```
In [9]: import Pkg
        Pkg.activate(@ DIR )
        Pkg.instantiate()
        using LinearAlgebra, Plots; plotly()
        import ForwardDiff as FD
        import MeshCat as mc
        using Test
        using Random
        import Convex as cvx
        import ECOS  # the solver we use in this hw
        # import Hypatia # other solvers you can try
        # import COSMO # other solvers you can try
        using ProgressMeter
        include(joinpath(@__DIR__, "utils/rendezvous.jl"))
          Activating environment at `~/ocrl_ws/16745-ocrl/HW2_S23/Project.toml`
          Warning: For saving to png with the `Plotly` backend `PlotlyBase` and `PlotlyKaleido` need to be installed.
            err =
             ArgumentError: Package PlotlyBase not found in current path:
             - Run `import Pkg; Pkg.add("PlotlyBase")` to install the PlotlyBase package.
          @ Plots ~/.julia/packages/Plots/9Q9pN/src/backends.jl:552
```

Q3

Out[9]: thruster model (generic function with 1 method)

Notes:

- 1. Some of the cells below will have multiple outputs (plots and animations), it can be easier to see everything if you do Cell -> All Output -> Toggle Scrolling, so that it simply expands the output area to match the size of the outputs.
- 2. Things in space move very slowly (by design), because of this, you may want to speed up the animations when you're viewing them. You can do this in MeshCat by doing Open Controls -> Animations -> Time Scale, to modify the time scale. You can also play/pause/scrub from this menu as well.
- 3. You can move around your view in MeshCat by clicking + dragging, and you can pan with right click + dragging, and zoom with the scroll wheel on your mouse (or trackpad specific alternatives).

Out[10]: vec_from_mat (generic function with 1 method)

Is LQR the answer for everything?

Unfortunately, no. LQR is great for problems with true quadratic costs and linear dynamics, but this is a very small subset of convex trajectory optimization problems. While a quadratic cost is common in control, there are other available convex cost functions that may better motivate the desired behavior of the system. These costs can be things like an L1 norm on the control inputs ($||u||_1$), or an L2 goal error ($||x-x_{goal}||_2$). Also, control problems often have constraints like path constraints, control bounds, or terminal constraints, that can't be handled with LQR. With the addition of these constraints, the trajectory optimization problem is stil convex and easy to solve, but we can no longer just get an optimal gain K and apply a feedback policy in these situations.

The solution to this is Model Predictive Control (MPC). In MPC, we are setting up and solving a convex trajectory optimization at every time step, optimizing over some horizon or window into the future, and executing the first control in the solution. To see how this works, we are going to try this for a classic space control problem: the rendezvous.

Q3: Optimal Rendezvous and Docking (50 pts)

In this example, we are going to use convex optimization to control the SpaceX Dragon 1 spacecraft as it docks with the International Space Station (ISS). The dynamics of the Dragon vehicle can be modeled with Clohessy-Wiltshire equations, which is a linear dynamics model in continuous time. The state and control of this system are the following:

$$x = [r_x, r_y, r_z, v_x, v_y, v_z]^T, (1)$$

$$u = [t_x, t_y, t_z]^T, \tag{2}$$

where r is a relative position of the Dragon spacecraft with respect to the ISS, v is the relative velocity, and t is the thrust on the spacecraft. The continuous time dynamics of the vehicle are the following:

10/03/2023, 22:33

$$\dot{x} = \begin{bmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 3n^2 & 0 & 0 & 0 & 2n & 0 \\ 0 & 0 & 0 & -2n & 0 & 0 \\ 0 & 0 & -n^2 & 0 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} u, \tag{3}$$

where $n=\sqrt{\mu/a^3}$, with μ being the standard gravitational parameter, and a being the semi-major axis of the orbit of the ISS.

We are going to use three different techniques for solving this control problem, the first is LQR, the second is convex trajectory optimization, and the third is convex MPC where we will be able to account for unmodeled dynamics in our system (the "sim to real" gap).

