddAnatomy AccessoriesStickerPack
## pellington      springrose      8bit2 mmlm julyfourth      tropicalparadise
```

```
top5_recom["Maroon5V",]
```

5. Top 5 of your chosen bundles

```
##           1           2   3   4   5
## Maroon5V OddAnatomy beatsmusic xoxo alien word
```

Not really surprised to see that Maroon5 is similiar to aliens, only aliens can make that kind of cool beatsmusic huh? Since aliens are here, it's quite normal that anatomy is here too. I heard that aliens are notorious for dissecting homo sapiens, kinda gross lol.

```
center_apply <- function(x) {
  apply(x, 2, function(y) y - mean(y))
}
centered_ac_bundles <- center_apply(ac_bundles_matrix)
head(mk_recom5(centered_ac_bundles), 3)
```

ii. Create correlation based recommendations

```
##              1      2      3      4
## Maroon5V      OddAnatomy beatsmusic      xoxo      alien
## between      BlingStickerPack      xoxo      gwen OddAnatomy
## pellington      springrose      8bit2 tropicalparadise      mmlm
##              5
## Maroon5V      word
## between      AccessoriesStickerPack
## pellington      julyfourth
```

The recommended items are still the same for Maroon5.

```
transpose_ac <- t(ac_bundles_matrix)
center_apply <- function(x) {
  apply(x, 2, function(y) y - mean(y))
}
t_centered_ac_bundles <- center_apply(transpose_ac)
t1_centered_ac_bundles <- t(t_centered_ac_bundles)
head(mk_recom5(t1_centered_ac_bundles),3)
```

iii. Create adjusted cosine based recommendations

