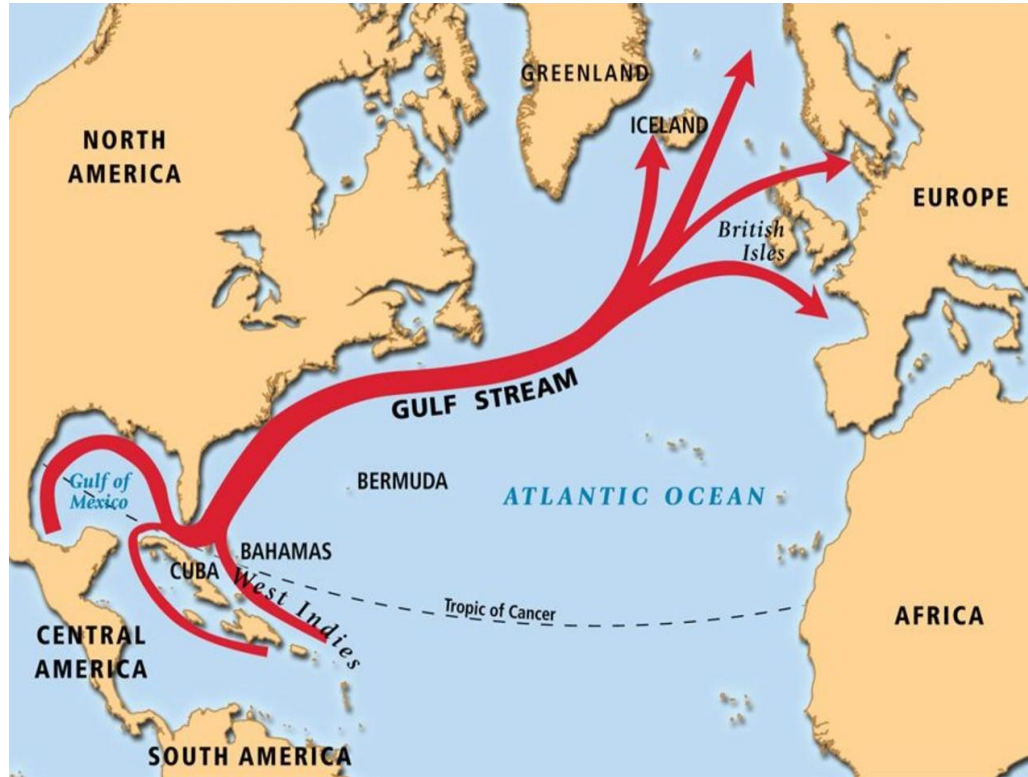


# Deep Learning for Physics

Foundations of AI's masterclass



# Marie Déchelle

## *Past*

Master in Machine Learning - Télécom ParisTech (Sophia Antipolis)

Master in Environmental Engineering - KTH (Sweden)

## *Present*

### **3rd year PhD student**

Neural Networks for the Modeling of Ocean Surface Dynamics

ISIR (Institut des Systèmes Intelligents et de Robotique) / LOCEAN (Laboratoire d'Océanographie et du Climat)



