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903178639-vla6-hw2

# Logistic Regression Proofs

## 1.1.a Batch Gradient Descent

*Derive the gradient of the negative log-likelihood in terms of* ***w*** *for this setting.*

We know that:

First, we prove that

Note that

So now that we know this identity we can proceed.

To derive the gradient of the negative log-likelihood we have:

## 1.2 Stochastic Gradient Descent

### 1.2.a

*Show the log likelihood, l, of a single (x\_t, y\_t) pair*

For a single (x\_t, y\_t) pair, recall that y\_t can only take on values 1 or 0 (since we’re assuming binary classifier.

Thus, log likelihood, l, of a single pair is

### 1.2.b

*Show how to update the coefficient vector*

For a single training point, recall that

This is taken from question 1.1 of this HW assignment.

Thus, the update rule is

Where the learning rate is represented by *.*

### 1.2.c

*What is the time complexity of the update rule from* ***b if x\_t is very sparse?***

Notice that if x\_t is very sparse, then in the update rule, notice that if ; then . Thus in the case where it is very sparse then in the case where the feature is 0, then you don’t actually need to update.

Let represent the non-zero features. Then, the time complexity is

Or I suppose that if x\_t is actually very very sparse, then the time complexity might be argued as or constant.

### 1.2.d

Briefly explain the consequence of using a very large learning rate and very small learning rate.

If learning rate is too small, it will take longer to converge; if the learning rate is too large, may fail to converge.

### 1.2.e

Under the penalty of L2 norm regularization, notice that

Thus the update rule becomes

Notice that now when x^j is zero, or when there is a sparse matrix, there is still an update that happens. Thus the time complexity is

Where D is the number of features.

## 2.1 Descriptive Statistics

|  |  |  |
| --- | --- | --- |
| Metric | Deceased Patients | Alive Patients |
| Event Count |  |  |
| 1. Average Event Count | 1027.74 | 683.16 |
| 1. Max Event Count | 16829 | 12627 |
| 1. Min Event Count | 2 | 1 |
| Encounter Count |  |  |
| 1. Average Encounter Count | 24.84 | 18.695 |
| 1. Max Encounter Count | 375 | 391 |
| 1. Min Encounter Count | 1 | 1 |
| Record Length |  |  |
| 1. Average Record Length | 157.042 | 194.702 |
| 1. Median Record Length | 25.0 | 16 |
| 1. Max Record Length | 5364 | 3103 |
| 1. Min Record Length | 0 | 0 |
| Common Diagnosis | DIAG320128  DIAG319835  DIAG313217  DIAG197320  DIAG132797 | DIAG320128  DIAG319835  DIAG317576  DIAG42872402  DIAG313217 |
| Common Laboratory Test | LAB3009542  LAB3023103  LAB3000963  LAB3018572  LAB3016723 | LAB3009542  LAB3000963  LAB3023103  LAB3018572  LAB3007461 |
| Common Medication | DRUG19095164  DRUG43012825  DRUG19049105  DRUG956874  DRUG19122121 | DRUG19095164  DRUG43012825  DRUG19049105  DRUG19122121  DRUG956874 |