In [1]:

```
import torch
import torchvision
from torchvision import transforms
import matplotlib.pyplot as plt
import numpy as np
import cupy as np_gpu
import math
from torch.utils.data import DataLoader
import time
import torch.nn as nn
from sklearn.metrics import ConfusionMatrixDisplay

# Random Seeds
np_gpu.random.seed(123456789)
np.random.seed(123456789)

plt.rcParams.update({'font.size': 8})
DRIVE = '/content/drive/MyDrive/Sem7/DL/A1/plots/'
```

0. Common Functions

In [2]:

```
def plot_loss(trainLP, testLP, fileName):
    X_plot = [i * 200 for i in range(len(trainLP))]

    # For using CuPy uncomment these 2 lines
    if(type(trainLP[0]) == np_gpu._core.core.ndarray):
        trainLP, testLP = np_gpu.array(trainLP).get(), np_gpu.array(testLP).get
()

    plt.plot(X_plot, trainLP)
    plt.plot(X_plot, testLP)
    plt.xlabel('No. of batches')
    plt.ylabel('Loss')
    plt.legend(['Train', 'Test'])
    plt.savefig(DRIVE + fileName)

def get_accuracy(pred, truth):
    return np.sum(pred == truth) / pred.shape[0]

def confusion_mat(pred, truth, fileName):
    ConfusionMatrixDisplay.from_predictions(truth, pred)
    plt.savefig(DRIVE + fileName)
```

1. BackProp from scratch

Loading dataset

In [3]:

```
def one_hot(x):
    np_arr = np.zeros(10)
    np_arr[x] = 1
    return np_arr

mnist_train = torchvision.datasets.MNIST(root = ".", train = True, download = Tr
ue); nTrain = len(mnist_train)
mnist_test = torchvision.datasets.MNIST(root = ".", train = False, download = Tr
ue); nTest = len(mnist_test)

X_train = np_gpu.array([np.array(mnist_train[i][0]).reshape(-1) / 255 * 2 - 1 fo
r i in range(nTrain)])
Y_train = np_gpu.array([one_hot(mnist_train[i][1]) for i in range(nTrain)])

X_test = np_gpu.array([np.array(mnist_test[i][0]).reshape(-1) / 255 * 2 - 1 for
i in range(nTest)])
Y_test = np_gpu.array([one_hot(mnist_test[i][1]) for i in range(nTest)])
```

Functions

In [4]:

```
def ReLU(X):
    return np_gpu.maximum(0, X)
def ReLU_derivative(X):
    return (X >= 0) * 1.0

def Tanh(X):
    return np_gpu.tanh(X)
def Tanh_derivative(X):
    return 1 - np_gpu.square(np_gpu.tanh(X))

def sigmoid(X):
    return 1 / (1 + np_gpu.exp(-X))
def sigmoid_derivative(X):
    return sigmoid(X) * (1 - sigmoid(X))

def softmax(X):
    return np_gpu.exp(X) / np_gpu.sum(np_gpu.exp(X), axis = 0)

def applyAct(X):
    if(actFn == 'sigmoid'): return sigmoid(X)
    if(actFn == 'ReLU'): return ReLU(X)
    if(actFn == 'Tanh'): return Tanh(X)

def derivative_act(X):
    if(actFn == 'sigmoid'): return sigmoid_derivative(X)
    if(actFn == 'ReLU'): return ReLU_derivative(X)
    if(actFn == 'Tanh'): return Tanh_derivative(X)

def forward(X):
    A, Z = [X], [X]
    for i in range(1, nl):
        Z.append(W[i-1] @ A[i-1] + B[i-1])
        if i == nl - 1: A.append(softmax(Z[i])) # Last layer softmax
        else: A.append(applyAct(Z[i]))
    return A, Z

def backward(A, Z, Y):
    Delta = [None for i in range(nl)]
    Delta[nl-1] = -(Y - A[nl-1]) * (1/batchSize) # Last layer soft_max
    for l in range(nl-2, 0, -1):
        Delta[l] = (W[l].T @ Delta[l+1]) * derivative_act(Z[l])
    return Delta

def loss(A, Y):
    return -np_gpu.sum(Y * np_gpu.log(A[nl-1])) / A[nl-1].shape[1]

def M(i):
    return math.sqrt(6 / (layers[i] + layers[i+1]))
```