# Modeling Dynamical Systems

**System** = a set of things working together as parts of a mechanism

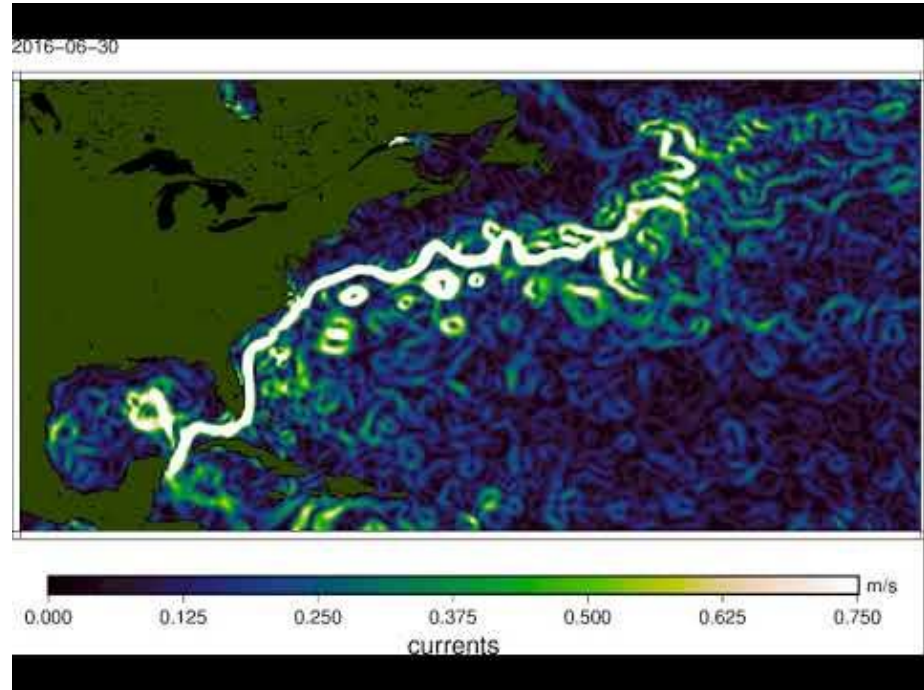
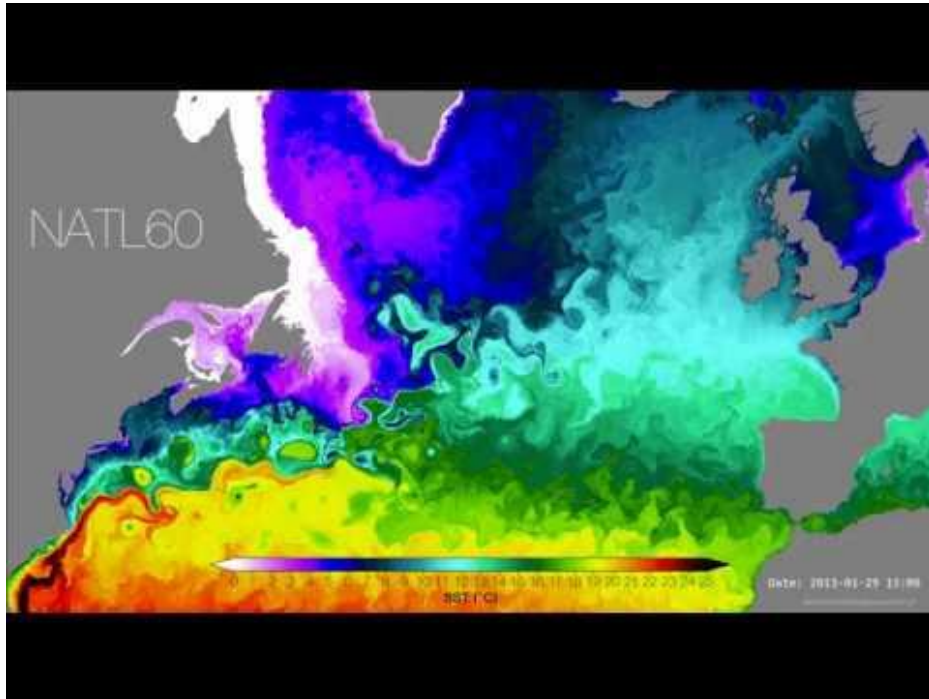
**Dynamical system** = system and a law describing the evolution of the system



**We are interested in predicting the evolution of the system of interest.**

→ we seek for the law describing the evolution of the system

# Ocean Surface Dynamics



# Ocean Modeling

Necessary to model climate.

Rely on a very old knowledge...

Claude-Louis Navier (1822) and George Gabriel Stokes (1840s) described the motion of viscous fluid substances with **differential equations**:

$$\frac{\partial X_t}{\partial t} = f(X_t, t)$$

where  $X_t$  stands for temperature, pressure, currents velocity, salinity, heat exchanges,...

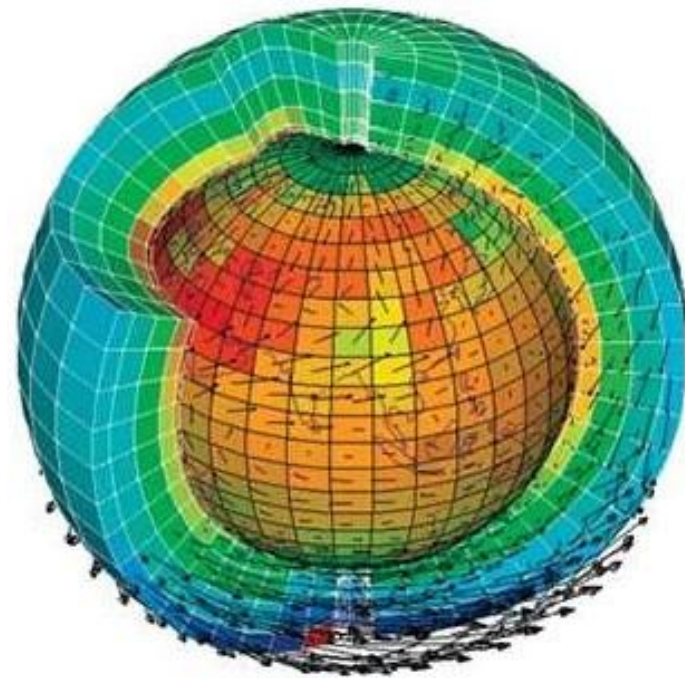
Traditional approach : we know  $f$  and use it to predict  $X_t$  at future timesteps.





