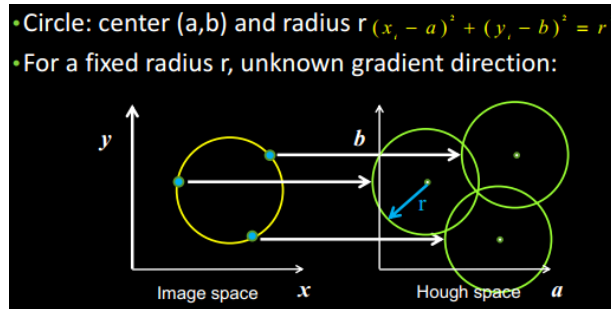


2B-L2 Hough transform - Circles

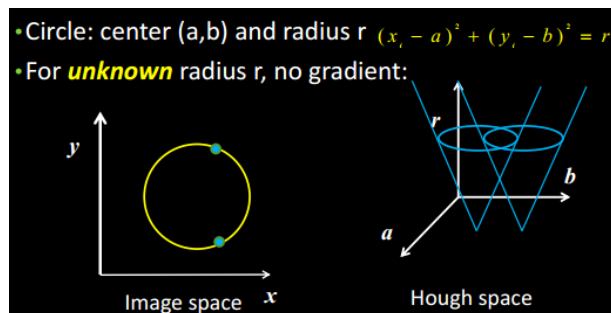
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1. Detecting Circles with Hough

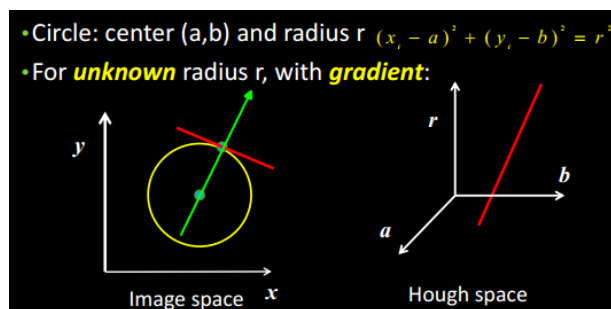


- i. duality: one point in xy is a circle with r in ab ;
vise versa
- ii. the intersection point of these three circles in ab
defines a circle in xy

1. Hough Transform for Circles



- i. when r is not know, the hough space become 3 dim, abr.
still, to find the intersection. but computationally very
expensive



1. the gradient of one point in the circle
restrict the radius to be a line in the abr
space

1. Algorithm for Circles

```

1. For every edge pixel (x,y) :
2.   For each possible radius value r:
3.     For each possible gradient direction  $\theta$ :
4.       %% or use estimated gradient
5.        $a = x - r \cos(\theta)$ 
6.        $b = y + r \sin(\theta)$ 
7.        $H[a,b,r] += 1$ 
8.     end
9.   end

```

4. Voting Practical Tips

- a. Minimize irrelevant tokens first (take edge points with significant gradient magnitude)
- b. • Choose a good grid / discretization:
 - i. • Too coarse: large votes obtained when too many different lines correspond to a single bucket
 - ii. • Too fine: miss lines because some points that are not exactly collinear cast votes for different buckets
- c. Vote for neighboring bins (like smoothing in accumulator array)
- d. • Utilize direction of edge to reduce free parameters by 1
- e. • To read back which points voted for “winning” peaks, keep tags on the votes

5. Pros and Cons

Pros

- All points are processed independently, so can cope with occlusion
- Some robustness to noise: noise points unlikely to contribute consistently to any single bin
- Can detect multiple instances of a model in a single pass

Cons

- *Complexity of search time increases exponentially with the number of model parameters*
- Non-target shapes can produce spurious peaks in parameter space
- Quantization: hard to pick a good grid size

6. End

- a. it's an old technique, but it still worth learning to extract structure with it