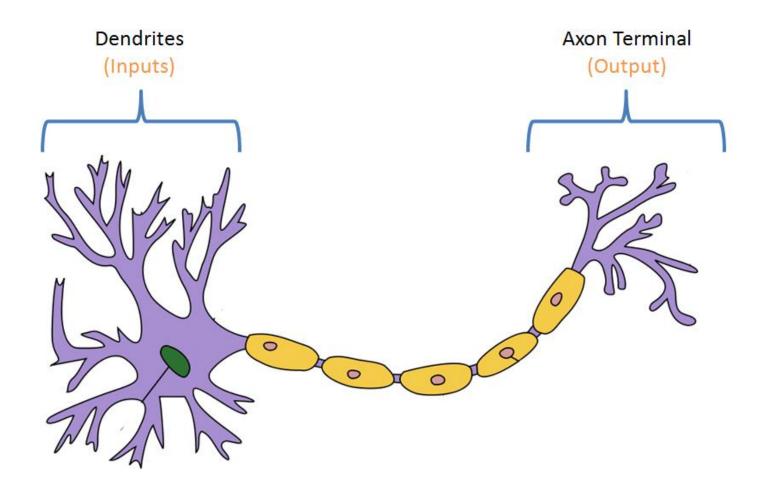
Neural Nets

Hey this is artificial intelligence, let's take a look at the gold standard of intelligence: the brain!

As we know, the brain consists of about 100 *billion* neurons that resemble a certain basic structure:



Here we have a basic neuron structure with dendrites, which collect the neurotransmitters from other connected neurons at their synapses...

...and if enough neurotransmitters are excitatory such that the neuron "fires," it will then release neurotransmitters of its own into the synapses connected to its axon terminals.

In simplest terms, we want to try to model certain computational problems using the input / output semantics of actual neurons to tackle tasks like classification and deep learning.

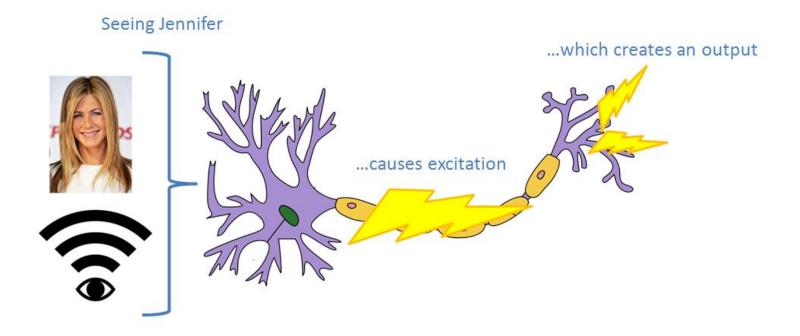
Let's root neural networks in a familiar problem: classification.

Remember that classification is the task of deciding whether our input attributes is indicative of a particular class, and returns a yes / no answer.

Example

^t Take, for example, a very simple neuron which (through some process irrelevant to us) gets activated whenever you're looking at Jennifer Aniston (this was a real study, look it up):

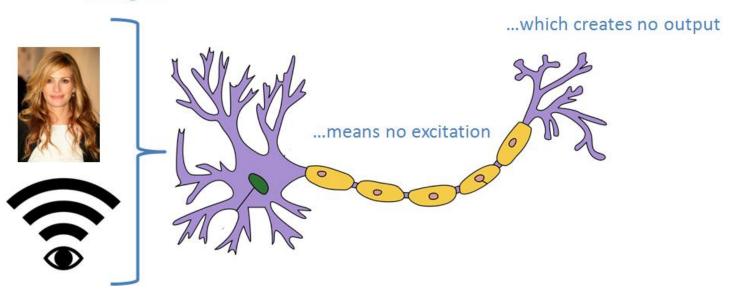
This might look like the following:



(somewhere, someone who actually studies neuroscience is reading this and cringing)

However, if that same neuron were to respond to input of seeing Julia Roberts instead (which is, I believe, what they did in the study) it might not activate!

Seeing Julia



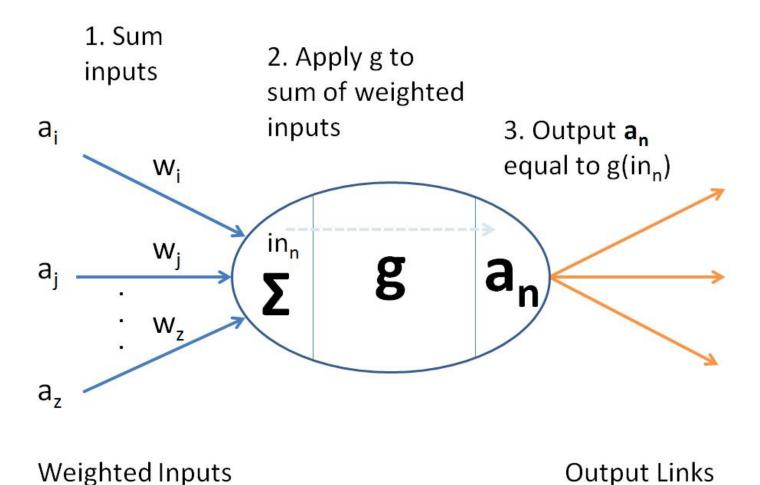
It would be nice, then, if we could take a bunch of neurons with certain activation patterns, and combine their outputs to serve our computation interests.