Neural Network Configuration

In [5]:

```
layers = [784, 500, 250, 100, 10] # I/P, h1, h2, h3, O/P
nl = len(layers)
batchSize = 64
epochs = 15
learningRate = 0.01
actFn = 'sigmoid' # 'ReLU' / 'Tanh' / 'sigmoid'
```

Training

In [7]:

```
trainLossProgress, testLossProgress = [], []
W = [(2 * np_gpu.random.random_sample((layers[i+1], layers[i])) - 1) * M(i) for
i in range(nl-1)]
B = [np_gpu.zeros((layers[i+1], 1)) for i in range(nl-1)]

startTime = time.time()
for epoch_id in range(epochs):
    id = 0

    startTimeEpoch = time.time()
    while(id + batchSize <= nTrain):
        X_train_batch, Y_train_batch = X_train[id:id+batchSize, :], Y_train[id:i
d+batchSize, :]
        id += batchSize

        # Initialise gradients to zero
        gradW, gradB = [np_gpu.zeros(W[i].shape) for i in range(nl-1)], [np_gpu.
zeros(B[i].shape) for i in range(nl-1)]

        # Forward and Backward pass
        A, Z = forward(X_train_batch.T)
        Delta = backward(A, Z, Y_train_batch.T)

        # Computer gradients using delts
        for l in range(len(layers) - 1):
            gradW[l] += Delta[l+1] @ A[l].T
            gradB[l] += np_gpu.sum(Delta[l+1], axis = 1).reshape(-1, 1)

        # Update Weights and Biases
        for l in range(len(layers) - 1):
            W[l] -= learningRate * gradW[l]
            B[l] -= learningRate * gradB[l]

        step_id = (id-1) // batchSize
        if(step_id % 200 == 0):
            A_train, _ = forward(X_train.T)
            A_test, _ = forward(X_test.T)
            trainLossProgress.append(loss(A_train, Y_train.T))
            testLossProgress.append(loss(A_test, Y_test.T))
            print(f'Epoch: [{epoch_id + 1} / {epochs}], Step: [{step_id}/{nTrain
//64}], Train Loss: {trainLossProgress[-1]:.2f}, Test Loss: {testLossProgress[-1
]:.2f}')

    print(f'Epoch {epoch_id + 1} took {format(time.time() - startTimeEpoch, ".2
f")} seconds\n')

print('TRAINING DONE', format(time.time() - startTime, ".2f")+" seconds")
```

```
Epoch: [1 / 15], Step: [0/937], Train Loss: 2.37, Test Loss: 2.37
Epoch: [1 / 15], Step: [200/937], Train Loss: 2.30, Test Loss: 2.30
Epoch: [1 / 15], Step: [400/937], Train Loss: 2.29, Test Loss: 2.29
Epoch: [1 / 15], Step: [600/937], Train Loss: 2.28, Test Loss: 2.28
Epoch: [1 / 15], Step: [800/937], Train Loss: 2.28, Test Loss: 2.28
Epoch 1 took 4.62 seconds

Epoch: [2 / 15], Step: [0/937], Train Loss: 2.27, Test Loss: 2.27
Epoch: [2 / 15], Step: [200/937], Train Loss: 2.26, Test Loss: 2.26
Epoch: [2 / 15], Step: [400/937], Train Loss: 2.25, Test Loss: 2.25
Epoch: [2 / 15], Step: [600/937], Train Loss: 2.24, Test Loss: 2.24