Q3

Part A: Discretize the dynamics (5 pts)

Use the matrix exponential to convert the linear ODE into a linear discrete time model (hint: the matrix exponential is just exp() in Julia when called on a matrix.

```
In [11]: | function create_dynamics(dt::Real)::Tuple{Matrix,Matrix}
            mu = 3.986004418e14 # standard gravitational parameter
            a = 6971100.0  # semi-major axis of ISS
            n = sqrt(mu/a^3) # mean motion
            # continuous time dynamics \dot{x} = Ax + Bu
                      0 0 1 0 0;
                      0 0 0 1 0;
                      0 0 0 0 1;
                 0
                 3*n^2 0 0 0 2*n 0;
                    0 0 -2*n 0 0;
                      0 -n^2 0 0 0]
            B = Matrix([zeros(3,3);0.1*I(3)])
            nx, nu = size(B)
            # TODO: convert to discrete time X_{k+1} = Ad*x_k + Bd*u_k
              Ad = zeros(6,6)
              Bd = zeros(6,3)
            expmat = exp([A B; zeros(nu, nx + nu)] .* dt)
            Ad = expmat[1:nx,1:nx]
            Bd = expmat[1:nx,nx+1:nx+nu]
            return Ad, Bd
        end
```

Out[11]: create_dynamics (generic function with 1 method)

```
discrete dynamics | 3 3
Out[12]: Test.DefaultTestSet("discrete dynamics", Any[], 3, false, false)
```

Part B: LQR (10 pts)

Now we will take a given reference trajectory X_ref and track it with finite-horizon LQR. Remember that finite-horizon LQR is solving this problem:

$$\min_{x_{1:N}, u_{1:N-1}} \quad \sum_{i=1}^{N-1} \left[\frac{1}{2} (x_i - x_{ref,i})^T Q(x_i - x_{ref,i}) + \frac{1}{2} u_i^T R u_i \right] + \frac{1}{2} (x_N - x_{ref,N})^T Q_f(x_N - x_{ref,N})$$
(4)

st
$$x_1 = x_{\rm IC}$$
 (5)

$$x_{i+1} = Ax_i + Bu_i \quad \text{for } i = 1, 2, \dots, N-1$$
 (6)

where our policy is $u_i = -K_i(x_i - x_{ref,i})$. Use your code from the previous problem with your fhlqr function to generate your gain matrices.

One twist we will throw into this is control constraints u_min and u_max . You should use the function $clamp.(u, u_min, u_max)$ to clamp the values of your u to be within this range.

If implemented correctly, you should see the Dragon spacecraft dock with the ISS successfuly, but only after it crashes through the ISS a little bit.

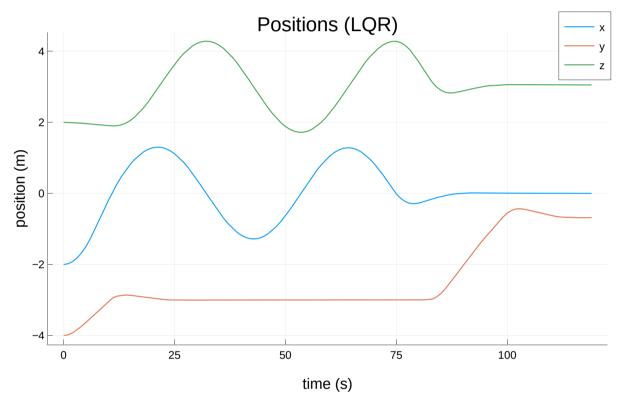
Q3

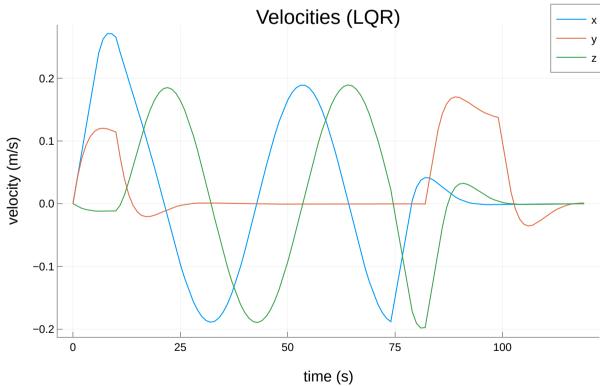
```
In [13]: function fhlqr(A::Matrix, # A matrix
                         B::Matrix, # B matrix
                         Q::Matrix, # cost weight
                         R::Matrix, # cost weight
                         Qf::Matrix,# term cost weight
                         N::Int64 # horizon size
                         )::Tuple{Vector{Matrix{Float64}}}, Vector{Matrix{Float64}}} # return two matrices
             # check sizes of everything
             nx,nu = size(B)
             @assert size(A) == (nx, nx)
             @assert size(Q) == (nx, nx)
             @assert size(R) == (nu, nu)
             @assert size(Qf) == (nx, nx)
             # instantiate S and K
             P = [zeros(nx,nx) for i = 1:N]
             K = [zeros(nu,nx) for i = 1:N-1]
             # initialize S[N] with Qf
             P[N] = deepcopy(Qf)
             # Ricatti
             for k = N-1:-1:1
                 # TODO
                 K[k] = (R + B' * P[k+1] * B) \setminus (B' * P[k+1] * A)
                  P[k] = Q + A' * P[k+1] * (A - B * K[k])
             end
              return P, K
         end
```