# Ocean Modeling

- Ocean models are based on a 3D grid representing the entire ocean
- Each variable is constant for each grid point.
- Current model : grid points with 100km-sides



## Problems still unsolved...

- Computationally infeasible to run models at fine resolution in space and time
- Processes which are not completely understood
- Uncertainty Quantification

# Data-driven models and physics

- Success of machine learning (ML) for multiple tasks in computer vision, NLP,...
- Available data (satellites, floats,...)
- How could ML help for physics ?

$$\frac{\partial X_t}{\partial t} = f(X_t, t)$$

Models rely on a new approach : we learn  $f$  to predict  $X_{t+1}$

**Note the paradigm shift : such models don't rely on physical knowledge !**

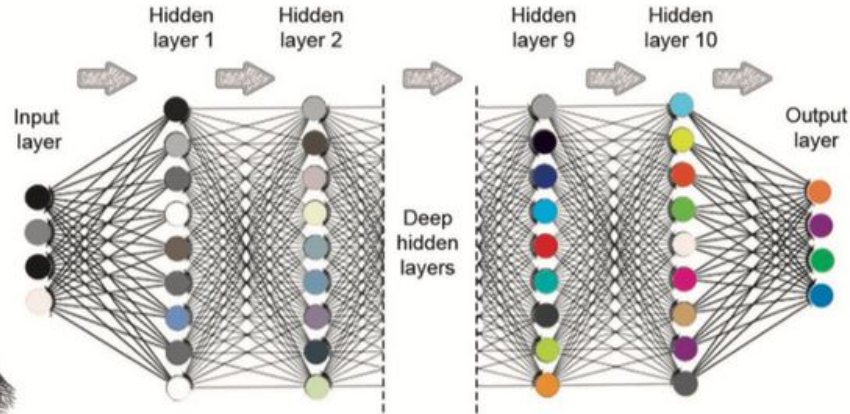
Problems:

- Complex systems : lots of interactions, lots of variables
- Interpretability : we want our model to respect the underlying physics
- Learning may be unsupervised

# Best of both worlds ?

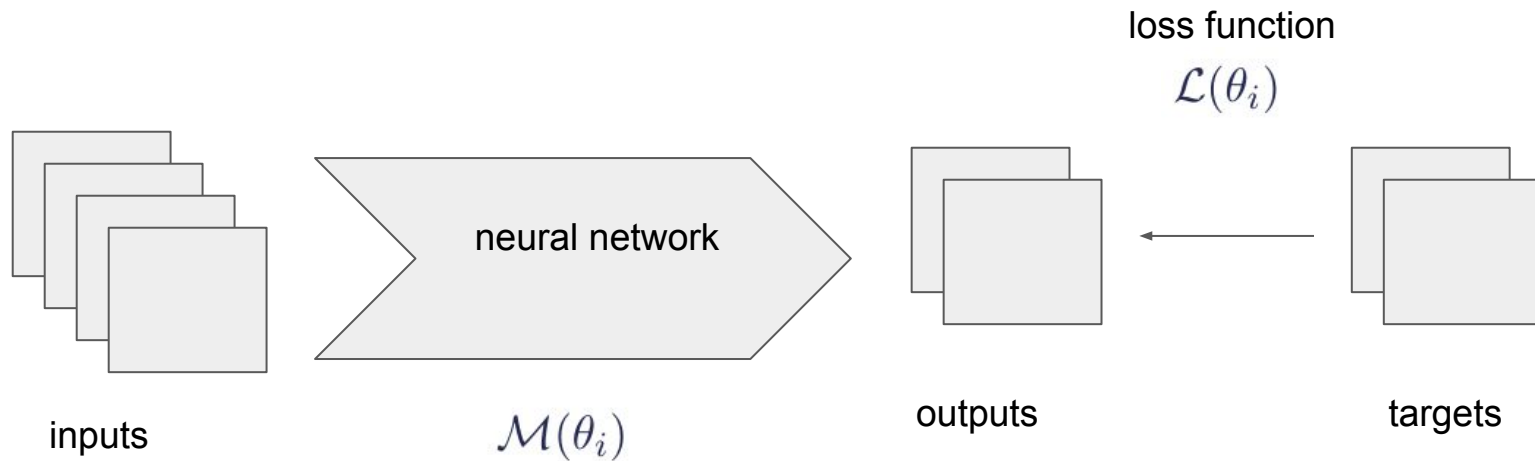
Physics-guided learning is a very recent topic...

