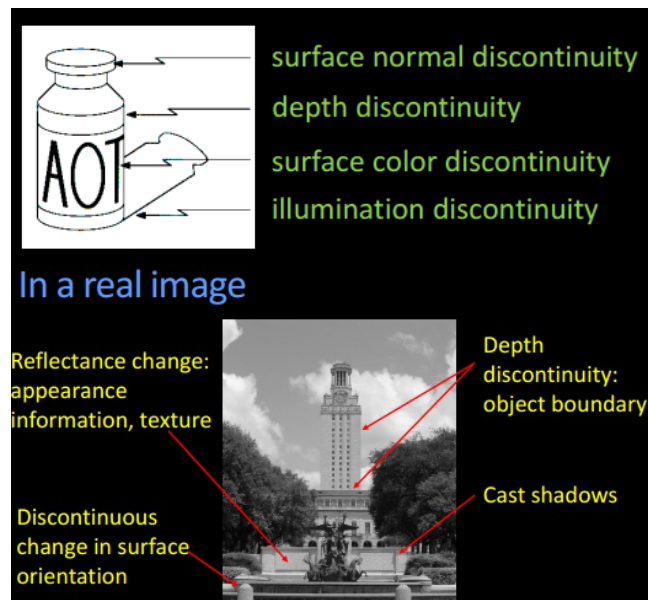


## 2A-L5 Edge detection - Gradients

2017/11/11 00:41

1. Sum
  - a. to find/recognize the obj, the obj boundary helps.
  - b. edge: where discontinuity happens: color, surface, depth, lumination
  - c. finit difference
  - d. gradient filter: sobel
  - e. use gradient to help find the edge
    - i. smooth
    - ii. gradient
      1. derivative of the filter first to save the computation
    - iii. 2nd gradient to find the max
2. Intro
  - a. working on the problem, to find the obj on generic images which is not suitable through a template
3. Reduced Images
  - a. Edges are important and they give a lot of info. sometimes
4. Edges
  - a. origin
    - i. surface normal discontinuity
    - ii. depth discontinuity
    - iii. color discontinuity
    - iv. illumination discontinuity



5. Quiz: Change Boundaries Quiz

Edges seem to occur “change boundaries” that are related to shape or illumination. Which is not such a boundary?

- a) An occlusion between two people
- b) A cast shadow on the sidewalk
- c) A crease in paper
- d) A stripe on a sign

i. analysis

1. An occlusion occurs when a physical object (or part of one) is in front of another, with respect to the viewing angle. This is part of the geometry or overall shape of the scene.
2. A shadow is caused due to difference in illumination falling on a surface.
3. A crease alters the shape of the paper, which is observable from certain viewing angles.
4. A stripe is essentially a color discontinuity, which is not caused by shape or illumination.

1. Edge Detection

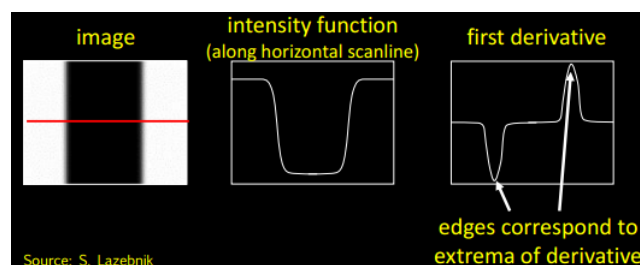
- a. how to define a edge, or how can we determine certain pixel is on the edge?
  - i. on an image, edges look like steep cliffs, pixels with a strong change in a neighborhood
- b. so the Basic idea: look for a neighborhood with strong signs of change.

i. Problems

1. neighborhood size
2. how to define a change is a strong change which can be regarded as boundary

2. Derivatives and Edges

- a. when talking about changes in math, we rely on derivatives so
  - i. An edge is a place of rapid change in the image intensity function, and this rapid change corresponds to the maximum of the derivative, see e.g.