Out[13]: fhlqr (generic function with 1 method)

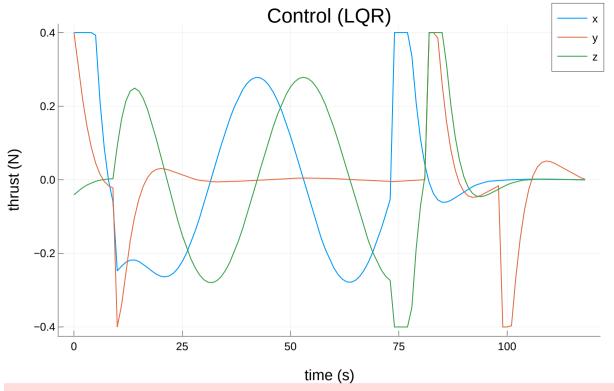
```
In [14]: @testset "LQR rendezvous" begin
             # create our discrete time model
             A,B = create_dynamics(dt)
             # get our sizes for state and control
             nx,nu = size(B)
             # initial and goal states
             x0 = [-2; -4; 2; 0; 0; .0]
             xg = [0, -.68, 3.05, 0, 0, 0]
             # bounds on U
             u_max = 0.4*ones(3)
             u_min = -u_max
             # problem size and reference trajectory
             N = 120
             t_{vec} = 0:dt:((N-1)*dt)
             X_ref = desired_trajectory_long(x0,xg,200,dt)[1:N]
             # TODO: FHLQR
             Q = diagm(ones(nx))
             R = diagm(ones(nu))
             Qf = 10*Q
             # TODO get K's from fhlqr
             P, K = fhlqr(A,B,Q,R,Qf,N)
             # simulation
             X_{sim} = [zeros(nx) for i = 1:N]
             U \sin = [zeros(nu) \text{ for } i = 1:N-1]
             X_{sim}[1] = x0
             for i = 1:(N-1)
                 # TODO: put LQR control law here
                 # make sure to clamp
                 U_sim[i] = -K[i]* (X_sim[i] - X_ref[i])
                   U_sim[i] = -K[i] * X_sim[i]
                  U_{sim}[i] = clamp.(U_{sim}[i], u_{min}, u_{max})
                  # simulate 1 step
                  X_{sim[i+1]} = A*X_{sim[i]} + B*U_{sim[i]}
             # -----plotting/animation-----
             Xm = mat_from_vec(X_sim)
```

```
Um = mat_from_vec(U_sim)
   display(plot(t_vec,Xm[1:3,:]',title = "Positions (LQR)",
               xlabel = "time (s)", ylabel = "position (m)",
               label = ["x" "y" "z"]))
   display(plot(t_vec,Xm[4:6,:]',title = "Velocities (LQR)",
          xlabel = "time (s)", ylabel = "velocity (m/s)",
               label = ["x" "y" "z"]))
   display(plot(t_vec[1:end-1],Um',title = "Control (LQR)",
           xlabel = "time (s)", ylabel = "thrust (N)",
               label = ["x" "y" "z"]))
   # feel free to toggle `show_reference`
   display(animate_rendezvous(X_sim, X_ref, dt;show_reference = false))
   # -----plotting/animation-----
   # testing
   xs=[x[1] for x in X_sim]
   ys=[x[2] for x in X_sim]
   zs=[x[3] for x in X_sim]
   [end] - xg < .01 \# goal
   @test maximum(zs) >= 4 # check to see if you did the circle
   @test minimum(zs) <= 2 # check to see if you did the circle</pre>
   @test maximum(xs) >= 1 # check to see if you did the circle
   @test maximum(norm.(U_sim,Inf)) <= 0.4 # control constraints satisfied</pre>
end
```

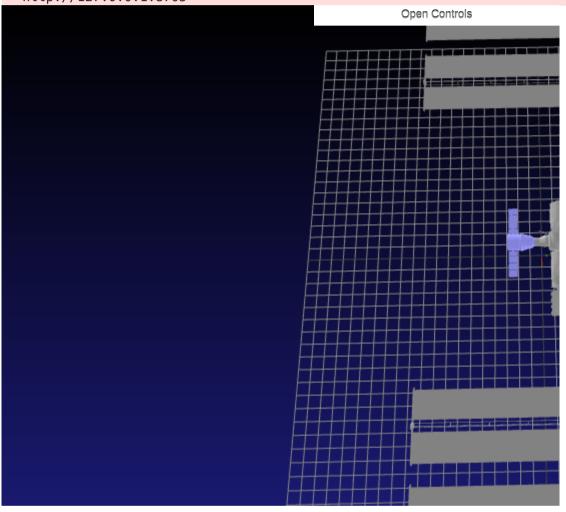




10/03/2023, 22:33 Q3



Info: MeshCat server started. You can open the visualizer by visiting the following URL in your browser: http://127.0.0.1:8705