2 publications in 2017, 8 in 2018, 27 in 2019, 63 in 2020 !





# Physics-guided learning

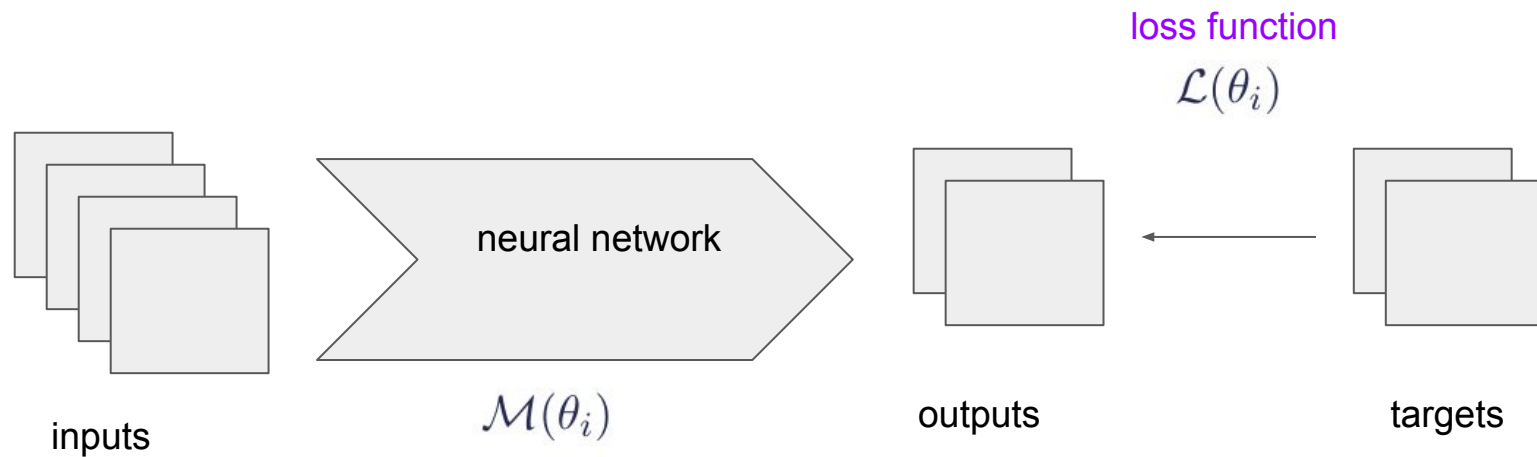


Inputs: coordinates (latitude, longitude), variable of interest (ex: temperature), ...

Outputs: variable at coordinates, prediction, ...