```
##              1      2      3      4      5
## Maroon5V      OddAnatomy word      xoxo      beatsmusic supercute
## between      BlingStickerPack xoxo      gwen      Monsterhigh OddAnatomy
## pellington      springrose 8bit2 backtocol tropicalparadise julyfourth
```

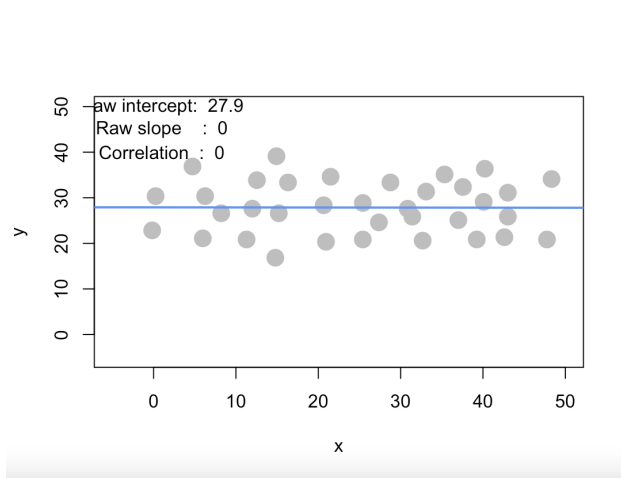
The recommended items changes slightly here, Maroon 5 is not similar to aliens, and beatsmusic differs to this bundle more. However, anatomy is still in first place, which is quite odd indeed.

c. Are the three sets of geometric recommendations similar in nature (theme/keywords) to the recommendations you picked earlier using your intuition alone? What reasons might explain why your computational geometric recommendation models produce different results from your intuition?

d. Conceptual difference in cosine similarity, correlation, and adjusted-cosine?

Question 2

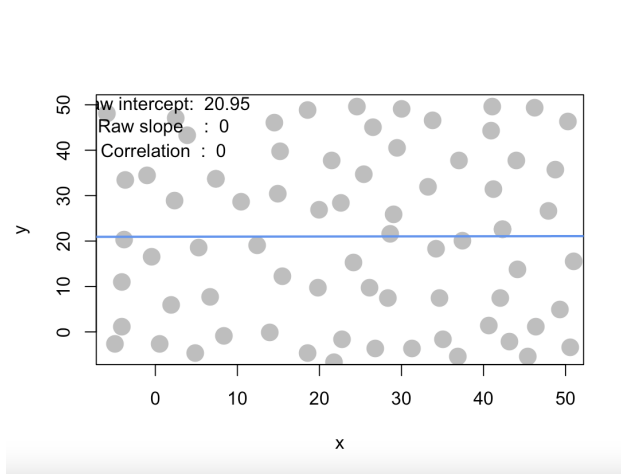
a. Create horizontal random points



i. **Raw Slope** **ANSWER:** Since the points are horizontal, the slope would be expected to be around zero ($0/x = 0$), and thus the simulation proves it.

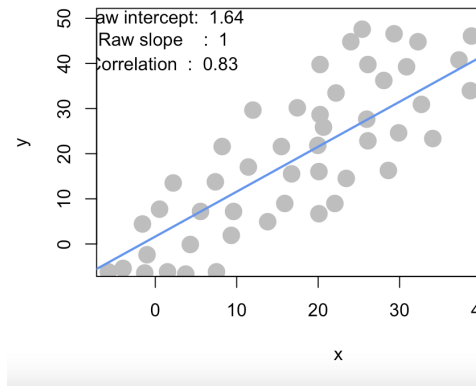
i. **Correlation** **ANSWER:** Since the points are horizontal, the y points only hover up and down in a little amount. Hence, we can expect the correlation to be zero, since y can be seen as not altered by increasing x.

b. Create a completely random set of points to fill the entire plotting area, along both x-axis and y-axis



i. **Raw Slope** **ANSWER:** Since the points are distributed entirely and randomly in the plot, it can be expected that the raw slope will be near zero if the y axis and x axis are distributed evenly.

i. **Correlation** **ANSWER:** Since the points are randomly distributed and filling the entire plot, it can be expected that the correlation will be about zero. Because the points are randomly distributed along the plot without any geometric meaning.

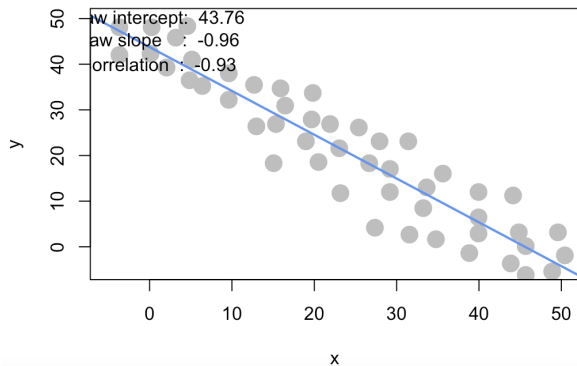


c. Create a diagonal set of random points trending upwards at 45 degrees

i. **Raw Slope** **ANSWER:** Since the points are distributed around a 45 degree angle line, the slope can be expected to be 1 ($y/x = 1$).

i. **Correlation** **ANSWER:** Since the x points trend the same as the y points, the expected correlation should be 1.

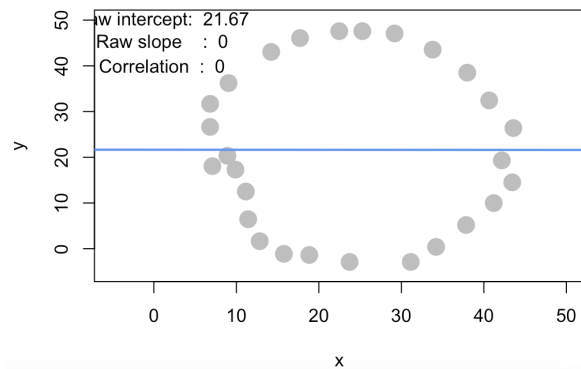
d. Create a diagonal set of random trending downwards at 45 degrees



i. **Raw Slope** **ANSWER:** Since the points are distributed around a 45 degree angle line but sloping downward, the slope can be expected to be -1 ($-y/x = -1$).

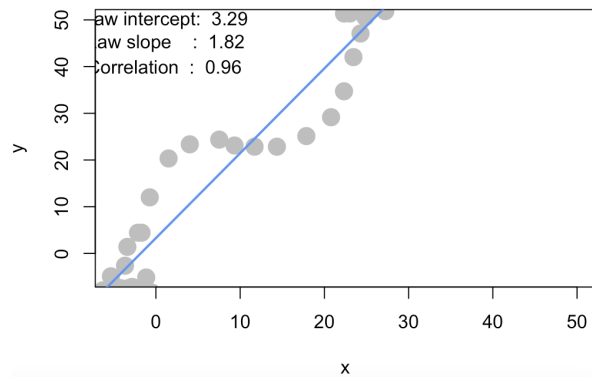
i. **Correlation** **ANSWER:** Since the x points trend the exact opposite way as the y points, the expected correlation should be -1.

e. Find another pattern of data points with no correlation



We can easily see that this resembles an ugly circle, which can be described by $(x - 25)^2 + (y - 25)^2 = r^2$. However, the x and y points do not have correlation.

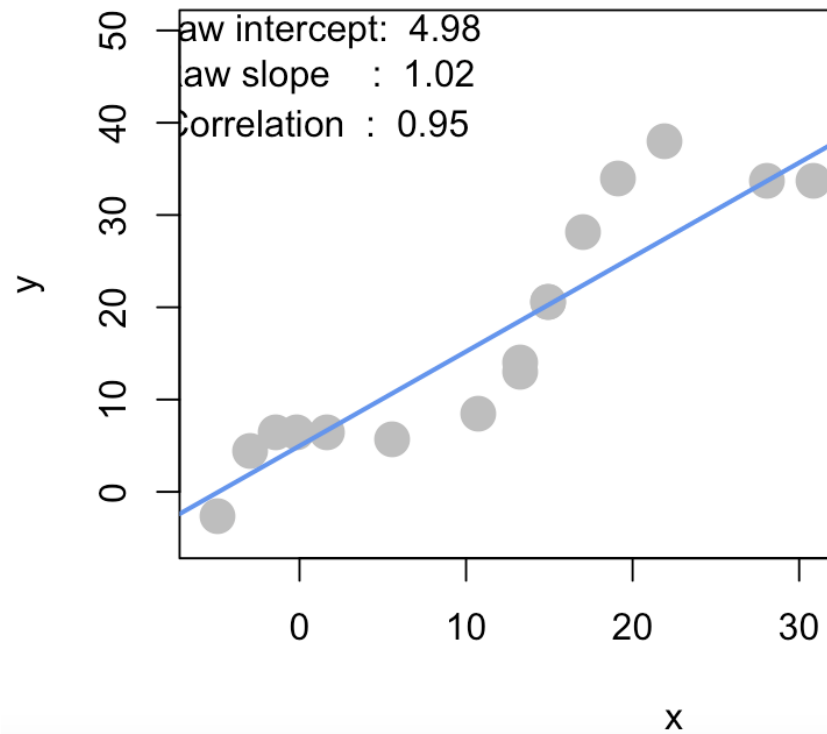
f. find another pattern of data points with perfect correlation



This plot is highly correlated x and y, also able to find an odd degree polynomial equation to describe this plot too.

g. How correlation relates to simple regression