Test Summary: | Pass Total
LQR rendezvous | 6 6

Out[14]: Test.DefaultTestSet("LQR rendezvous", Any[], 6, false, false)

Part C: Convex Trajectory Optimization (15 pts)

Now we are going to assume that we have a perfect model (assume there is no sim to real gap), and that we have a perfect state estimate. With this, we are going to solve our control problem as a convex trajectory optimization problem.

$$\min_{x_{1:N}, u_{1:N-1}} \quad \sum_{i=1}^{N-1} \left[\frac{1}{2} (x_i - x_{ref,i})^T Q(x_i - x_{ref,i}) + \frac{1}{2} u_i^T R u_i \right] + \frac{1}{2} (x_N - x_{ref,N})^T Q_f(x_N - x_{ref,N})$$
(7)

st
$$x_1 = x_{\rm IC}$$
 (8)

$$x_{i+1} = Ax_i + Bu_i \quad \text{for } i = 1, 2, \dots, N-1$$
 (9)

$$u_{min} \leq u_i \leq u_{max} \quad ext{for } i=1,2,\ldots,N-1$$

$$x_i[2] \le x_{goal}[2] \quad \text{for } i = 1, 2, \dots, N$$
 (11)

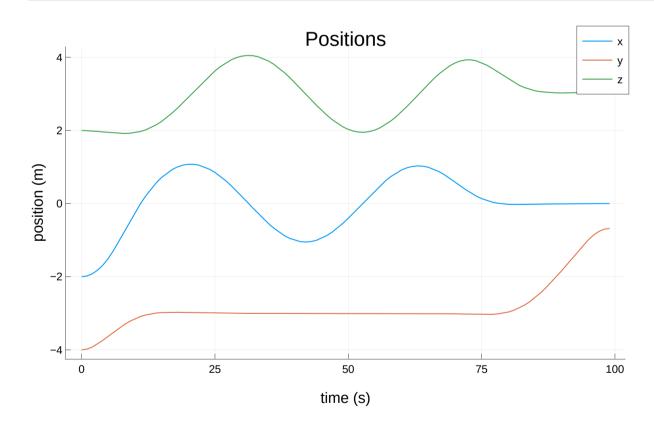
 $x_N = x_{goal}$ (12)

Where we have an LQR cost, an initial condition constraint $(x_1=x_{\rm IC})$, linear dynamics constraints $(x_{i+1}=Ax_i+Bu_i)$, bound constraints on the control ($\leq u_i \leq u_{max}$), an ISS collision constraint $(x_i[2] \leq x_{goal}[2])$, and a terminal constraint $(x_N=x_{goal})$. This problem is convex and we will setup and solve this with Convex.jl.

