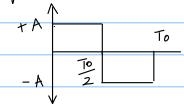
Assignment 3

Out: 07/08/2018, Due: 14/08/2018

## Review of Fourier Legies

- (1) (given two peniodic signals x(t) and y(t) each with peniod To. What is the vector acpresentation of x(t) and y(t), when the basis vectors for the vector space use the complex exponentials & e+j211 kfot, KEZY. What is the distance between the signals a(t) and y(t)?
- Find out the Fourica scaies / spectaum / vector nepresentation of the following signals a) 100 cos (211 fot)
  - b) The periodic square wave, with one period given by



- 3 2 cos (2π fot) + 3 sin (2π fot) (discuss for different cases fo = for, fo = a multiple of fi, to \ any multiple of fi and vice vesse, H(F(fi, fo))
- 3) A signal, that is not realistic/practically realisable, but of immense use in mathematical analysis is the impalse train, defined as

 $\lambda_m(t) = Z_t \lambda_k . S(t - k T_0).$ 

- draw an enample of an impulse train (ie, choose to and in as you wish)
- find out the Fougica scarces appresentation of the impulse train in (t).

(look at Example 2.4.2 from the textbook)

- Properties of Fourier scries derive the properties listed below
  - a) linearity
  - b) time delay
  - c) Fougica segies of a real valued signal is conjugate symmetrice d) Harmonic structure.
  - d) Harmonic structure
  - e) Dlffuentiation
  - f) Parscral's identity
  - ( see the section 2.4.1 in the teathook for the definition of all these properties)

Suppose 
$$u(t)$$
 and  $v(t)$  are periodic signals with fundamental frequencies fund for aespectively: ( $\int u \neq f_V$ ), and the following Fourier series exist.

$$u(t) = \sum_{k=-\infty}^{\infty} u_k \in J^{2\pi} k f u t \text{ and } v(t) = \sum_{k=-\infty}^{\infty} v_k e^{-\frac{1}{2\pi}k} f_V t.$$

what can you say about the Fourier scries of u(t) + v(t)? can this be empressed in terms of un and vx?

6 If u(t) and v(t) are two periodic signals with the same fundamental period fo and the following Fourier segies exist:

$$u(\epsilon) = \sum_{k} u_{k} e^{\int 2\pi k \int_{0}^{\infty} t} \text{ and } v(\epsilon) = \sum_{k} v_{k} e^{\int 2\pi k \int_{0}^{\infty} t}$$

- a) is the product u(t) v(E) periodic? what is the period?
- b) suppose alt) and u(E) have finite power What about the product u(t) v(E)?
- c) (anyou empress the Fourier series of the product alf) V(t) in trans of the trans and un:
- d) suppose now that u(t) and v(t) have different fundamental frequencies by and for Acspectively with the Fourier scries being  $u(t) = \sum_{k} u_k e^{\int 2\pi k \int_{0}^{\infty} t}$  and  $v(t) = \sum_{k} v_k e^{\int 2\pi k \int_{0}^{\infty} t}$

Do you think you can get a fourier begies sepresentation for the product ult) v(t) and that bo in terms of un and vx. Elaborate ...