Epoch: [2 / 15], Step: [800/937], Train Loss: 2.23, Test Loss: 2.23
Epoch 2 took 4.46 seconds

Epoch: [3 / 15], Step: [0/937], Train Loss: 2.22, Test Loss: 2.22
Epoch: [3 / 15], Step: [200/937], Train Loss: 2.20, Test Loss: 2.20
Epoch: [3 / 15], Step: [400/937], Train Loss: 2.18, Test Loss: 2.18
Epoch: [3 / 15], Step: [600/937], Train Loss: 2.15, Test Loss: 2.15
Epoch: [3 / 15], Step: [800/937], Train Loss: 2.12, Test Loss: 2.12
Epoch 3 took 4.46 seconds

Epoch: [4 / 15], Step: [0/937], Train Loss: 2.10, Test Loss: 2.09
Epoch: [4 / 15], Step: [200/937], Train Loss: 2.05, Test Loss: 2.04
Epoch: [4 / 15], Step: [400/937], Train Loss: 1.99, Test Loss: 1.98
Epoch: [4 / 15], Step: [600/937], Train Loss: 1.92, Test Loss: 1.91
Epoch: [4 / 15], Step: [800/937], Train Loss: 1.84, Test Loss: 1.83
Epoch 4 took 4.51 seconds

Epoch: [5 / 15], Step: [0/937], Train Loss: 1.77, Test Loss: 1.76
Epoch: [5 / 15], Step: [200/937], Train Loss: 1.68, Test Loss: 1.67
Epoch: [5 / 15], Step: [400/937], Train Loss: 1.58, Test Loss: 1.57
Epoch: [5 / 15], Step: [600/937], Train Loss: 1.49, Test Loss: 1.48
Epoch: [5 / 15], Step: [800/937], Train Loss: 1.40, Test Loss: 1.39
Epoch 5 took 4.46 seconds

Epoch: [6 / 15], Step: [0/937], Train Loss: 1.34, Test Loss: 1.33
Epoch: [6 / 15], Step: [200/937], Train Loss: 1.26, Test Loss: 1.25
Epoch: [6 / 15], Step: [400/937], Train Loss: 1.20, Test Loss: 1.18
Epoch: [6 / 15], Step: [600/937], Train Loss: 1.13, Test Loss: 1.12
Epoch: [6 / 15], Step: [800/937], Train Loss: 1.08, Test Loss: 1.07
Epoch 6 took 4.53 seconds

Epoch: [7 / 15], Step: [0/937], Train Loss: 1.04, Test Loss: 1.03
Epoch: [7 / 15], Step: [200/937], Train Loss: 0.99, Test Loss: 0.98
Epoch: [7 / 15], Step: [400/937], Train Loss: 0.95, Test Loss: 0.94
Epoch: [7 / 15], Step: [600/937], Train Loss: 0.91, Test Loss: 0.90
Epoch: [7 / 15], Step: [800/937], Train Loss: 0.88, Test Loss: 0.87
Epoch 7 took 4.46 seconds

Epoch: [8 / 15], Step: [0/937], Train Loss: 0.85, Test Loss: 0.84
Epoch: [8 / 15], Step: [200/937], Train Loss: 0.82, Test Loss: 0.81
Epoch: [8 / 15], Step: [400/937], Train Loss: 0.79, Test Loss: 0.78
Epoch: [8 / 15], Step: [600/937], Train Loss: 0.76, Test Loss: 0.75
Epoch: [8 / 15], Step: [800/937], Train Loss: 0.74, Test Loss: 0.73
Epoch 8 took 4.53 seconds

Epoch: [9 / 15], Step: [0/937], Train Loss: 0.72, Test Loss: 0.71
Epoch: [9 / 15], Step: [200/937], Train Loss: 0.70, Test Loss: 0.69
Epoch: [9 / 15], Step: [400/937], Train Loss: 0.68, Test Loss: 0.67
Epoch: [9 / 15], Step: [600/937], Train Loss: 0.66, Test Loss: 0.65
Epoch: [9 / 15], Step: [800/937], Train Loss: 0.64, Test Loss: 0.63
```