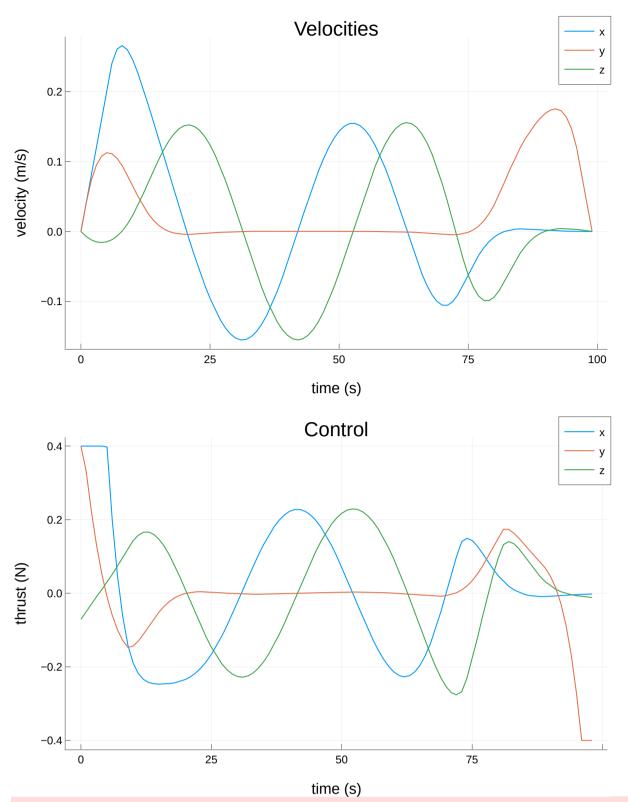
In [15]:
 """
 Xcvx,Ucvx = convex_trajopt(A,B,X_ref,x0,xg,u_min,u_max,N)
 setup and solve the above optimization problem, returning
 the solutions X and U, after first converting them to

```
vectors of vectors with vec_from_mat(X.value)
function convex_trajopt(A::Matrix, # discrete dynamics A
                        B::Matrix, # discrete dynamics B
                        X_ref::Vector{Vector{Float64}}, # reference trajectory
                        x0::Vector, # initial condition
                        xg::Vector, # goal state
                        u_min::Vector, # lower bound on u
                        u_max::Vector, # upper bound on u
                        N::Int64, # length of trajectory
                        )::Tuple{Vector{Float64}}, Vector{Vector{Float64}}} # return Xcvx,Ucvx
    # get our sizes for state and control
    nx,nu = size(B)
    @assert size(A) == (nx, nx)
    @assert length(x0) == nx
    @assert length(xg) == nx
    # LQR cost
    Q = diagm(ones(nx))
    R = diagm(ones(nu))
    # variables we are solving for
    X = cvx.Variable(nx,N)
    U = cvx.Variable(nu,N-1)
    Xref = mat_from_vec(X_ref)
    # TODO: implement cost
    obj = 0
    for k = 1:(N-1)
        # add stagewise cost
        xk = X[:,k]
        uk = U[:,k]
        xrefk = Xref[:,k]
        obj += (0.5 * cvx.quadform(xk - xrefk,Q))
        obj += (0.5 * cvx.quadform(uk,R))
    obj += (0.5 * cvx.quadform(X[:,N] - Xref[:,N],Q))
    # create problem with objective
    prob = cvx.minimize(obj)
    # TODO: add constraints with prob.constraints +=
    prob.constraints += (X[:,1] == x0)
    for k = 1:(N-1)
        # dynamics constraints
        prob.constraints += (X[:,k+1] == A*X[:,k] + B*U[:,k])
        prob.constraints += (U[:,k] <= u_max)</pre>
        prob.constraints += (U[:,k] >= u_min)
        prob.constraints += (X[2,k] \le xg[2])
   end
    prob.constraints += (X[2,N] \le xg[2])
    prob.constraints += (X[:,N] == xg)
    cvx.solve!(prob, ECOS.Optimizer; silent_solver = true)
    X = X.value
    U = U.value
    Xcvx = vec from mat(X)
    Ucvx = vec_from_mat(U)
    return Xcvx, Ucvx
end
@testset "convex trajopt" begin
    # create our discrete time model
    dt = 1.0
    A,B = create_dynamics(dt)
    # get our sizes for state and control
    nx,nu = size(B)
    # initial and goal states
    x0 = [-2; -4; 2; 0; 0; .0]
    xg = [0, -.68, 3.05, 0, 0, 0]
    # bounds on U
    u \max = 0.4*ones(3)
    u_min = -u_max
    # problem size and reference trajectory
```