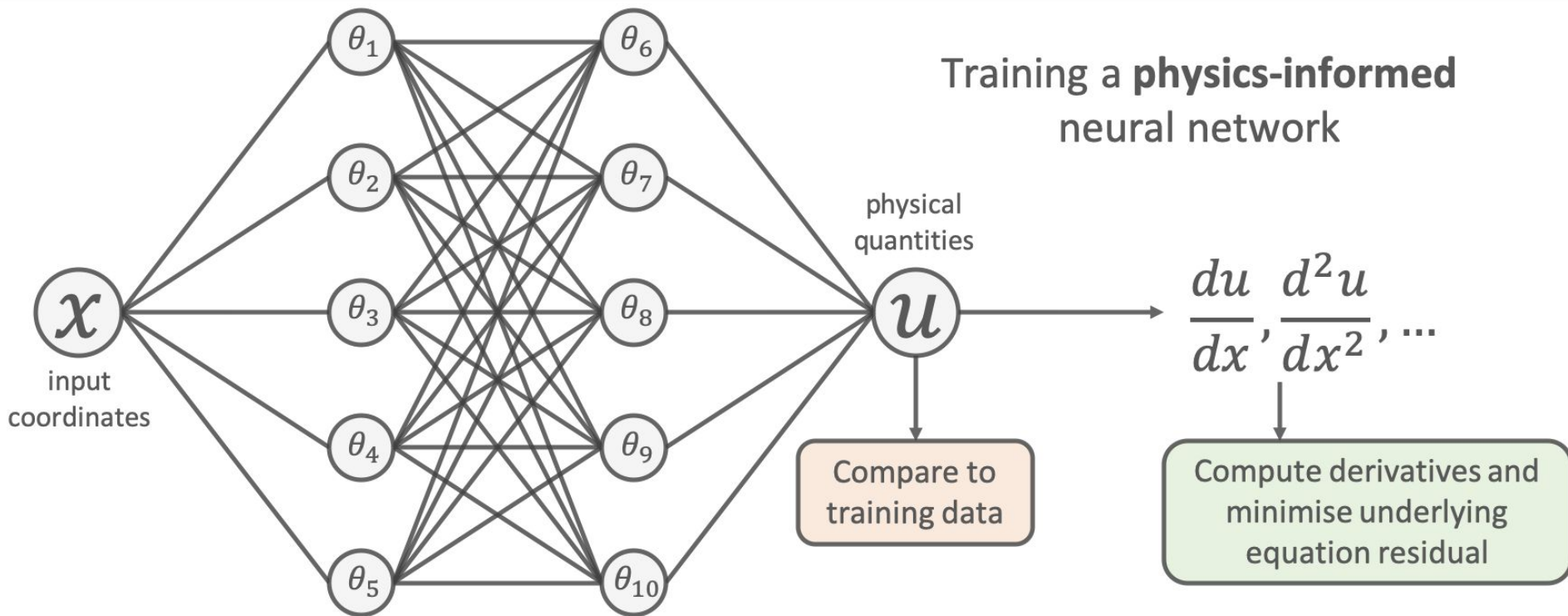
**How to integrate scientific knowledge into the ML framework ?**