Let's look at the basic case first...

The anology to our neural networks is as follows:

- ^d Artificial neural networks have **input** elements representing our attributes of interest (like the dendrites).
- ^á Artificial neurons have **activation functions** that determine whether or not, based on the input, they will fire.
- ^á Artificial neural networks have **output** elements that can be used for classification or simply returning results of the internal computations...

Let's look at a very simple artificial neuron and then look at how to use it.



What you choose for the activation function is up to you, but typical choices are the following:

^á An activation function that is a **step / threshold function** will only produce an output when some minimum value is reached for its sum of weighted inputs.

Typically, step functions output 0 if we haven't reached some threshold yet, or 1 otherwise.

These bear a close semblance to how actual neurons operate.

^á An activation function that is a **logistic function** (the inverse of the natural logit function) produces an s-curve used to convert the logarithm of odds into a probability (positive inputs approach a ceiling of 1, negative inputs approach a floor of -1).

Why don't we look at a single node neuron and see how this all fits together.

Here are the steps for computation at a single neuron:

```
; Step One: Sum weighted inputs
; for n input links

n
in_j = \Sigma w_i * a_i
    i = 0

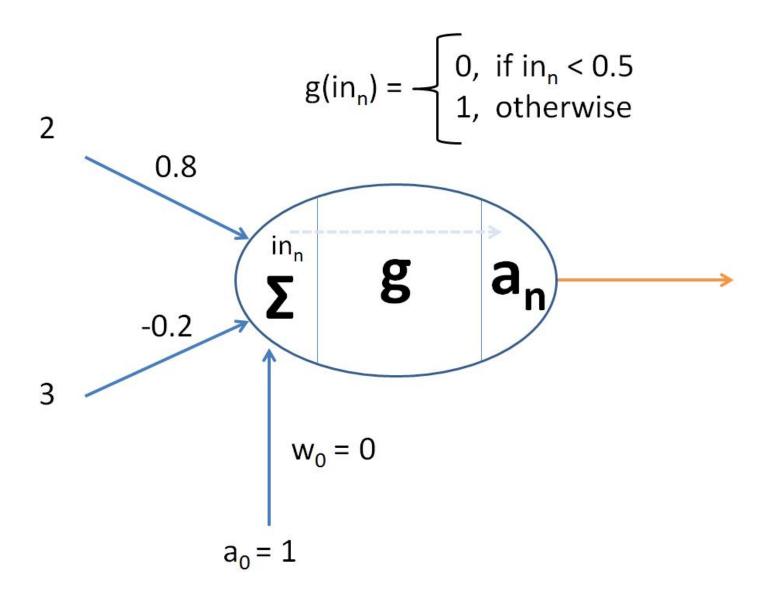
; Step Two: Apply g(in_j)
; where g is the activation function

a_j = g(in_j)

; Step Three: Propagate the output
; a_j to any output links
```

Example

^t What will the following neuron output for the given inputs, weights, and activation function?



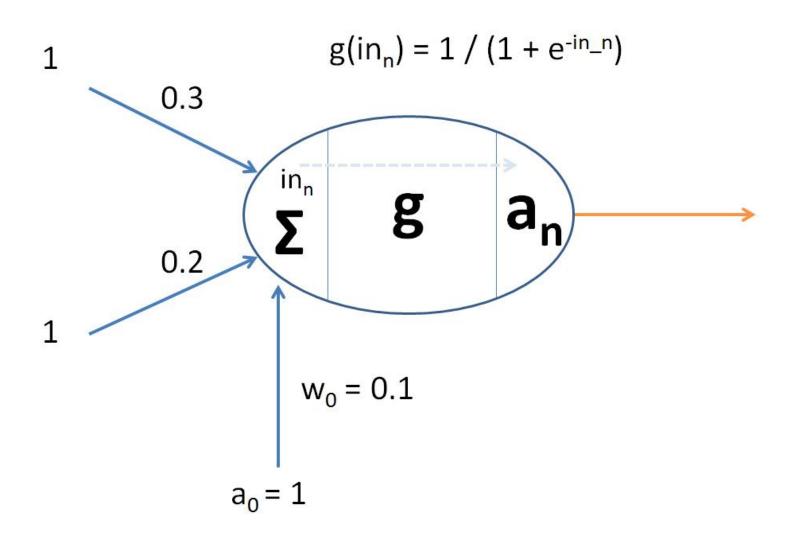
 $^{\acute{a}}$ The above neuron, which is a single unit whose activation function is a step function, is called a **perceptron**.

Some things to notice:

- Weights can be negative (to immitate an inhibitory effect like our own neurons have)
- · Weights can be 0
- (not shown) Weights can be any real number, not necessarily percentage values
- · The bias input value is always 1 though its weight can be modified
- · Other input values can be whatever you'd like to suit the problem at hand

Example

^t What will the following neuron output for the given inputs, weights, and activation function?