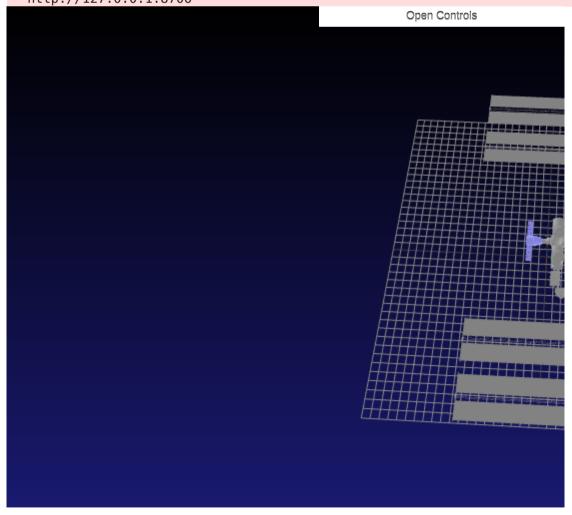
```
N = 100
   t_{vec} = 0:dt:((N-1)*dt)
   X_ref = desired_trajectory(x0,xg,N,dt)
   # solve convex trajectory optimization problem
   X_{cvx}, U_{cvx} = convex_{trajopt}(A,B,X_{ref}, x0,xg,u_{min},u_{max},N)
   X_{sim} = [zeros(nx) for i = 1:N]
   X sim[1] = x0
   for i = 1:N-1
       X_{sim[i+1]} = A*X_{sim[i]} + B*U_{cvx[i]}
   # -----plotting/animation-----
   Xm = mat from vec(X sim)
   Um = mat_from_vec(U_cvx)
   display(plot(t vec,Xm[1:3,:]',title = "Positions",
                xlabel = "time (s)", ylabel = "position (m)",
                label = ["x" "y" "z"]))
   display(plot(t vec,Xm[4:6,:]',title = "Velocities",
           xlabel = "time (s)", ylabel = "velocity (m/s)",
                label = ["x" "y" "z"]))
   display(plot(t_vec[1:end-1],Um',title = "Control",
           display(animate_rendezvous(X_sim, X_ref, dt;show_reference = false))
   # -----plotting/animation-----
   @test maximum(norm.( X_sim .- X_cvx, Inf)) < 1e-3</pre>
   @test norm(X_sim[end] - xg) < 1e-3 # goal</pre>
   xs=[x[1] for x in X_sim]
   ys=[x[2] for x in X_sim]
   zs=[x[3]  for x  in X_sim]
    \text{@test maximum(ys)} \leftarrow (xg[2] + 1e-3) 
   @test maximum(zs) >= 4 # check to see if you did the circle
   @test minimum(zs) <= 2 # check to see if you did the circle</pre>
   @test maximum(xs) >= 1 # check to see if you did the circle
   @test maximum(norm.(U_cvx,Inf)) <= 0.4 + 1e-3 # control constraints satisfied</pre>
end
```



10/03/2023, 22:33 Q3



Info: MeshCat server started. You can open the visualizer by visiting the following URL in your browser: http://127.0.0.1:8706



Test Summary: | Pass Total
convex trajopt | 7 7

Out[15]: Test.DefaultTestSet("convex trajopt", Any[], 7, false, false)

Part D: Convex MPC (20 pts)

In part C, we solved for the optimal rendezvous trajectory using convex optimization, and verified it by simulating it in an open loop fashion (no feedback). This was made possible because we assumed that our linear dynamics were exact, and that we had a perfect estimate of our state. In reality, there are many issues that would prevent this open loop policy from being successful, here are a few:

- · imperfect state estimation
- · unmodeled dynamics
- misalignments
- · actuator uncertainties

Together, these factors result in a "sim to real" gap between our simulated model, and the real model. Because there will always be a sim to real gap, we can't just execute open loop policies and expect them to be successful. What we can do, however, is use Model Predictive Control (MPC) that combines some of the ideas of feedback control with convex trajectory optimization.

A convex MPC controller will set up and solve a convex optimization problem at each time step that incorporates the current state estimate as an initial condition. For a trajectory tracking problem like this rendezvous, we want to track x_{ref} , but instead of optimizing over the whole trajectory, we will only consider a sliding window of size N_{mpc} (also called a horizon). If $N_{mpc}=20$, this means our convex MPC controller is reasoning about the next 20 steps in the trajectory. This optimization problem at every timestep will start by taking the relevant reference trajectory at the current window from the current step i, to the end of the window $i+N_{mpc}-1$. This slice of the reference trajectory that applies to the current MPC window will be called $\tilde{x}_{ref}=x_{ref}[i,(i+N_{mpc}-1)]$.

$$\min_{x_{1:N}, u_{1:N-1}} \quad \sum_{i=1}^{N-1} \left[\frac{1}{2} (x_i - \tilde{x}_{ref,i})^T Q(x_i - \tilde{x}_{ref,i}) + \frac{1}{2} u_i^T R u_i \right] + \frac{1}{2} (x_N - \tilde{x}_{ref,N})^T Q_f(x_N - \tilde{x}_{ref,N})$$
(13)

$$x_{i+1} = Ax_i + Bu_i \quad \text{for } i = 1, 2, \dots, N-1$$
 (15)

$$u_{min} \le u_i \le u_{max} \quad \text{for } i = 1, 2, \dots, N - 1 \tag{16}$$

$$x_i[2] \le x_{goal}[2] \quad \text{for } i = 1, 2, \dots, N \tag{17}$$

where N in this case is N_{mpc} . This allows for the MPC controller to "think" about the future states in a way that the LQR controller cannot. By updating the reference trajectory window (\tilde{x}_{ref}) at each step and updating the initial condition (x_{IC}), the MPC controller is able to "react" and compensate for the sim to real gap.

You will now implement a function $convex_mpc$ where you setup and solve this optimization problem at every timestep, and simply return u_1 from the solution.