```
#pts <- interactive_regression()
pts <- data.frame(x = c(-4.9244164, -2.9675264, -1.4299699, -0.1719691, 1.6451431, 5.5589232,
10.7307041, 13.2467056, 13.2467056, 14.9240399, 14.9240399, 17.0207078, 19.1173758, 21.9129330, 28.063158,
8.467709, 13.010537, 14.020054, 20.581917, 20.581917, 28.153297,
33.958022, 37.996091, 33.705642, 33.705642, 33.705642, 40.772264,
47.838885, 47.586506))
```



i. Simulate points with interactive regression

```
summary( lm( pts$y ~ pts$x ))
```

ii. Use the `lm()` function to estimate the regression intercept

```
##
## Call:
## lm(formula = pts$y ~ pts$x)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -7.4909 -3.2683 -0.1017  2.6020 10.5929
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   4.9761     1.7707    2.81  0.0116 *
## pts$x         1.0235     0.0806   12.70 2.02e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.154 on 18 degrees of freedom
```

```
## Multiple R-squared:  0.8996, Adjusted R-squared:  0.894
## F-statistic: 161.2 on 1 and 18 DF,  p-value: 2.02e-10
```

The slope and intercept is same in plot.

```
cor(pts)
```

iii. Estimate the correlation of x and y

```
##           x           y
## x 1.0000000 0.9484594
## y 0.9484594 1.0000000
```

Same as indicated in plot, however it is quite obvious since the `demo_simple_regression.R` also uses `cor` function to calculate correlation.

```
std_pts <- data.frame(x = scale(pts$x), y = scale(pts$y))
summary( lm( std_pts$y ~ std_pts$x ))
```

iv. Re-estimate the regression using standardized values of both x and y from pts

```
##
## Call:
## lm(formula = std_pts$y ~ std_pts$x)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.47320 -0.20646 -0.00642  0.16437  0.66916
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.941e-17  7.280e-02     0.0      1
## std_pts$x   9.485e-01  7.469e-02    12.7 2.02e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3256 on 18 degrees of freedom
## Multiple R-squared:  0.8996, Adjusted R-squared:  0.894
## F-statistic: 161.2 on 1 and 18 DF,  p-value: 2.02e-10
```

After standardization, the intercept is close to 0.

```
cor(std_pts)
```

```
##           x           y
## x 1.0000000 0.9484594
## y 0.9484594 1.0000000
```

The correlation doesn't change after standarization.

v.Relationship between correlation and the standardized simple-regression estimates The coefficients of the linear model(x) is the correlation of x and y points!