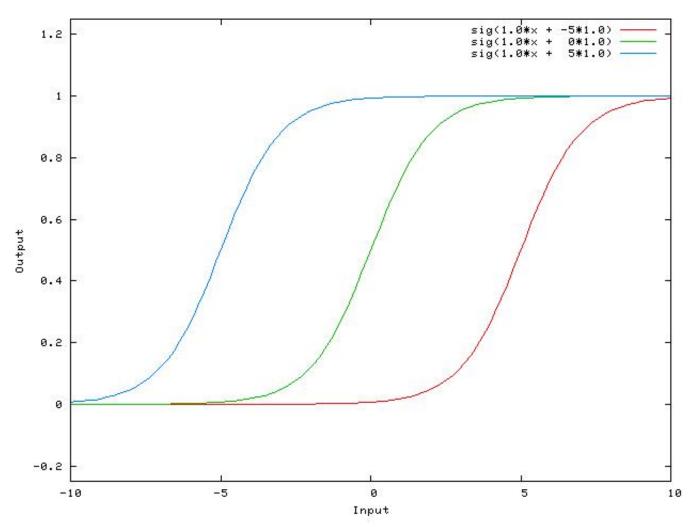
^á The above neuron, which is a single unit whose activation function is a logistic function, is called a **sigmoid perceptron**, sometimes used as a probability calculator.

^á The **bias** input is simply a means of shifting our sigmoid curve left and right by manipulating its weight, and (described later) for handling learning where our inputs are 0.

Observe how the output of a sigmoid perceptron changes by manipulating the bias input:

```
; Say for perceptron n with 2 inputs
; and 1 bias input:
; (where sig() is the sigmoid logistic function)
a_n = sig(w_i * a_i +
         w_j * a j +
         w_0 * a_0; Here is the bias term
a n = sig(0.3 * 1 +
         0.2 * 1 +
         0.0 * 1)
   = 0.62
; Change w 0 to 0.5 shifts right
a_n = sig(0.3 * 1 +
         0.2 * 1 +
         0.5 * 1)
   = 0.73
; Change w_0 to -0.5 shifts left
a n = sig(0.3 * 1 +
         0.2 * 1 +
         -0.5 * 1)
   = 0.5
```

Visually, we can see the shift as the following (depicted below: only one input and taken from a really good SO article on Bias inputs, linked):



(http://stackoverflow.com/questions/2480650/role-of-bias-in-neural-networks)

Typically you will have one bias input connected to all non-input neurons, though you can have one per level as well.

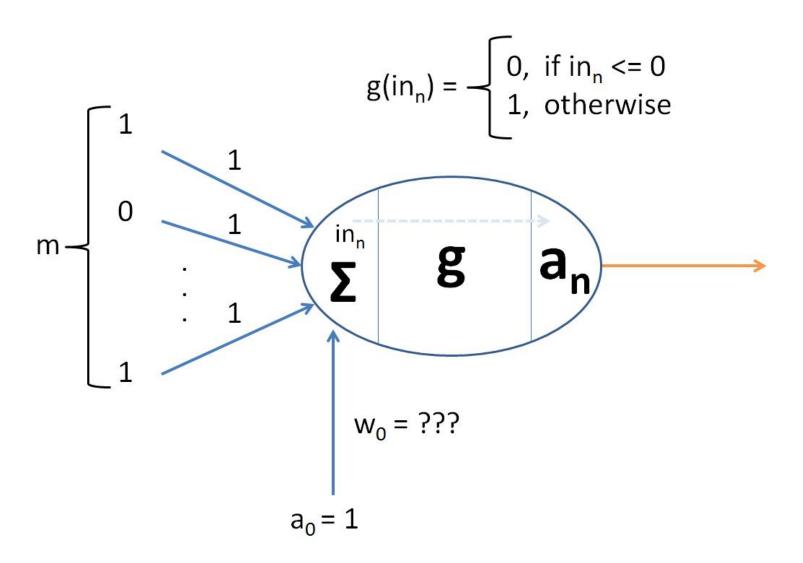
Succinctly, the output of some neuron n is given by:

Perceptrons on their own can do many tasks quite well. The majority function is one of them:

Example

t Consider the following perceptron (step activation function) that implements the **majority function**,

outputting 1 whenever the majority (MORE than half) of its inputs are also 1. Determine the weight of the bias input for m inputs (each with weight and activation values of 1).

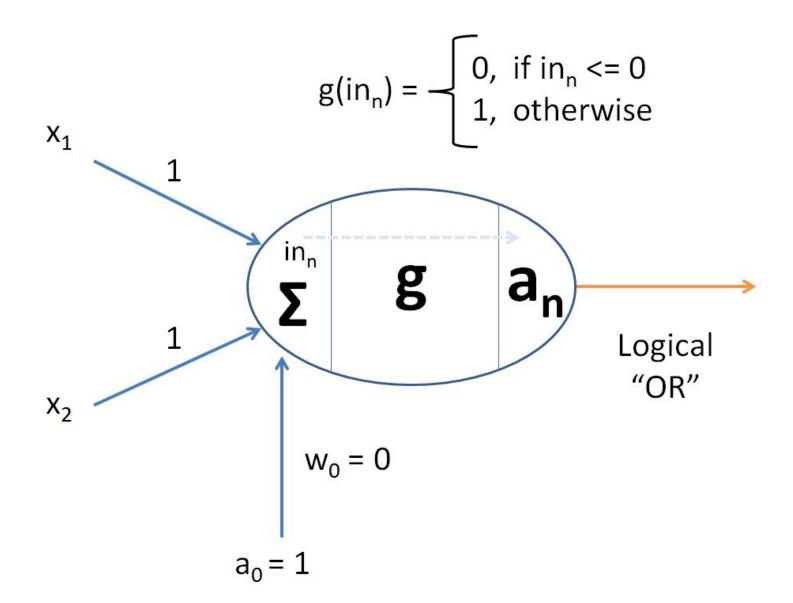


Need a hint? Consider m = 10 with 2 separate cases: in Case 1, 5 of those inputs are 1 and the others 0; in Case 2, 6 of those inputs are 1 and the others 0.