- ii. so the problem turns out to be find the peaks of the derivatives
- a. how to compute the derivative
  - i. differential operator, just like other filters
    1. Differential operators - when applied to the image returns some derivatives.
    2. • Model these “operators” as masks/kernels that compute the image gradient function.
    3. • Threshold the this gradient function to select the edge pixels.
- 1. What is a Gradient
  - a. The gradient points in the direction of most rapid increase in intensity

**Image gradient**

The gradient of an image:  $\nabla f = \left[ \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$

The gradient direction is given by:  $\theta = \tan^{-1} \left( \frac{\frac{\partial f}{\partial y}}{\frac{\partial f}{\partial x}} \right)$

The *edge strength* is given by the gradient magnitude:  $\|\nabla f\| = \sqrt{\left( \frac{\partial f}{\partial x} \right)^2 + \left( \frac{\partial f}{\partial y} \right)^2}$

## 9. Finite Differences

For 2D function,  $f(x,y)$ , the partial derivative is:

$$\frac{\partial f(x,y)}{\partial x} = \lim_{\varepsilon \rightarrow 0} \frac{f(x + \varepsilon, y) - f(x, y)}{\varepsilon}$$

- a. finite difference

For discrete data, we can approximate using finite differences:

$$\frac{\partial f(x,y)}{\partial x} \approx \frac{f(x+1,y) - f(x,y)}{1}$$

$$\approx f(x+1,y) - f(x,y)$$

*“right derivative” But is it???*

- i. this is also called right derivative
  - a. e. g.

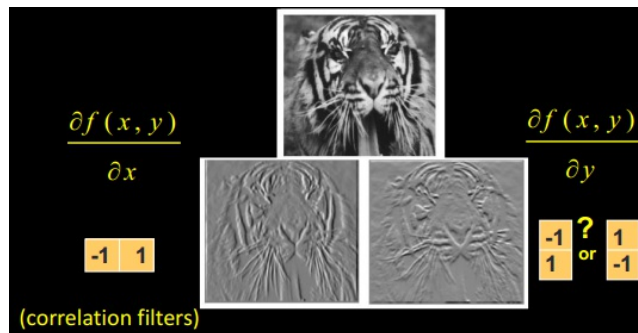
## Finite differences – x or y?



1. it's a finite difference on x, since horizontally, the edges are stronger than the vertical ones

### 1. Partial Derivatives of an Image

- filters along the x, is  $[-1, 1]$ ; along the y depends on your origin, if on the top-left corner, positive downside[CS choice]; if on the bottom left corner, positive upside[math choice].



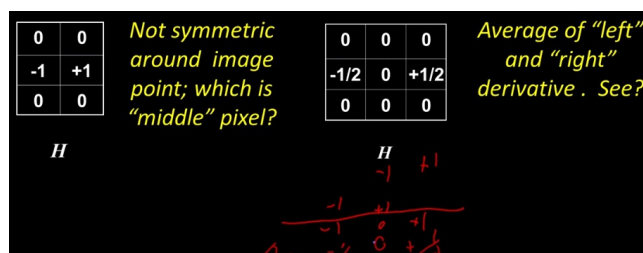
- here correlation and convolution are different, be careful
- how does this  $[-1, 1]$  filter work?



i. it is an awful image for edge detection

### 1. The Discrete Gradient Filter

- what kind of filter should we use



i. the first is not suitable to find the middle pixel; so the left one, and the  $1/2$  is the average of the left and

## right derivatives

### 1. Sobel Operator

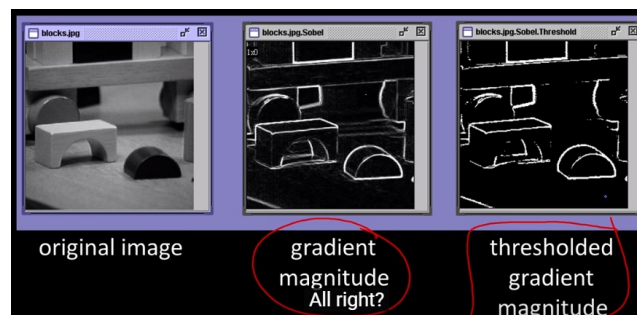
$$\frac{1}{8} * \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \quad \frac{1}{8} * \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} \quad (\text{here positive } y \text{ is up})$$

$S_x$                        $S_y$

**(Sobel) Gradient is  $\nabla I = [g_x \ g_y]^T$**

$g = (g_x^2 + g_y^2)^{1/2}$     is the gradient magnitude.  
 $\theta = \text{atan2}(g_y, g_x)$     is the gradient direction.

- a. the idea of adding the -1 & 1 is that we assume that images are sort of locally smooth so when compute the derivatives, it's better to look around the neighborhood and then normalize the filter.
- b. `imgradient` in matlab applies sobel operator by default but it doesn't normalize it by dividing 8
- c. how does it work



- i. it's not a great edge detection, but also not an awful one. So it's better than the previous one with  $[-1, 1]$

### 1. Well Known Gradients

#### a. matlab code

- i. `filt = fspecial('sobel')`
- ii. `outim = imfilter(double(im), filt);`
- iii. `imagesc(outim);`
- iv. `colormap gray`

#### b. functions

- i. `h = fspecial(type)` creates a two-dimensional filter `h` of the specified `type`.