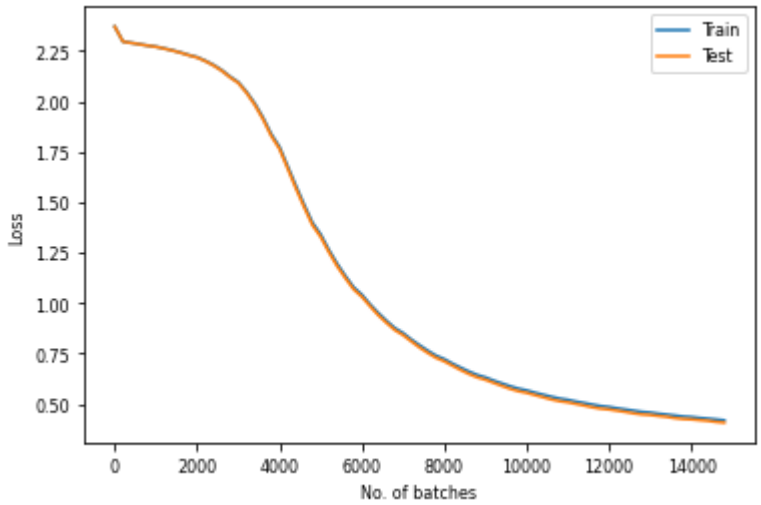
```
Epoch 9 took 4.50 seconds

Epoch: [10 / 15], Step: [0/937], Train Loss: 0.63, Test Loss: 0.62
Epoch: [10 / 15], Step: [200/937], Train Loss: 0.62, Test Loss: 0.60
Epoch: [10 / 15], Step: [400/937], Train Loss: 0.60, Test Loss: 0.59
Epoch: [10 / 15], Step: [600/937], Train Loss: 0.59, Test Loss: 0.57
Epoch: [10 / 15], Step: [800/937], Train Loss: 0.58, Test Loss: 0.56
Epoch 10 took 4.51 seconds

Epoch: [11 / 15], Step: [0/937], Train Loss: 0.57, Test Loss: 0.56
Epoch: [11 / 15], Step: [200/937], Train Loss: 0.56, Test Loss: 0.54
Epoch: [11 / 15], Step: [400/937], Train Loss: 0.55, Test Loss: 0.53
Epoch: [11 / 15], Step: [600/937], Train Loss: 0.54, Test Loss: 0.52
Epoch: [11 / 15], Step: [800/937], Train Loss: 0.53, Test Loss: 0.51
Epoch 11 took 4.51 seconds

Epoch: [12 / 15], Step: [0/937], Train Loss: 0.52, Test Loss: 0.51
Epoch: [12 / 15], Step: [200/937], Train Loss: 0.51, Test Loss: 0.50
Epoch: [12 / 15], Step: [400/937], Train Loss: 0.50, Test Loss: 0.49
Epoch: [12 / 15], Step: [600/937], Train Loss: 0.50, Test Loss: 0.48
Epoch: [12 / 15], Step: [800/937], Train Loss: 0.49, Test Loss: 0.48
Epoch 12 took 4.49 seconds

Epoch: [13 / 15], Step: [0/937], Train Loss: 0.48, Test Loss: 0.47
Epoch: [13 / 15], Step: [200/937], Train Loss: 0.48, Test Loss: 0.47
Epoch: [13 / 15], Step: [400/937], Train Loss: 0.47, Test Loss: 0.46
Epoch: [13 / 15], Step: [600/937], Train Loss: 0.47, Test Loss: 0.45
Epoch: [13 / 15], Step: [800/937], Train Loss: 0.46, Test Loss: 0.45
Epoch 13 took 4.54 seconds

Epoch: [14 / 15], Step: [0/937], Train Loss: 0.46, Test Loss: 0.45
Epoch: [14 / 15], Step: [200/937], Train Loss: 0.45, Test Loss: 0.44
Epoch: [14 / 15], Step: [400/937], Train Loss: 0.45, Test Loss: 0.44
Epoch: [14 / 15], Step: [600/937], Train Loss: 0.44, Test Loss: 0.43
Epoch: [14 / 15], Step: [800/937], Train Loss: 0.44, Test Loss: 0.43
Epoch 14 took 4.48 seconds

Epoch: [15 / 15], Step: [0/937], Train Loss: 0.43, Test Loss: 0.42
Epoch: [15 / 15], Step: [200/937], Train Loss: 0.43, Test Loss: 0.42
Epoch: [15 / 15], Step: [400/937], Train Loss: 0.43, Test Loss: 0.42
Epoch: [15 / 15], Step: [600/937], Train Loss: 0.42, Test Loss: 0.41
Epoch: [15 / 15], Step: [800/937], Train Loss: 0.42, Test Loss: 0.41
Epoch 15 took 4.52 seconds

TRAINING DONE 67.59 seconds
```

