



CSCA48

Introduction to Computer Science II

导师: **VC**

UTSC Week 10 Graph | 2025/3/10



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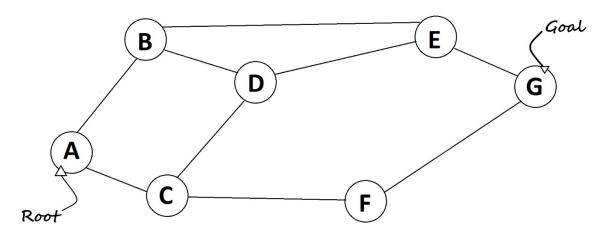
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Definition of Graph

• Definition of a Graph



- A graph consists of:
 - A set of nodes corresponding to data items we are working with. The set of nodes is
 usually called V. In books, lecture notes, and future courses, you may find the term
 vertex is used instead of node. They are the same thing.
 - A set of edges which are the connections between nodes, and represent the relationships existing between data items in our collection. The set of edges is usually called E.
 - Together, they define the graph G = (V, E).

- Two types of graphs:
 - Un-directed graphs
 - Directed graphs



Important terms of Graph

- Neighbours
 - o Un-directed graph
 - o Directed graph

- Neighbourhood
 - Un-directed graph
 - o Directed graph

- Degree
 - o Un-directed graph
 - Directed graph



Important terms of Graph

- Path
 - o Un-directed graph
 - o Directed graph

- Cycles
 - o Un-directed graph

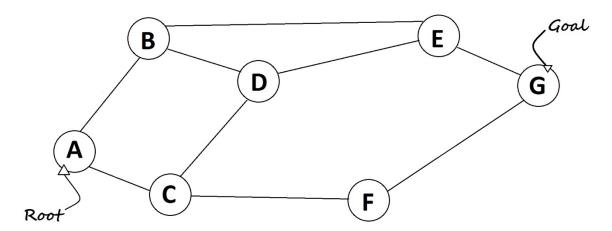
o Directed graph





Representing Graphs

Adjacency List



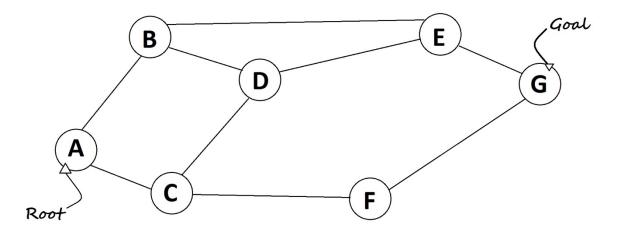
- The adjacency list is an **array** with **one entry per node**. The **i**th entry in the array contains a pointer to **a linked list** that stores the indexes of nodes to which node i is connected.
- The **advantage** of being space efficient if the graph has a large number of nodes, but each node is connected to at most a few neighbours, then the adjacency list stores the required edge information in a very compact format without wasting memory. **Conversely**, common graph operations such as querying an edge (figuring out whether two nodes are connected) requires list traversal, which as we know can be slow.





Representing Graphs

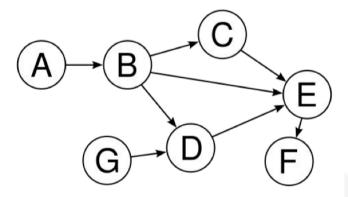
Adjacency Matrix



- ◆ As the name implies, the adjacency matrix is a 2D array of size N x N, where N is the number of nodes in the graph. For un-directed graphs, The entry A[i][j] is 1 if nodes i and j are connected, and zero otherwise. For directed graphs, entry A[i][j] is set to 1 if there is an edge from i to j, and is zero otherwise.
- Adjacency matrices have the same advantages and disadvantages of arrays: Edge queries now have no overhead, unlike linked lists which require list traversal. Adding or deleting edges, and finding out whether two nodes are connected requires a single access to the matrix. Conversely, they are not space efficient. Even in the small example above, you can see that the majority of the entries in the matrix are zero. For a very large graph, the adjacency matrix will waste a significant amount of space and may in fact not fit in memory!



Representing Graphs – Practice



• Show the Adjacency List, use indexes 0 though 6, starting with A at index 0.

• Show the Adjacency Matrix for the graph.