à Click for solution.

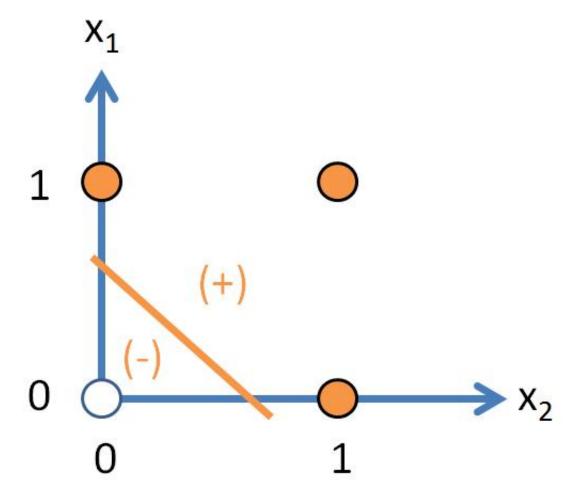
Now there is one problem to discuss with perceptrons. Let's condider the perceptron that performs a logical, binary OR, i.e., outputs 1 if either of its inputs (or both) are 1.

We might create a perceptron that looks like:

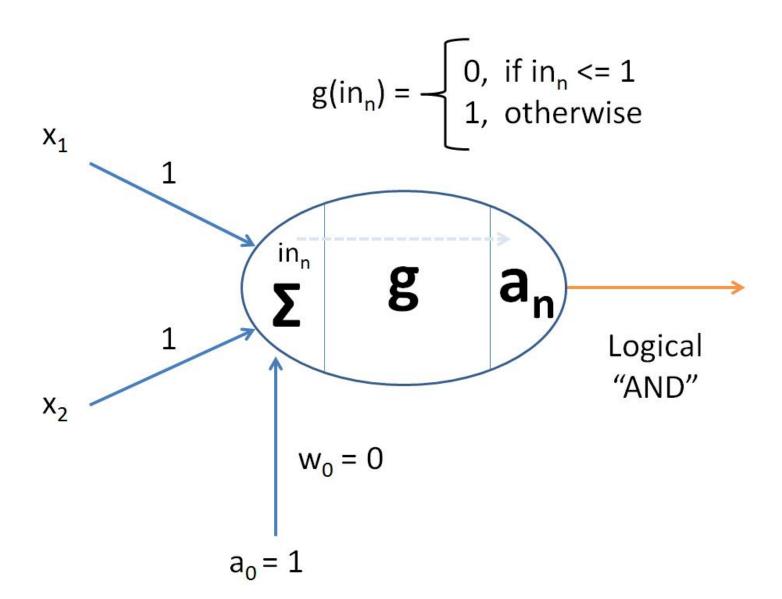


Which works out for the classification task of separating the 0 outcomes of a binary logical OR from the 1 outcomes:

Perceptron Logical "OR"

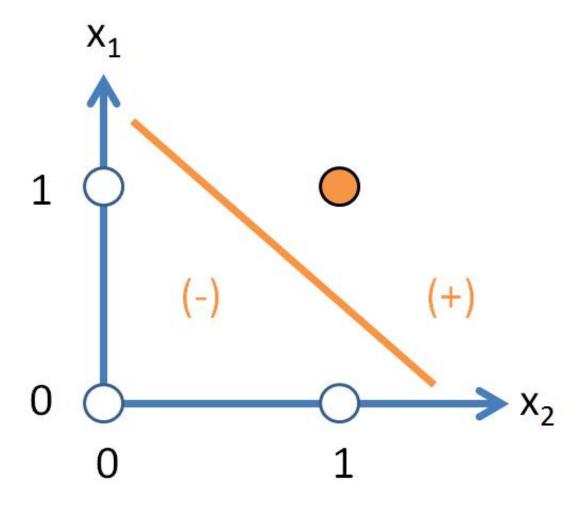


The same can be said of a perceptron that performs a logical, binary AND, i.e., outputs 1 iff both inputs are 1.



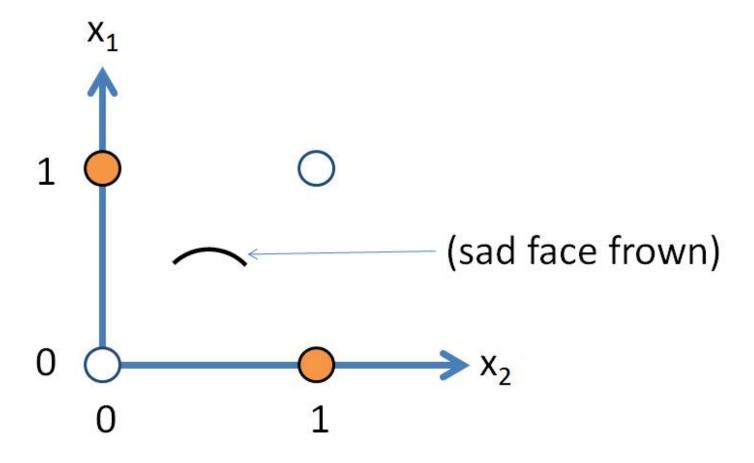
Which works out for the classification task of separating the 0 outcomes of the AND operation from the 1 outcomes:

Perceptron Logical "AND"



But what about logical XOR? i.e., returning 1 iff both inputs are different values:

Perceptron Logical "XOR"



Can't do it with a single dividing line like we did with AND and OR!