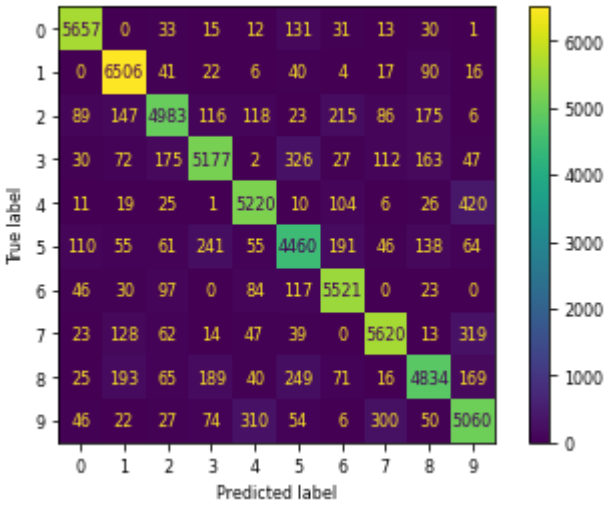
Testing

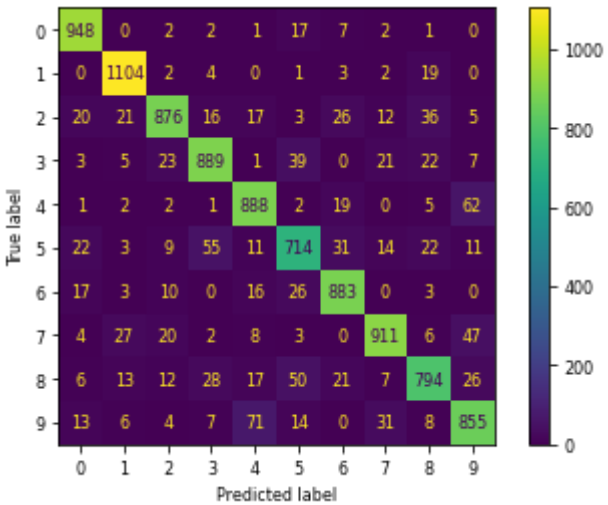
In [8]:

```
A, _ = forward(X_test.T)
pred_test, truth_test = np_gpu.argmax(A[nl-1], axis = 0).reshape(-1), np_gpu.arg
max(Y_test.T, axis = 0).reshape(-1)

A, _ = forward(X_train.T)
pred_train, truth_train = np_gpu.argmax(A[nl-1], axis = 0).reshape(-1), np_gpu.a
rgmax(Y_train.T, axis = 0).reshape(-1)

print('Test Accuracy:', get_accuracy(pred_test.get(), truth_test.get()) * 100)
print('Train Accuracy:', get_accuracy(pred_train.get(), truth_train.get()) * 100
)

prefix = 'scratch_' + actFn

plot_loss(trainLossProgress, testLossProgress, prefix + '_loss.svg')

confusion_mat(pred_train.get(), truth_train.get(), prefix + '_cmat_train.svg')
confusion_mat(pred_test.get(), truth_test.get(), prefix + '_cmat_test.svg')
```

```
Test Accuracy: 88.62
Train Accuracy: 88.39666666666666
```