Complexity of fundamental operations on Graphs

•	Edge query : Finding out whether two nodes (u,v) are connected	
	Adj. List:	Adj. Graph:
•	Inserting a node: Adding a new node to the graph	
	Adj. List:	Adj. Graph:
•	Removing a node:	
	Adj. List:	Adj. Graph:
•	Inserting an edge:	
	Adj. List:	Adj. Graph:

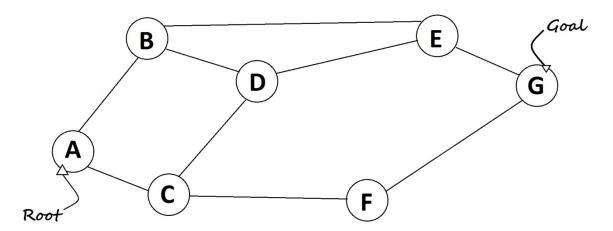
• Removing an edge:

Adj. List: Adj. Graph:



Graph Search

Breadth-First Search (BFS)

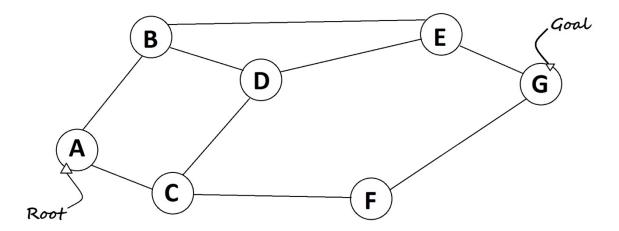


- It starts at the root and explores all of its children in the next level (neighbors) before moving to each of the root children, and then, it explores the children of the root children, and so on. The algorithm uses a queue to perform the BFS.
- Pseudocode: (Iterative)
 - 1. Add root node to the queue, and mark it as visited (already explored).
 - 2. Loop on the queue as long as it's not empty.
 - 1. Get and remove the node at the top of the queue(current).
 - 2. For every non-visited child of the current node, do the following:
 - 1. Mark it as visited.
 - 2. Check if it's the goal node, if so, then return it.
 - 3. Otherwise, push it to the queue.
 - 3. If queue is empty, then goal node was not found!



Graph Search

Depth-First Search (DFS)

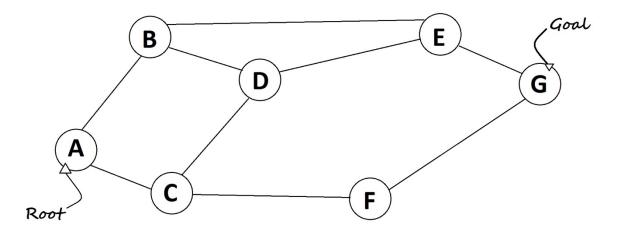


- It starts at the root and explores one of its children's sub tree, and then move to the next child's sub tree, and so on. It uses stack, or recursion to perform the DFS.
- Pseudocode: (Iterative)
- 1. Add root node to the stack.
- 2. Loop on the stack as long as it's not empty.
 - Get the node at the top of the stack(current), mark it as visited, remove it.
 - 2. For every non-visited child of the current node, do the following:
 - 1. Check if it's the goal node, if so, then return this child node.
 - 2. Otherwise, push it to the stack.
 - 3. If stack is empty, then goal node was not found!



Graph Search

Depth-First Search (DFS)

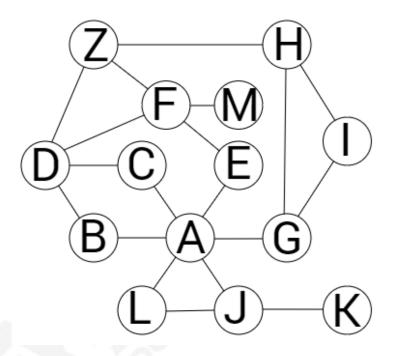


- It starts at the root and explores one of its children's sub tree, and then move to the next child's sub tree, and so on. It uses stack, or recursion to perform the DFS.
- Pseudocode: (Recursive)
- 1. Mark the *current* node as visited(initially *current* node is the *root* node)
- 2. Check if current node is the goal, If so, then return it.
- 3. Iterate over children nodes of current node, and do the following:
 - 1. Check if a child node is not visited.
 - 2. If so, then, mark it as visited.
 - 3. Go to it's sub tree recursively until you find the *goal* node (In other words, do the same steps here passing the *child* node as the *current* node in the next recursive call).
 - 4. If the child node has the goal node in this sub tree, then, return it.
- 4. If goal node is not found, then goal node is not in the tree!



Graph Search – Practice

• Perform BFS on the given graph.



• Perform DFS on the given graph.