^á Perceptrons by themselves can only solve classification problems that are linearly-separable.

For this reason, we need to talk about **networks** of perceptrons that handle **non-linear regression**.

Feed-Forward Networks

Now that we have some concept of the individual perceptrons, we can talk about tying them together to handle interesting tasks!

^á A **feed-forward neural network** is one with some number of input and output nodes with edges that form a directed, acyclic graph.

In other words, our feed-forward networks only propagate their outputs towards the output nodes.

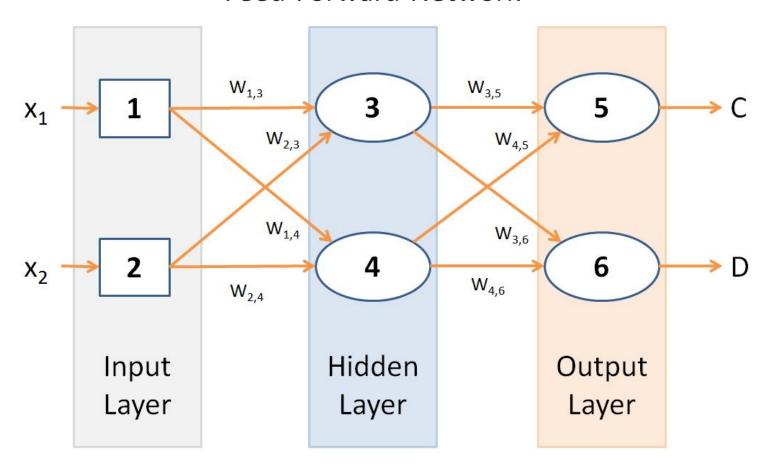
As such, we can connect layer after layer of neuron to one another with the outputs of neurons at level i serving as inputs to neurons at level i+1.

 $^{\acute{a}}$ A network's **input layer** for some vector of inputs X = (x1, x2, ...) sets each neuron's output in the input layer to its corresponding input value.

So, for input neurons 1, 2, ..., n the outputs of each is: (a1, a2, ..., an) = (x1, x2, ..., xn)

^á A network's **hidden layer** performs the internal computation for our network's task and are all neurons between the input and output layers.

Feed-Forward Network

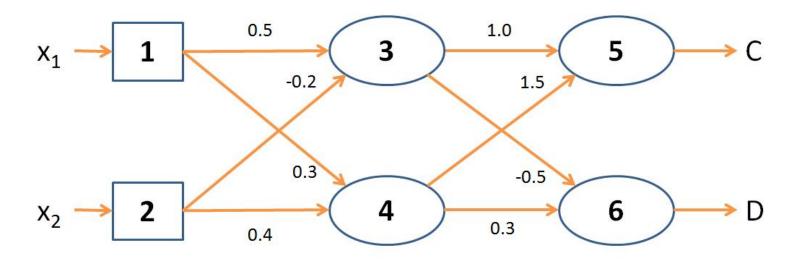


Here's an example:

Example

^t Say we had a simple, 3 layer network with 2 inputs, x1 and x2, and then 4 perceptrons (each with activation function g, which is a step function) with various output weights. What is the output of 5 and 6 (i.e., output values C and D), when x1 = 1 and x2 = 2? Assume a 0 weight for the bias input.

(for non-input layers): $g(in_i) = 1$, iff $in_i > 1$; 0 otherwise

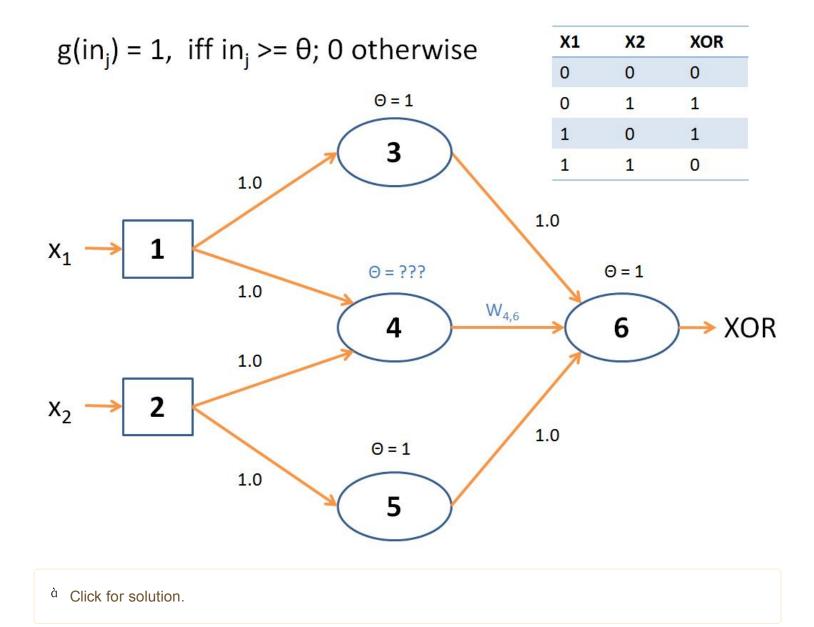


NOTE: In the above, our input layer still consists of neurons who just happen to be set to our input; they're still neurons due to their multiple output links, which isn't the case for the input values x1 and x2.

