

## AV312 - Lecture 14

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Figures from “Communication Systems” by Haykin and “An Intro. to Analog and Digital Commn.” by Haykin and Moher

6th September 2016

## Review of last classes

- ▶ Delta modulation
- ▶ Read Delta-Sigma modulation and Differential PCM from the textbook

# Today's class

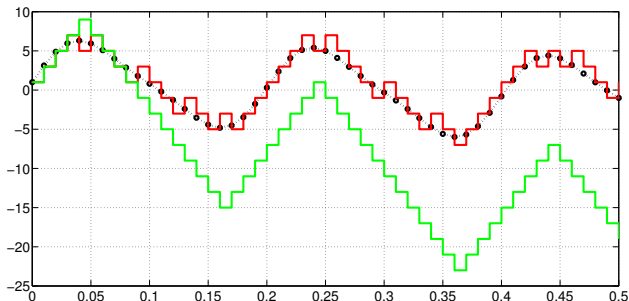
- ▶ Discussion about delta modulation
- ▶ Digital transmission
  - ▶ An example is PCM transmission
  - ▶ How to do digital transmission over baseband and passband channels?
- ▶ Today's scribes are Nikunj Gupta and Nitish Kumar for the first hour
- ▶ Today's scribes are Niwhashini and Palle Ananya for the second hour

## Discussion about Delta modulation - a counter example

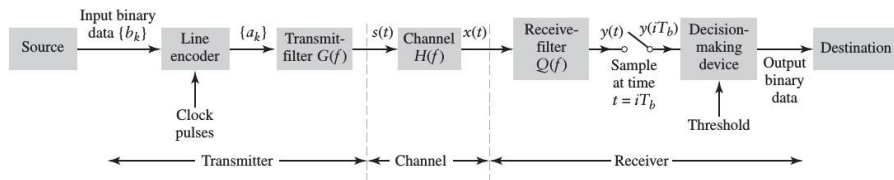
- ▶ We had interpreted delta modulation as a signalling scheme that signals “changes” in a signal from the  $n^{\text{th}}$  sampling instant to the  $(n + 1)^{\text{th}}$ .
- ▶ Why not signal the quantized form of the difference  $m(nT_s + T_s) - m(nT_s)$  instead of  $m(nT_s + T_s) - m_q(nT_s)$ ? The intuition is that a staircase waveform is what is available at the receiver.

# Discussion about Delta modulation - a counter example

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# Digital transmission

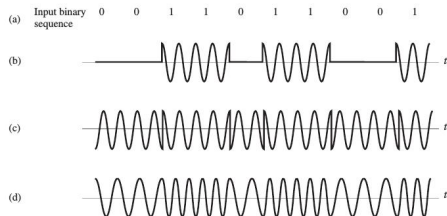


- ▶ Source of digital information - characterized by bit duration  $T_b$  (or bit rate)
- ▶ Converted into a line code whose levels are represented by  $a_k$  (say  $-A$  and  $+A$ )
- ▶ Further transformation of  $a_k$  to “match” the signal to the channel (what if the channel were bandpass?)
- ▶ We obtain a continuous time signal  $s(t)$  which is transmitted over the channel
- ▶ At the receiver need to convert it into a digital signal - so synchronized sampling, usually at rate  $T_b$
- ▶ A decision device decides whether 0 or 1 was transmitted
- ▶ M-ary transmission - transmit groups of bits using multiple levels in  $a_k$ .

# Transmission over Passband channels

- ▶ A sinusoidal carrier signal  
 $c(t) = A_c \cos(2\pi f_c t + \phi_c)$
- ▶ Binary amplitude shift keying (BASK)
- ▶ Binary phase shift keying (BPSK)
- ▶ Binary frequency shift keying (BFSK)
- ▶ A convenient normalization for unit carrier energy for a bit duration;

$$A_c = \sqrt{\frac{2}{T_b}}$$



# Binary amplitude shift keying

- ▶ For  $kT_b \leq t \leq (k+1)T_b$

$$b(t) = \begin{cases} \sqrt{E_b}, & \text{for } b_k = 1 \\ 0, & \text{for } b_k = 0. \end{cases}$$

- ▶  $s(t) = b(t)c(t)$

$$s(t) = \begin{cases} \sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_c t), & \text{for } b_k = 1 \\ 0, & \text{for } b_k = 0. \end{cases}$$

- ▶ Average transmitted energy  $\frac{E_b}{2}$
- ▶ Generation of BASK signal - can a multiplier be used?
- ▶ Detection of a BASK signal - what property does the envelope have?



## Binary phase shift keying

- ▶ For  $kT_b \leq t \leq (k+1)T_b$

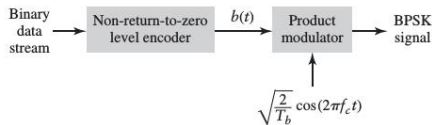
$$b(t) = \begin{cases} \sqrt{E_b}, & \text{for } b_k = 1 \\ -\sqrt{E_b}, & \text{for } b_k = 0. \end{cases}$$

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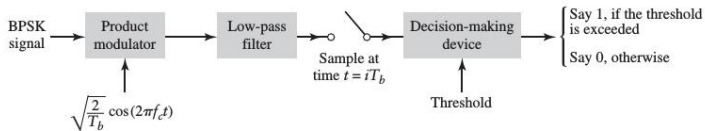
$$s(t) = \begin{cases} \sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_c t), & \text{for } b_k = 1 \\ -\sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_c t), & \text{for } b_k = 0. \end{cases}$$

- ▶ Average transmitted energy  $E_b$
- ▶ Generation of BPSK signal - can a multiplier be used?
- ▶ Detection of a BPSK signal - does the envelope detector work here?