2. Using PyTorch

In [9]:

```
device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
```

Data Loading

In [10]:

```
mnist_train = torchvision.datasets.MNIST(root = ".", train = True, download = Tr
ue, transform=transforms.ToTensor()); nTrain = len(mnist_train)
mnist_test = torchvision.datasets.MNIST(root = ".", train = False, download = Tr
ue, transform=transforms.ToTensor()); nTest = len(mnist_test)

train_loader = DataLoader(mnist_train, batch_size=batchSize, shuffle=False)
test_loader = DataLoader(mnist_test, batch_size=batchSize, shuffle=False)

train_loader_1 = DataLoader(mnist_train, batch_size=len(mnist_train), shuffle=Fa
lse)
X_train, Y_train = next(iter(train_loader_1))
X_train = X_train.reshape(-1, 784).to(device)
Y_train = Y_train.to(device)

test_loader_1 = DataLoader(mnist_test, batch_size=len(mnist_test), shuffle=False
)
X_test, Y_test = next(iter(test_loader_1))
X_test = X_test.reshape(-1, 784).to(device)
Y_test = Y_test.to(device)
```

Model Configuration

In [11]:

```
layers = [784, 500, 250, 100, 10] # I/P, h1, h2, h3, O/P
nl = len(layers)
batchSize = 64
epochs = 5
learningRate = 0.001
actFn = 'ReLU' # 'ReLU' / 'Tanh' / 'sigmoid'
weightDecay = 1e-4 # For L2 Regularisation, 0 if you don't want L2 regularisatio
n
```

In [12]:

```
modelList = []
for i in range(nl-1):
    modelList.append(nn.Linear(layers[i], layers[i+1]))
    if(i == nl-2):
        modelList.append(nn.Softmax(1))
    else:
        if actFn == 'ReLU': modelList.append(nn.ReLU())
        if actFn == 'sigmoid': modelList.append(nn.Sigmoid())
        if actFn == 'Tanh': modelList.append(nn.Tanh())
```

In [13]:

```
model = nn.Sequential(*modelList).to(device)
lossFunction = nn.CrossEntropyLoss()
optimizer = torch.optim.Adam(model.parameters(), lr=learningRate, weight_decay=w
eightDecay)
```

Training

In [14]:

```
trainLossProgress = []
testLossProgress = []

startTime = time.time()
for epoch_id in range(epochs):
    startTimeEpoch = time.time()
    for step_id, (X_train_batch, Y_train_batch) in enumerate(train_loader):
        X_train_batch = X_train_batch.reshape(-1,784).to(device)
        Y_pred_batch = model(X_train_batch)
        loss = lossFunction(Y_pred_batch, Y_train_batch.to(device))
        optimizer.zero_grad()
        loss.backward()
        optimizer.step()

        if(step_id % 200 == 0):
            with torch.no_grad():
                trainLossProgress.append(lossFunction(model(X_train), Y_train).i
tem())
                testLossProgress.append(lossFunction(model(X_test), Y_test).item
())
                print(f'Epoch: [{epoch_id + 1} / {epochs}], Step: [{step_id}/{nT
rain//64}], Train Loss: {trainLossProgress[-1]:.2f}, Test Loss: {testLossProgres
s[-1]:.2f}')
    print(f'Epoch {epoch_id + 1} took {format(time.time() - startTimeEpoch, ".2
f")} seconds\n')

print('TRAINING DONE', format(time.time() - startTime, ".2f")+" seconds")
```