1. `sobel`, `prewitt`, `roberts`

- ii. `B = imfilter(A, h)` filters the multidimensional array `A` with the multidimensional filter `h`

1. The result `B` has the same size and class as `A`.
2. `B`, using double-precision floating point. so we need the conversion
3. by default, it uses correlation rather than convolution, but it can be changed.

- iii. `imagesc(C)` displays the data in array `C` as an image that uses the full range of colors in the colormap. Each element of `C` specifies the color for 1 pixel of the image.

iv. `colormap` `maptype` sets the `colormap` for the current figure to one of the predefined `colormaps`.

1. `maptype: gray, spring, summer, ..., copper, colorcube, ...`

2. Quiz: Gradient Direction Quiz

a. to compute, it's better to use correlation since it's easy to know the left and right ???

b. matlab code

i. %% Load and convert image to double type, range [0, 1] for convenience

1. `img =`

`double(rgb2gray((imread('moon.jpg')))) / 255.;`

a. % assumes [0, 1] range for double images. since `imgshow`

`img` range [0,1] or [min, max]

b. or `imshow(img, [0, 255])`

c. but if `imshow(img)`, the range is [min, max] may cause some problem, just like `imagesc()`

2. `imshow(img);`

ii. %% Compute x, y gradients

1. `[gx gy] = imgradientxy(img, 'sobel');` %

Note: `gx, gy` are not normalized

2. `figure(5);imshow((gx + 4)/8);`

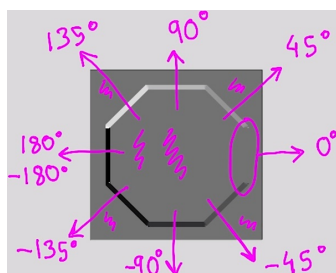
iii. %% Obtain gradient magnitude and direction

1. `[gmag gdir] = imgradient(gx, gy);`

2. `figure(2);imshow(gmag / (4 * sqrt(2)));;`

%  $\text{mag} = \sqrt{gx^2 + gy^2}$ , so [0, (4 \* sqrt(2))]

3. `figure(3);imshow((gdir + 180.0) / 360.0);` % angle in degrees [-180, 180]



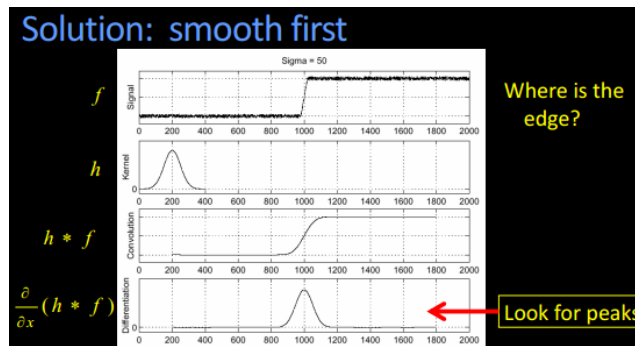
4. %% Find pixels with desired gradient direction -- set the desired pixels 1, the

others 0

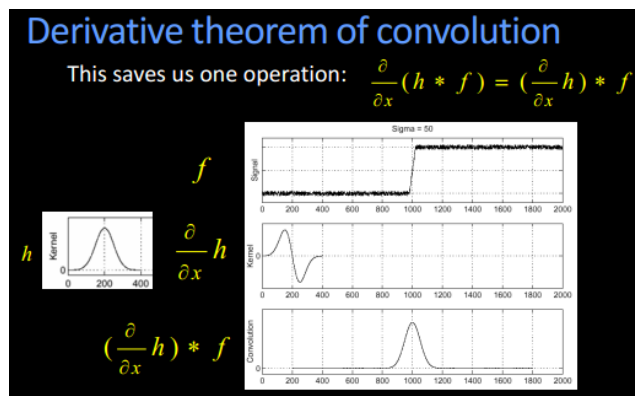
- a. `result = gmag > mag_min & gdir > angle_low & gdir < angle_high;`
  - i. `&` is the element-wise logic AND when applied with matrix
  - ii. `expr1 && expr2`, `&&` is for expression

1. But in the Real World

- a. Since in the real world, there're noise in the images, so we can't compute the gradient directly
- b. filter to smooth the images first and then gradient



- i. to save the computation, do the conv first



- c. edge is corresponds to the max of the gradient, so compute the second order derivative