# Physics-guided learning

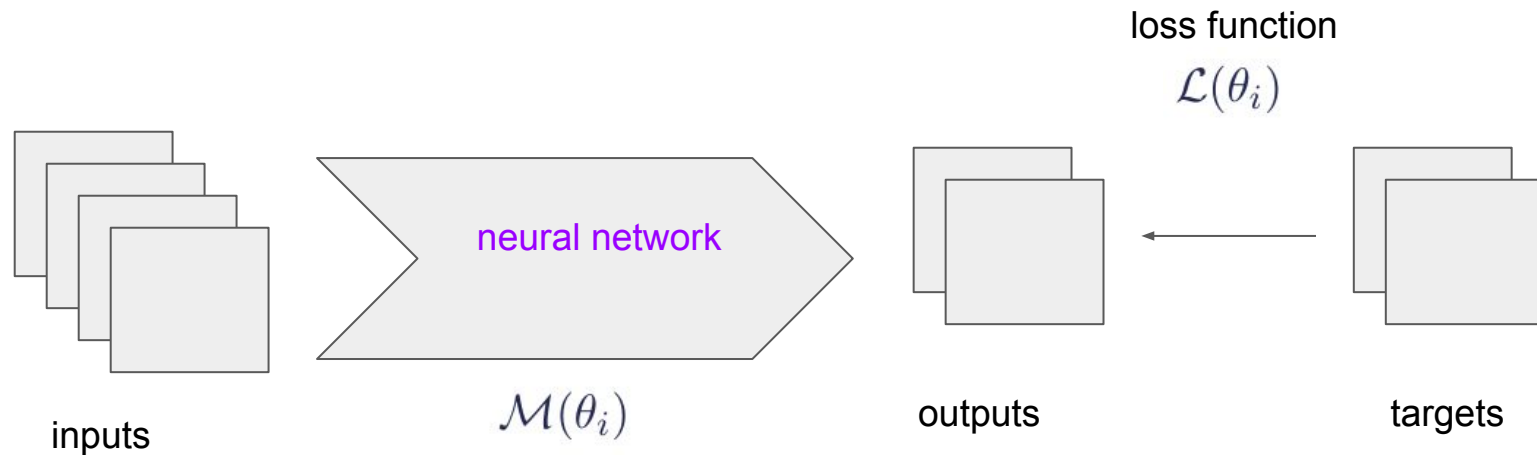


# Physics-guided learning

## Physics-informed neural network



# Physics-guided learning



New area of research : hybrid physics-ML modeling

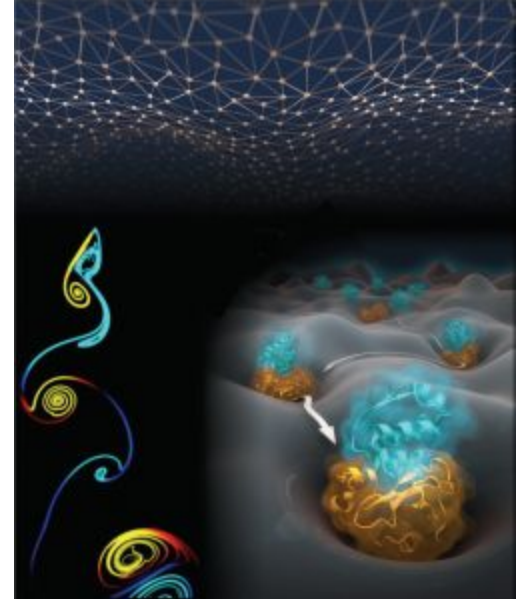
$$\frac{\partial X_t}{\partial t} = f(X_t, t) = (f_p + f_d)(X_t, t)$$

the known part of the dynamics (physical knowledge)

the unknown part of the dynamics (to be learnt)

# Conclusion

- Two paradigms to model dynamical systems : knowledge-based and data-driven
- Physics-guided learning : how to integrate knowledge into the ML framework ?
- Lots of possible applications...



Thank you very much !



# Hybrid Physics-ML models

$$\frac{\partial X_t}{\partial t} = f(X_t, t) = (f_p + f_d)(X_t, t)$$

where  $f$  is the dynamics associated to  $X_t$

which we decompose into

$f_p$  the known part of the dynamics (physical knowledge)  
it relies on physical knowledge, but still depends on unknown parameters  $\theta_p$  such that

$$f_p = f_p(\theta_p)$$

$f_d$  the unknown part of the dynamics (to be learnt)

# Hybrid Physics-ML models

$$\frac{\partial X_t}{\partial t} = f(X_t, t) = (f_p + f_d)(X_t, t)$$

Possible pitfall:

- $f_d$  may learn all the dynamics  $f$
- In this case, the hybrid model has no physical sense anymore !

→ We have to constrain both  $f_p$  and  $f_d$

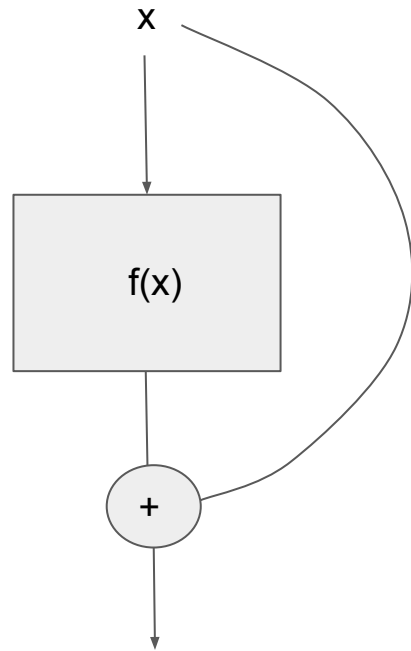
# Physics-guided learning

## Physics-guided design of architecture

Established link between residual networks and

$$\frac{\partial X_t}{\partial t} = f(X_t, t)$$

$$X_{t+\Delta t} = X_t + \Delta t f(X_t, t)$$



# Hybrid Physics-ML ocean models

$$\begin{aligned}\frac{\partial T}{\partial t} &= -\nabla \cdot (TU) + D^T + F^T \\ &= f_p(T, U) + f_d(T)\end{aligned}$$

where  $T$  is the surface temperature. It is observed with satellites.

$U$  is the surface velocity. It is unobserved !

$f_p$  the known part of the dynamics (physical knowledge)  
it relies on physical knowledge, but still depends on unknown parameters  $U$

$f_d$  the unknown part of the dynamics (to be learnt)

# Hybrid Physics-ML ocean models

$$\begin{aligned}\frac{\partial T}{\partial t} &= -\nabla \cdot (TU) + D^T + F^T \\ &= f_p(T, U) + f_d(T)\end{aligned}$$

We have to learn both  $U$  and  $f_d$

Possible pitfall:

- $f_d$  may learn all the dynamics
- In this case, the hybrid model has no physical sense anymore !

→ We have to constrain both  $f_p$  and  $f_d$