Now that we know about multi-layer networks, we can solve our XOR problem! Let's do that now.

Example

 $^{\rm t}$ Complete the following feed-forward perceptron network to elicit the XOR behavior of two binary inputs, x1 and x2. i.e., solve for Θ of node 4 and W_4,6



So, we see that our neural *networks* are really just **non-linear regressors** since we can find separations in classification problems that are non-linear so long as we use multiple neurons.

This brings us to the next section: how do we train our networks? What learning tools do we have available to us?

How to Train Your Neurons

One of the most powerful features of Neural Networks is to be able to learn a classification problem.

As a form of supervised learning, we can give our networks a vector of inputs X and a vector of the expected outputs for that input Y, and train our network to make correct output.

^d The learning **parameters** (i.e., what we have liberty to change in order to achieve our correct classification) in a neural network are its **weights**

Furthermore, since each weight affects only one other neuron at its link's terminus, for m weights in the network we actually perform m separate learning problems!

So, how do we fine tune our weights in order to get the proper output?

The trick is: we're going to guess!

We'll start by guessing the correct answer, and depending on how wildly we were wrong from the expected answer, we will then **update** our weights.

^d **Back-propagation learning** is the learning task whereby we successively update our network weights based on the given, expected outputs for given inputs.

The technique is called "back-propagation" because we always start by comparing our output guess to the actual answer, and then attempt to modify our weights to minimize error.

In this way, we are propagating the output error backwards in levels until we have changed the greatest weightoffenders (that might have led to a wrong answer) to their correct values.

One thing to note: although we're attempting to discover the proper weights that are appropriate given our network, we have no means of determining the actual network structure.

^d Cross validation techniques allow us to try several putative models, run back-prop and determine which had the best performance.

But, for now, we'll just assume that we had settled on some sort of network structure and now need to find the proper weights.

The backprop strategy is interested in the derivatives of our activation functions, and will use these to find a sort of gradient descent to minimizing error.

^á For this reason, the activation functions of our nodes must be differentiable.

Luckily, logistic functions have a nice derivative that will prove handy for an example. Before we look at the algorithm, a review of notation:

- w_i,j = the weight associated with a link from node i to node j
- x_i = an input from a training data point's input vector corresponding to input node i
- in j = the sum of weighted inputs to node j
- g(in_j) = the activation function for node j which is a function of the input weighted sum
- a j = the output of node j equivalent to g(in j)
- g'(in_j) = the derivative of the activation function of node j
- y_j = an output from a training data point's output vector corresponding to output node i
- Δ[j] = the error term associated with node j, i.e., how distant its output is compared to the expected one
- α = the learning rate, which is usually a small number like 0.01, which dictates how quickly our weights will
 change based on updates

Let's take a look at the algorithm and then start off an example in gory detail.

```
; Takes the network structure (network) and a set
; of training data (examples) to return a network
; with proper weight parameters set

function BACK-PROP-LEARNING (examples, network)
local variables: Δ, a vector of errors indexed by node

repeat

for each weight w_i,j in network do
    ; Seed network with our random guesses
    w_i,j = a small random number

; Example data point from training set with
; input vector x and expected output y
    for each example (x, y) in examples do

; Propagate the inputs, x, forward to
; obtain our outputs, and then compare to
; the expected
```

```
for each node i in the input layer do
             a i = x i
         ; Go through each hidden layer up to
         ; the output one, L
         for layer = 2 in L do
             ; Compute the inputs to every node
             for each node j in layer do
                  in j \leftarrow \Sigma i w i, j * a i
                  a j \leftarrow g(in j)
         ; At this point, we can compare the outputs
         ; that we got to the outputs we expected (y)
         ; and get an error term to store in the delta
         for each node j in output layer do
             ; Here g'(in_j) is the derivative of the
             ; activation function g(in j)
             \Delta[j] \leftarrow g'(in_j) * (y_j - a_j)
         ; Populate the errors of each node in the hidden
         ; layer
         for layer = L - 1 to 1 do
             for each node i in layer do
                  \Delta[i] \leftarrow g'(in i) * \Sigma j w i, j * \Delta[j]
         ; Finally, update the weights, where \alpha is our
         ; learning rate constant
         for each weight w i, j in network do
             w_i, j \leftarrow w_i, j + \alpha * a_i * \Delta[j]
until (MAX ITERATIONS reached) OR
       (Global error over \Delta below some minimum)
return network
```

Whew! That's a big algorithm! So notationally heavy!