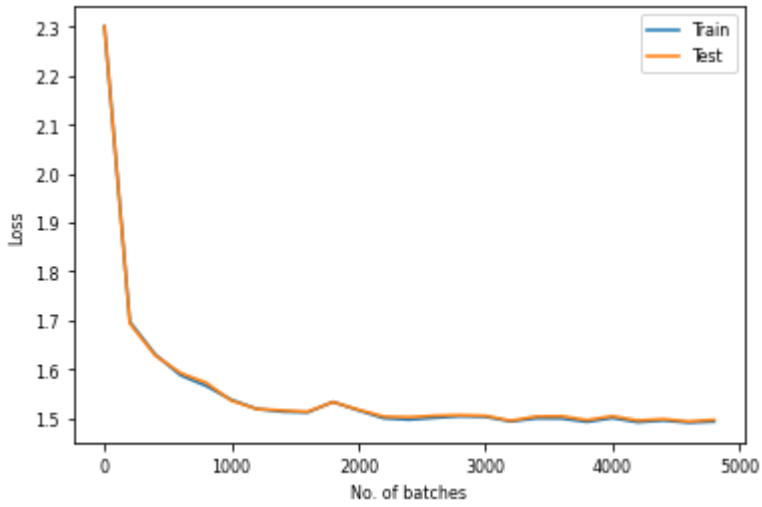
```
Epoch: [1 / 5], Step: [0/937], Train Loss: 2.30, Test Loss: 2.30
Epoch: [1 / 5], Step: [200/937], Train Loss: 1.70, Test Loss: 1.69
Epoch: [1 / 5], Step: [400/937], Train Loss: 1.63, Test Loss: 1.63
Epoch: [1 / 5], Step: [600/937], Train Loss: 1.59, Test Loss: 1.59
Epoch: [1 / 5], Step: [800/937], Train Loss: 1.57, Test Loss: 1.57
Epoch 1 took 6.77 seconds

Epoch: [2 / 5], Step: [0/937], Train Loss: 1.54, Test Loss: 1.54
Epoch: [2 / 5], Step: [200/937], Train Loss: 1.52, Test Loss: 1.52
Epoch: [2 / 5], Step: [400/937], Train Loss: 1.51, Test Loss: 1.52
Epoch: [2 / 5], Step: [600/937], Train Loss: 1.51, Test Loss: 1.51
Epoch: [2 / 5], Step: [800/937], Train Loss: 1.53, Test Loss: 1.53
Epoch 2 took 6.74 seconds

Epoch: [3 / 5], Step: [0/937], Train Loss: 1.52, Test Loss: 1.52
Epoch: [3 / 5], Step: [200/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [3 / 5], Step: [400/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [3 / 5], Step: [600/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [3 / 5], Step: [800/937], Train Loss: 1.50, Test Loss: 1.51
Epoch 3 took 6.73 seconds

Epoch: [4 / 5], Step: [0/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [4 / 5], Step: [200/937], Train Loss: 1.49, Test Loss: 1.49
Epoch: [4 / 5], Step: [400/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [4 / 5], Step: [600/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [4 / 5], Step: [800/937], Train Loss: 1.49, Test Loss: 1.50
Epoch 4 took 6.75 seconds

Epoch: [5 / 5], Step: [0/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [5 / 5], Step: [200/937], Train Loss: 1.49, Test Loss: 1.50
Epoch: [5 / 5], Step: [400/937], Train Loss: 1.50, Test Loss: 1.50
Epoch: [5 / 5], Step: [600/937], Train Loss: 1.49, Test Loss: 1.49
Epoch: [5 / 5], Step: [800/937], Train Loss: 1.49, Test Loss: 1.50
Epoch 5 took 6.86 seconds

TRAINING DONE 33.85 seconds
```

