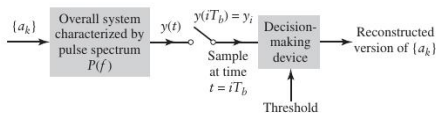




AVD623: Communication Systems-II  
Vineeth B. S.  
Dept. of Avionics  
**Lecture 3**

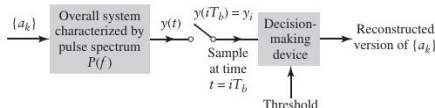
Figures are taken from “Communication Systems” by Simon Haykin

## An effective pulse shape $p(t)$



►  $y(t) = \sum_{k=-\infty}^{\infty} a_k p(t - kT_b)$ , where  $p(t) = g(t) \star h(t) \star q(t)$

# Intersymbol interference problem



- ▶ At the sampling instants  $y(iT_b)$  we have  $y(iT_b) = \sum_{k=-\infty}^{\infty} a_k p((i - k)T_b)$  (notation: pulse is centered at zero)
- ▶ Suppose  $y_i = y(iT_b)$  and  $p_i = p(iT_b)$
- ▶  $y_i = \sum_{k=-\infty}^{\infty} a_k p_{i-k}$
- ▶ We need  $y_i = p_0 a_i$  for all  $i$ . Let us say that  $p_0 = \sqrt{E}$
- ▶ What we have is  $y_i = \sqrt{E} a_i + \sum_{k \neq i} a_k p_{i-k}$



- ▶ We have to design  $p(t)$  such that  $y_i = \sqrt{E}a_i$
- ▶  $p(t)$  has to be designed so that  $P(f)$  has minimum bandwidth
- ▶ Designing  $p(t)$  is called pulse shaping

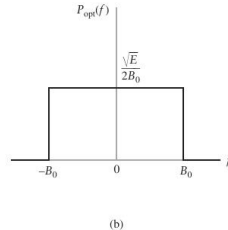
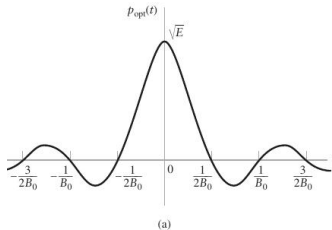


## Nyquist channel

- ▶ If  $y_i = p_0 a_i$  for every  $i$  then we require that

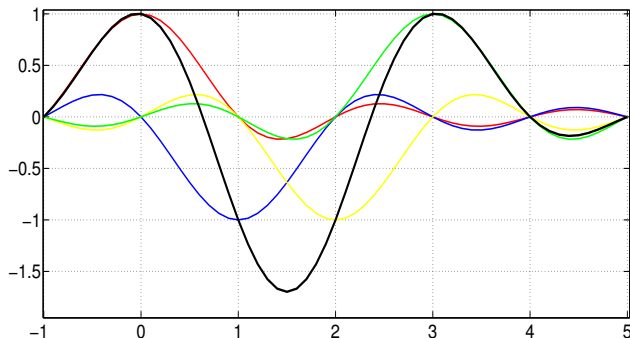
$$p_n = \begin{cases} \sqrt{E}, & \text{for } n = 0, \\ 0, & \text{otherwise.} \end{cases}$$

- ▶ Note that  $p_n = p(nT_b)$
- ▶ Is it possible to get  $P(f)$ ? Assuming that  $P(f)$  is bandlimited
- ▶ Consider the choice of  $p(t) = \text{sinc}\left(\frac{t}{T_b}\right)$
- ▶ With  $B_0 = \frac{1}{2T_b}$  we have the following optimal pulse shape  $p_{\text{opt}}(t)$



- ▶ The PAM system with  $P_{\text{opt}}(f)$  is called the **Nyquist channel**
- ▶ The bandwidth  $B_0$  is called the **Nyquist bandwidth**

- ▶ The transfer function  $P(f)$  is not realizable
- ▶ Issue of timing jitter

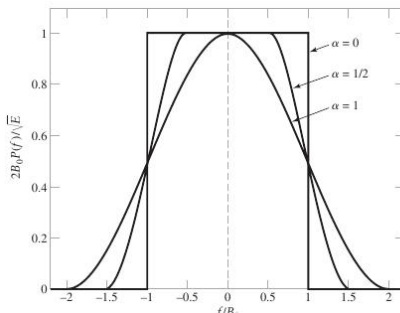


- ▶ Suppose sampling instants at which decoding is done has a *jitter*. Then is correct decoding possible?