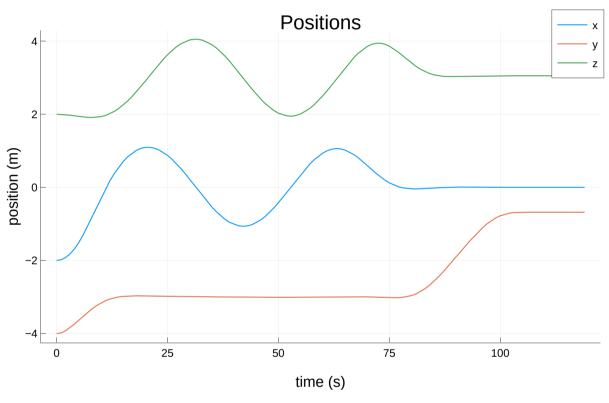
```
In [16]:
          `u = convex_mpc(A,B,X_ref_window,xic,xg,u_min,u_max,N_mpc)`
         setup and solve the above optimization problem, returning the
         first control u_1 from the solution (should be a length nu
         Vector{Float64}).
         function convex_mpc(A::Matrix, # discrete dynamics matrix A
                              B::Matrix, # discrete dynamics matrix B
                             X_ref_window::Vector{Vector{Float64}}, # reference trajectory for this window
                              xic::Vector, # current state x
                              xg::Vector, # goal state
                              u_min::Vector, # lower bound on u
                              u_max::Vector, # upper bound on u
                              N_mpc::Int64, # length of MPC window (horizon)
                              )::Vector{Float64} # return the first control command of the solved policy
             # get our sizes for state and control
             nx,nu = size(B)
             # check sizes
             @assert size(A) == (nx, nx)
             @assert length(xic) == nx
             @assert length(xg) == nx
             @assert length(X_ref_window) == N_mpc
             # LQR cost
             Q = diagm(ones(nx))
             R = diagm(ones(nu))
             # variables we are solving for
             X = cvx.Variable(nx, N mpc)
             U = cvx.Variable(nu,N_mpc-1)
             # TODO: implement cost function
             obi = 0
             XrefWin = mat_from_vec(X_ref_window)
             for k = 1:(N_mpc-1)
                 # add stagewise cost
                 xk = X[:,k]
                 uk = U[:,k]
                 xrefk = XrefWin[:,k]
                 obj += (0.5 * cvx.quadform(xk - xrefk,Q))
```

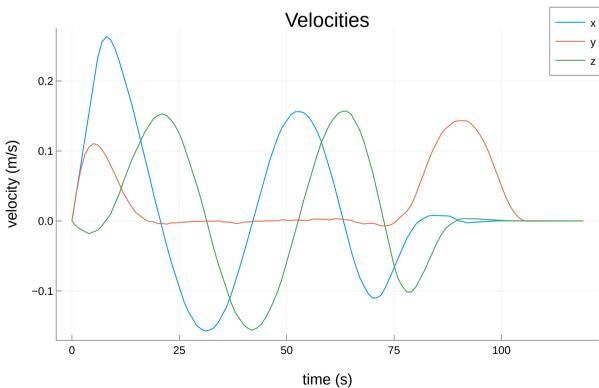
```
obj += (0.5 * cvx.quadform(uk,R))
    end
    obj += (0.5 * cvx.quadform(X[:,N_mpc] - XrefWin[:,N_mpc],Q))
    # create problem with objective
    prob = cvx.minimize(obj)
    # TODO: add constraints with prob.constraints +=
    prob.constraints += (X[:,1] == xic)
    for k = 1:(N_mpc-2)
        # dynamics constraints
        prob.constraints += (X[:,k+1] == A*X[:,k] + B*U[:,k])
        prob.constraints += (U[:,k] <= u_max)</pre>
        prob.constraints += (U[:,k] >= u_min)
        prob.constraints += (X[2,k] \le xg[2])
    end
    prob.constraints += (X[2,N_mpc] \le xg[2])
    prob.constraints += (X[:,N_mpc] == xg)
    # solve problem
    cvx.solve!(prob, ECOS.Optimizer; silent_solver = true)
    # get X and U solutions
   X = X.value
   U = U.value
    # return first control U
    return U[:,1]
end
@testset "convex mpc" begin
    # create our discrete time model
    dt = 1.0
    A,B = create_dynamics(dt)
    # get our sizes for state and control
    nx,nu = size(B)
    # initial and goal states
    x0 = [-2; -4; 2; 0; 0; .0]
    xg = [0, -.68, 3.05, 0, 0, 0]
    # bounds on U
    u_max = 0.4*ones(3)
    u_min = -u_max
    # problem size and reference trajectory
    N = 100
    t_{vec} = 0:dt:((N-1)*dt)
    X_{ref} = [desired_trajectory(x0,xg,N,dt)...,[xg for i = 1:N]...]
    # MPC window size
    N_mpc = 20
    # sim size and setup
    N_sim = N + 20
    t_{\text{vec}} = 0:dt:((N_{\text{sim}}-1)*dt)
    X_{sim} = [zeros(nx) for i = 1:N_{sim}]
    X_{sim}[1] = x0
    U_{sim} = [zeros(nu) for i = 1:N_{sim}-1]
    # simulate
    @showprogress "simulating" for i = 1:N_sim-1
        # get state estimate
        xi_estimate = state_estimate(X_sim[i], xg)
        # TODO: given a window of N mpc timesteps, get current reference trajectory
        X_ref_tilde = X_ref[i:i+N_mpc-1]
        # TODO: call convex mpc controller with state estimate
        u_mpc = convex_mpc(A,B,X_ref_tilde,xi_estimate,xg,u_min,u_max, N_mpc)
        # commanded control goes into thruster model where it gets modified
        U sim[i] = thruster model(X sim[i], xg, u mpc)
        # simulate one step
        X_{sim[i+1]} = A*X_{sim[i]} + B*U_{sim[i]}
    # -----plotting/animation-----
```