Care to just glance at a small example (and not all of one, just a few steps)

Consider the following network and training sample where each activation function is the logistic function:

```
; Logistic function:
g(in_j) = 1 / (1 + e^(-in_j))

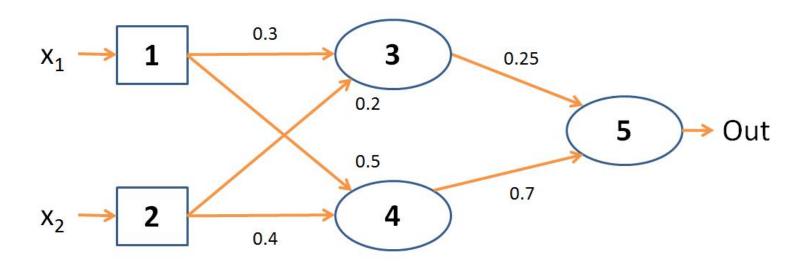
; Derivative of logistic function:
g'(in_j) = g(in_j) * (1 - g(in_j))
```

Now, consider the following (arbitrary) training set with input vector X and expected output vector Y.

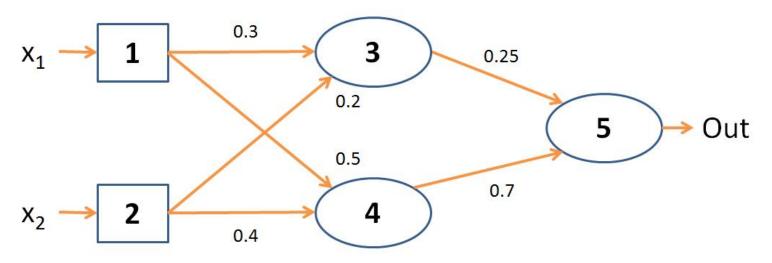
Case	x	Υ
1	{0.5, 1.0}	{0.2}
2	{0.3, 0.5}	{0.15}
3	{0.9, 0.4}	{0.8}
n		

And then we had the following network:

Step One: Seed weights with small random #s



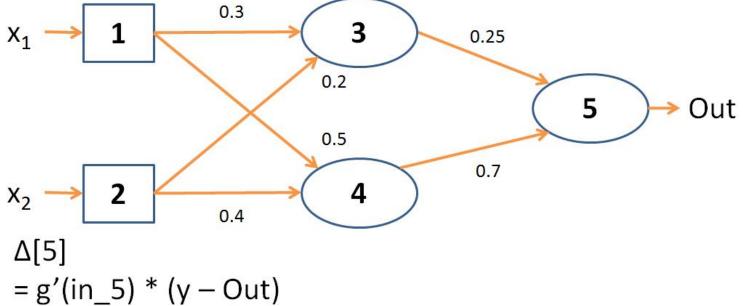
Step Two: Pick sample input X and propagate to Out $X = \{0.5, 1.0\}$



$$in_3 = 0.3 * 0.5 + 0.2 * 1.0 = 0.35$$
; $g(in_3) = 0.59 = a_3$
 $in_4 = 0.5 * 0.5 + 0.4 * 1.0 = 0.65$; $g(in_4) = 0.66 = a_4$
 $in_5 = 0.25 * 0.35 + 0.7 * 0.65 = 0.54$; $g(in_5) = 0.63 = a_5$

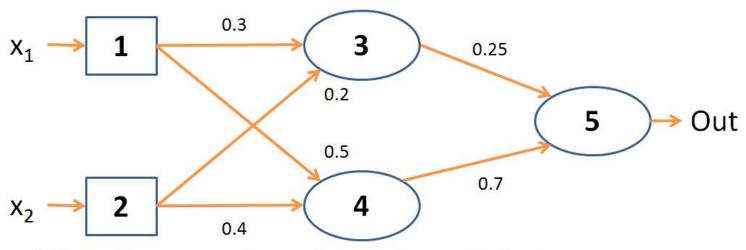
*Not shown: Bias node and weight (avoiding clutter)

Step Three: Find error in output compared to Y Y = 0.2; Out = 0.63



^{*}Not shown: Bias node and weight (avoiding clutter)

Step Four: Find deltas for each node (propagate back)! $\Delta[i] = g'(in_i) * \Sigma_i w_{i,j} * \Delta[j]$



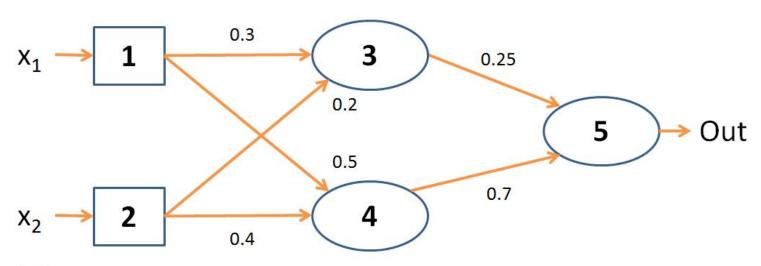
 $\Delta[3]$ (Do this for every node; not shown here because I'm lazy)

= g'(in_3) *
$$w_{i,j}$$
 * $\Delta[j]$
= g(in_3) * (1 - g(in_3)) * $w_{3,5}$ * $\Delta[5]$
= 0.59 * (1 - 0.59) * 0.25 * (-0.1) = -0.01

^{*}Not shown: Bias node and weight (avoiding clutter)

Step Five: Update weights

$$W_{i,j} = W_{i,j} + \alpha * a_i * \Delta[j]$$



 $W_{3.5}$ (Do this for every weight INCLUDING bias; not shown here because I'm lazy)

$$= w_{3,5} + \alpha * a_3 * \Delta[5]$$

=
$$0.25 + 0.1 * 0.59 * (-0.1)$$
; for $\alpha = 0.1$, (big α)

= 0.244

*Not shown: Bias node and weight (avoiding clutter)

Wow... that is just... wow.