# Generation and coherent detection of BPSK-ed $s(t)$



(a)



(b)

- ▶ The receiver is coherent; the local carrier has to be synchronous in phase as well as frequency to the transmitted (actually received) carrier.
- ▶ Note that the transmitter and receiver architecture is similar to that for DSBSC.
- ▶ Need to be careful about the cutoff frequency of the low pass filter.

## Binary frequency shift keying

- ▶ For  $kT_b \leq t < (k+1)T_b$

$$s(t) = \begin{cases} \sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_1 t), & \text{for } b_k = 1 \\ \sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_2 t), & \text{for } b_k = 0. \end{cases}$$

- ▶ BFSK could have continuous phase or discontinuous phase
- ▶ For continuous phase  $f_1(kT_b + T_b) = f_2(kT_b) + 2m\pi$

# Power spectrum of BPSK

- ▶ We are not really interested in analysing a deterministic sequence of bits, but rather a random sequence.
- ▶ We will revisit this analysis in the second pass.
- ▶ Note that we are interested in the power spectrum, more precisely it is a **normalized power spectrum**.
- ▶ The BPSK-ed  $s(t) = b(t)c(t)$ , where  $b(t)$  is a pulse train with  $\sqrt{E_b}$  and  $-\sqrt{E_b}$  levels.
- ▶ Suppose we have a rectangular pulse  $p(t)$  of duration  $T_b$  (assume non-zero in  $[0, T_b)$ ) and amplitude  $A$ . What is the normalized energy spectrum  $|P(f)|^2$  of this pulse?

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- ▶  $|P(f)|^2 = A^2 T_b^2 \text{sinc}^2(\pi f T_b)$
- ▶ Suppose we take bit sequences of length  $n$  and compute their normalized energy spectrums
- ▶ An average normalized power spectrum  $G(f)$  can be obtained as  $\frac{1}{nT_b} \times$  energy spectrum of  $n$  bit sequence.
- ▶ Turns out that the normalized energy spectrum for  $n$  pulses is  $nA^2 T_b^2 \text{sinc}^2(\pi f T_b)$
- ▶ Therefore, the normalized power spectrum  $|B(f)|^2$  is  $A^2 T_b \text{sinc}^2(\pi f T_b)$

# Power spectrum of BPSK

- ▶ So  $|B(f)|^2$  is  $A^2 T \text{sinc}^2(\pi f T_b)$
- ▶ We are translating this baseband spectrum to  $f_c$  and  $-f_c$  when we are multiplying it by the carrier signal  $c(t)$
- ▶ What is the normalized power spectrum of the BPSK signal?

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- ▶ We are translating this baseband spectrum to  $f_c$  and  $-f_c$  when we are multiplying it by the carrier signal  $c(t)$
- ▶ What is the normalized power spectrum of the BPSK signal?
- ▶ It is approximately  $\frac{1}{4} [A^2 T_b \text{sinc}^2(\pi(f - f_c) T_b) + A^2 T_b \text{sinc}^2(\pi(f + f_c) T_b)]$

# Power spectrum of BASK

- ▶ A BASK  $s(t)$  is  $\frac{A}{2} \cos(2\pi f_c t) + \frac{s_{PSK}(t)}{2}$  !
- ▶ We think of the BASK signal as a carrier component along with a BPSK signal.
- ▶ The spectrum has a carrier component at  $f_c$ , which is not present for BPSK.



# Power spectrum of BFSK

- ▶ A BFSK  $s(t)$  is the sum of two BASK signals
- ▶  $s(t) = b(t)\sqrt{\frac{2}{T_b}}\cos(2\pi f_1 t) + (1 - b(t))\sqrt{\frac{2}{T_b}}\cos(2\pi f_2 t)$
- ▶ The spectrum of  $s(t)$  can be obtained approximately as the sum of two BASK spectrums!

## Quadrature phase shift keying (QPSK)

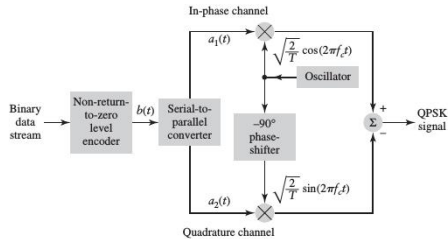
- ▶ For  $kT \leq t < (k+1)T$

$$s(t) = \sqrt{\frac{2E}{T}} \cos \left( 2\pi f_c t + (2i-1)\frac{\pi}{4} \right),$$

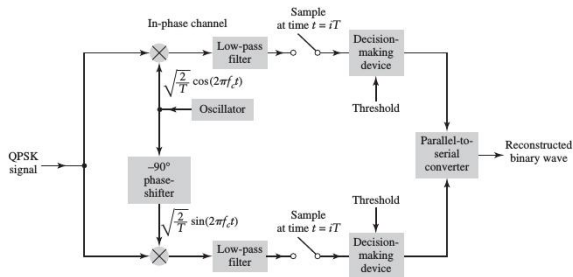
where  $i \in \{1, 2, 3, 4\}$

- ▶ Note that the time interval  $T$  is possibly different from  $T_b$
- ▶ A generalized version is M-ary PSK
- ▶ Recall quadrature carrier multiplexing - two signals multiplexed together using quadrature carriers but no increase in bandwidth
- ▶  $s(t) = \sqrt{\frac{2E}{T}} \cos \left( (2i-1)\frac{\pi}{4} \right) \cos(2\pi f_c t) - \sqrt{\frac{2E}{T}} \sin \left( (2i-1)\frac{\pi}{4} \right) \sin(2\pi f_c t)$ 
  - ▶ Combination of two BPSK signals - the bits can be chosen independently
  - ▶ A representation using vectors - constellation diagram

# QPSK - generation and detection



(a)



(b)