Q3

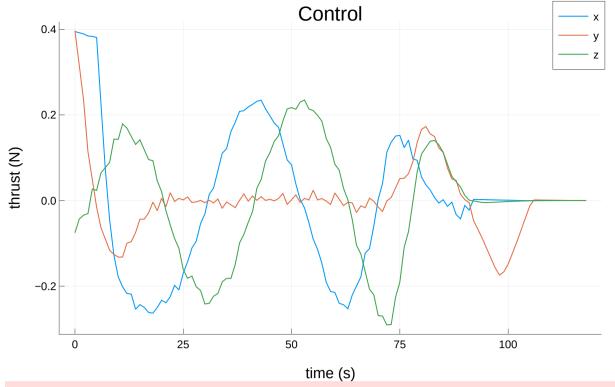
```
Xm = mat_from_vec(X_sim)
   Um = mat_from_vec(U_sim)
   display(plot(t_vec,Xm[1:3,:]',title = "Positions",
                xlabel = "time (s)", ylabel = "position (m)",
                label = ["x" "y" "z"]))
   display(plot(t_vec,Xm[4:6,:]',title = "Velocities",
           xlabel = "time (s)", ylabel = "velocity (m/s)",
                label = ["x" "y" "z"]))
   display(plot(t_vec[1:end-1],Um',title = "Control",
           xlabel = "time (s)", ylabel = "thrust (N)",
                label = ["x" "y" "z"]))
   display(animate_rendezvous(X_sim, X_ref, dt;show_reference = false))
   # -----plotting/animation-----
   [end] - xg < 1e-3 \# goal
   xs=[x[1] for x in X_sim]
   ys=[x[2] for x in X_sim]
   zs=[x[3] for x in X_sim]
    (xg[2] + 1e-3) 
   @test maximum(zs) >= 4 # check to see if you did the circle
   @test minimum(zs) <= 2 # check to see if you did the circle</pre>
   @test maximum(xs) >= 1 # check to see if you did the circle
   @test maximum(norm.(U_sim,Inf)) <= 0.4 + 1e-3 # control constraints satisfied</pre>
end
```

simulating 100%| Time: 0:00:03



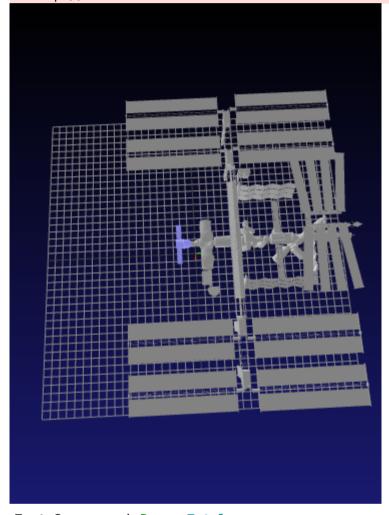


10/03/2023, 22:33 Q3



Info: MeshCat server started. You can open the visualizer by visiting the following URL in your browser: http://127.0.0.1:8707

Open Controls



Test Summary: | Pass Total
convex mpc | 6 6

Out[16]: Test.DefaultTestSet("convex mpc", Any[], 6, false, false)