Let's let that simmer for a bit...

At the end of this whole process, we end up with a network whose weights have hopefully been adjusted to fit our output requirements!

^d This is why, like Naive Bayes, neural networks are members of the **Probably, Approximately Correct** (PAC) algorithms and structures.

We can train to our sample data enough to generalize but we don't want to overtrain so we lose all flavor of generalizability.

Odds & Ends

Just to comment on the philosophical analyses of artificial intelligence, John Searle's Chinese Room Argument poses a thought-provoking glance into the boundaries of intelligence.

Questions about just what it meant for a machine to be "intelligent" arose after Turing's famous test for machine intelligence was posed, and continue to this day.

The Chinese Room scenario was posed by Searle in response to Turing's assertion that "intelligence" can be measured by the yardstick functionalism:

á A mental state is the abstract notion of a thought.

^á **Functionalism** asserts that a mental state is any intermediate causal condition between input and output.

In other words, given some input (like seeing a flower) evokes some thought about the input (the mental state) and then produces some behavioral output (like picking the flower).

In this capacity, if we were able to surgically replace all of the neurons in someone's brain with devices that reproduced the exact input-output of the neurons they replaced, then functionalists would argue that the mental state (i.e., the thought aspect of consciousness) remains unchanged.

Searle, and other **biological naturalists** like him, argue that consciousness would be disrupted, and someone who has undergone the above procedure would slowly lose their capacity for control.

^á **Biological naturalists** claim that mental state is not simply a neuronal-level product, but rather a higher level consequence of **patterns** of neural activation and unspecified properties of neurons.

In other words, the **high-level** notion of thought is a result of a bunch of separate interactions of the **low-level** neuronal activations.

Furthermore, there is something in the **unspecified** properties of neurons that allow for the notion of thought that we cannot encapsulate in a machine replacement.

The big difference in the two perspectives is this:

- Functionalists are OK with behavioral evidence of intelligence so long as a machine can reproduce humanlike responses to input.
- Biological naturalists claim that, although the input / output might be replicable, the mental state is not. As a tag phrase: "Brains (the physical) cause minds (thought)"

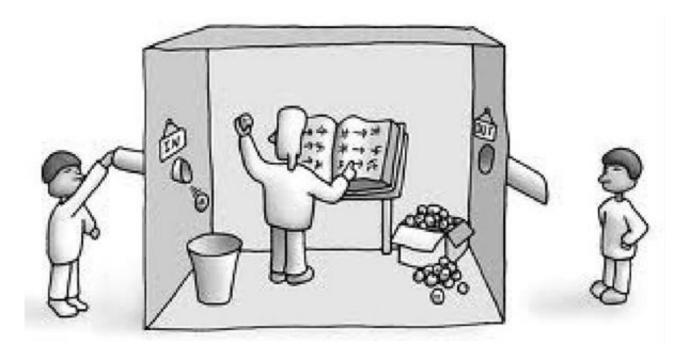
Put simply, machines might one day be able to mimic a human's behavior, but Searle claims that they'll never be able to rationalize why they are doing so or to think like a human does.

To illustrate his argument, Searle posed the Chinese Room scenario:

The Chinese Room Arugment

The scenario goes like this:

Suppose you have some human sitting in an isolated room with only two connections to the outside world: an **input** slot in which he may receive input on paper and an **output** slot on which he might send some paper out. Additionally, the man is equipped with a **rule book** that determines what the output should be given some sequence of inputs on paper. The man can also write what he wants on an infinite supply of paper.



Here's the catch: both the inputs on paper, and the outputs that the man is meant to reproduce, are **Chinese characters** and the man knows nothing about the Chinese language! Yet, by the dictations of the rule book, he is able to assess the given inputs and reproduce an output such that, to an outside observer, it will **appear** that the man understands Chinese!

then produce this shape,
"為天"
followed by this shape,
"下式".



Here, the man represents a computer's CPU and the input / output Chinese characters are simply the instructions being fed and retrieved from it.

The computer might be able to reproduce the expected output given the input, but that doesn't mean that it knows what it's doing!

There are a variety of critiques to Searle's critique, which you can find in the book, pgs. 1032 - 1033.

The chief of which are:

- Searle's argument is based on intuition rather than fact
- It is actually just speed that makes neural communication lead to thought, and that with sufficient speed in our computers we can simulate human thought.

Further Reading

You can view the Chinese Room argument in its glorious entirety here (http://plato.stanford.edu/entries/chinese-room/).

Farewell Announcements... (oxymoron?)

Week 10 already, how time has flown!

Just wanted to say what a pleasure it's been to be your TA--how much fun did we have?!

Some parting announcements:

^á If you haven't already filled out your **TA evaluations** for my discussion section, I implore you to do so! The feedback I get from you (who are technically my employers!) is vital and I'd love to know what worked and what didn't for you throughout the quarter.

Your **final** is this Monday, June 9th, at 6:30pm. Remember to bring a Blue Book! Apropos, be sure to peruse my practice final and relevant book chapters from Dr. Dyer's final topics note on CourseWeb.

Good luck all! Have fun with the final and enjoy the summer.