- The F.T of  $p(t)$  is

$$P(f) = \begin{cases} \frac{\sqrt{E}}{2B_0}, & \text{for } |f| \leq f_1, \\ \frac{\sqrt{E}}{4B_0} \left[ 1 + \cos \left\{ \frac{\pi(|f| - f_1)}{2(B_0 - f_1)} \right\} \right], & \text{for } f_1 < |f| < 2B_0 - f_1, \\ 0, & \text{o/w.} \end{cases}$$

- $\alpha = 1 - \frac{f_1}{B_0}$ .  $\alpha$  is the roll-off factor.
- Bandwidth of the pulse is  $2B_0 - f_1$  or  $B_0(1 + \alpha)$





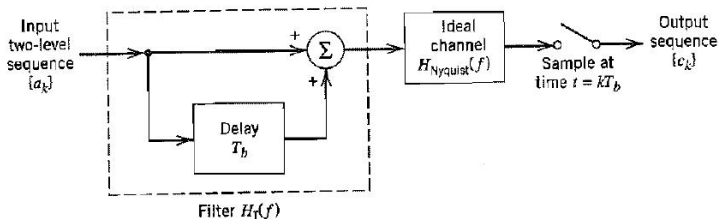
► Let  $r_b = \frac{1}{T_b}$

Scheme	Bandwidth	Power	Rate	Timing Jitter
Rectangular	$r_b$	95%	$r_b$	Robust
Sinc	$\frac{r_b}{2}$	100%	$r_b$	Weak
Raised cosine	$\frac{r_b}{2}(1 + \alpha)$	100%	$r_b$	less than Rect

► Read about square root raised cosine pulse shaping



- ▶ Let the input bit sequence  $b_k$  be converted to a baseband PAM signal  $a_k \in \{-1, 1\}$
- ▶ Let us think of the sequence  $a_k$  as being put into the following system

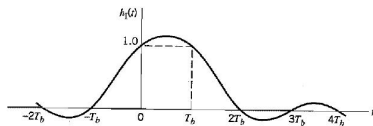
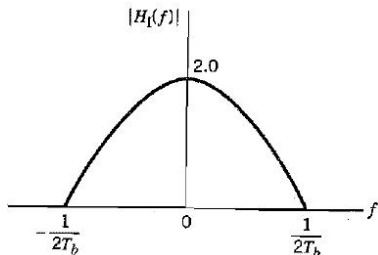


- ▶ What is the effective response of the system with  $a_k$  as input and  $c_k$  as output?

## Duobinary response



- ▶ The effective response is  $H_{nyquist}(f)(1 + e^{-j2\pi fT_b})$
- ▶ Or  $2H_{nyquist}(f)\cos(\pi fT_b)e^{-j\pi fT_b}$
- ▶ Note that  $H_{nyquist}(f) = 1$  for  $|f| \leq \frac{1}{2T_b}$  and 0 otherwise





- ▶  $c_k = a_k + a_{k-1}$
- ▶ If  $\hat{a}_{k-1}$  is the estimate of  $a_{k-1}$ , then  $a_k = c_k - \hat{a}_{k-1}$
- ▶ Prone to error propagation
- ▶ Read about the pre-coding method to avoid error propagation from "Communication Systems"
- ▶ There are other forms of combining  $a_k$  in order to obtain other responses
- ▶ Read about the partial response signalling from "Communication Systems"



- ▶ Recall the digital transmission system block diagram
- ▶ A transmit filter  $G(f)$ , a channel  $H(f)$ , and a receive filter  $Q(f)$
- ▶ Let us assume that transmit filtering is not done
- ▶ We have  $P(f) = H(f)Q(f)$
- ▶ We will consider a special form for  $Q(f)$  - a linear transversal filter
- ▶ The impulse response of  $Q(f)$  is  $q(t) = \sum_{k=-N}^N w_k \delta(t - kT_b)$
- ▶ Then  $p(t) = h(t) \star q(t)$



- ▶  $p(t) = h(t) \star q(t)$
- ▶ Or  $p(t) = \sum_{k=-N}^N w_k h(t - kT_b)$
- ▶ At the sampling instants  $p_n = p(nT_b) = \sum_{k=-N}^N w_k h((n - k)T_b)$
- ▶ Let  $h_n = h(nT_b)$
- ▶ Our requirement is

$$p_n = \begin{cases} \sqrt{E}, & \text{for } n = 0, \\ 0, & \text{otherwise.} \end{cases}$$

- ▶ Can we adjust  $w_k$  to satisfy these requirements?



- Our requirement is

$$p_n = \begin{cases} \sqrt{E}, & \text{for } n = 0, \\ 0, & \text{otherwise.} \end{cases}$$

- We can adjust  $w_k$  so that

$$p_n = \sum_{k=-N}^N w_k h_{n-k} = \begin{cases} \sqrt{E}, & \text{for } n = 0, \\ 0, & \text{for } n = \pm 1, \pm 2, \dots, \pm N. \end{cases}$$

- The receiver determines  $h_{n-k}$  via pilot sequence assisted training