

**Indian Institute of Space Science and Technology**  
**AVD623 - Assignment 4**  
**Department of Avionics**

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1. Read “Synchronization” from Chapter 6 of Simon Haykin and do the following problems
  - (a) Problems 6.47, 6.48, 6.49, and 6.50
2. Suppose  $x(t)$  is a real valued signal for which the Fourier transform  $X(f)$  exists. Then prove that  $X(f) = X^*(-f)$ , where  $X^*(f)$  is the complex conjugate of  $X(f)$ .
3. Read about the Hilbert transform and show the following
  - (a) Suppose  $\mathcal{H}(x(t))$  is the Hilbert transform of  $x(t)$ , then show that  $\mathcal{H}(\mathcal{H}(x(t)))$  is  $-x(t)$  (1 mark).
  - (b) Suppose  $x(t)$  is a real valued signal. Show that  $x(t)$  and its Hilbert transform  $\mathcal{H}(x(t))$  are orthogonal (2 marks). Two signals  $x(t)$  and  $y(t)$  are orthogonal if  $\int_{-\infty}^{\infty} x(t)y(t)dt = 0$ .
4. Reading assignment: Complex baseband representation from Appendix 2 of Simon Haykin