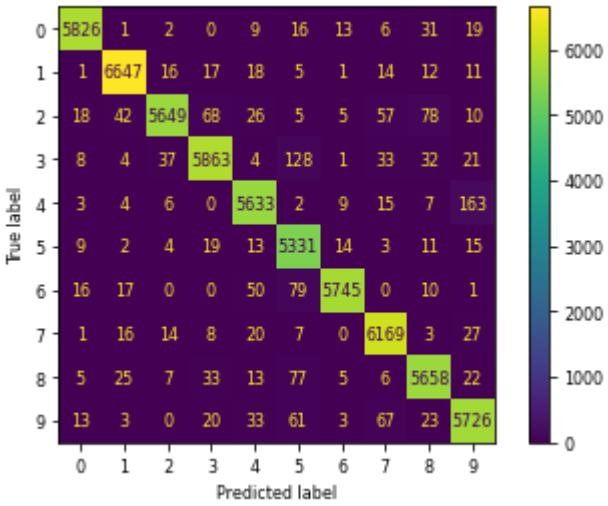
Testing

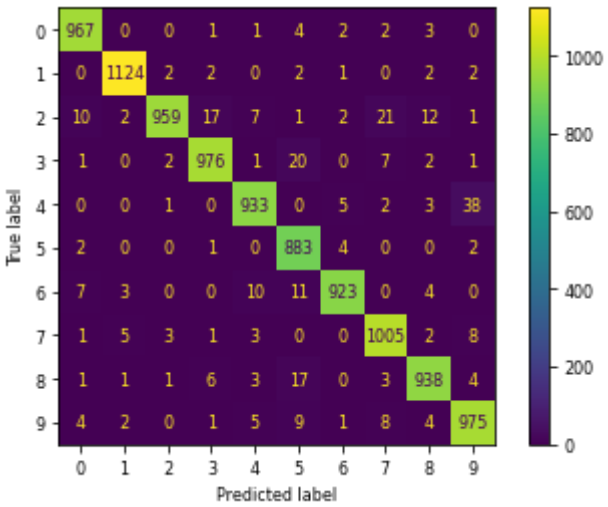
In [15]:

```
with torch.no_grad():
    _, pred_test = torch.max(model(X_test), 1)
    pred_test = pred_test.to(torch.device('cpu')).numpy()
    _, pred_train = torch.max(model(X_train), 1)
    pred_train = pred_train.to(torch.device('cpu')).numpy()

    truth_test = Y_test.to(torch.device('cpu')).numpy()
    truth_train = Y_train.to(torch.device('cpu')).numpy()

    print('Test Accuracy:', get_accuracy(pred_test, truth_test) * 100)
    print('Train Accuracy:', get_accuracy(pred_train, truth_train) * 100)

    prefix = 'pytorch_' + actFn + str(learningRate) + '_' + str(epochs) + '_' +
str(weightDecay)

    plot_loss(trainLossProgress, testLossProgress, prefix + '_loss.svg')

    confusion_mat(pred_train, truth_train, prefix + '_cmat_train.svg')
    confusion_mat(pred_test, truth_test, prefix + '_cmat_test.svg')
```

```
Test Accuracy: 96.83
Train Accuracy: 97.07833333333333
```







References

1. https://analyticsindiamag.com/guide-to-feed-forward-network-using-pytorch-with-mnist-dataset/ (https://analyticsindiamag.com/guide-to-feed-forward-network-using-pytorch-with-mnist-dataset/)
2. https://blog.paperspace.com/dataloaders-abstractions-pytorch/ (https://blog.paperspace.com/dataloaders-abstractions-pytorch/)
3. https://towardsdatascience.com/build-a-simple-neural-network-using-pytorch-38c55158028d (https://towardsdatascience.com/build-a-simple-neural-network-using-pytorch-38c55158028d)