

QMM assignment: module 11

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11/20/2022

AP is a shipping service that guarantees overnight delivery of packages in the continental US. The company has various hubs at major cities and airports across the country. Packages are received at hubs, and then shipped to intermediate hubs or to their final destination.

The manager of the AP hub in Cleveland is concerned about labor costs, and is interested in determining the most effective way to schedule workers. The hub operates seven days a week, and the number of packages it handles varies from one day to another.

Setting default values to get a clean output

```
knitr::opts_chunk$set(message = FALSE)
knitr::opts_chunk$set(warning = FALSE)
```

Loading the lpSolveAPI Package

```
library("lpSolveAPI")
```

Loading the lp file

```
table <- read.lp("pro.lp")
print(table)
```

```
## Model name:
##           x1  x2  x3  x4  x5  x6  x7
## Minimize  775 800 800 800 800 775 750
## Sunday    0   1   1   1   1   1   0 >= 18
## Monday    0   0   1   1   1   1   1 >= 27
## Tuesday   1   0   0   1   1   1   1 >= 22
## Wednesday 1   1   0   0   1   1   1 >= 26
## Thursday  1   1   1   0   0   1   1 >= 25
## Friday    1   1   1   1   0   0   1 >= 21
## Saturday  1   1   1   1   1   0   0 >= 19
## Kind      Std Std Std Std Std Std Std
## Type      Int Int Int Int Int Int Int
## Upper     Inf Inf Inf Inf Inf Inf Inf
## Lower      0   0   0   0   0   0   0
```

The number of workers required for each day of the week is estimated in the table below.

```
Day_Wise_Workers_Req <- matrix(c("Sunday", "Monday", "Tuesday", "Wednesday", "Thursday", "Friday", "Saturday"
18,27,22,26,25,21,19),ncol=2,byrow = F)
colnames(Day_Wise_Workers_Req) <- c("Day_of_the_week", "Workers_Required")
as.table(Day_Wise_Workers_Req)
```

```
##   Day_of_the_week Workers_Required
## A Sunday          18
```

```
## B Monday      27
## C Tuesday     22
## D Wednesday   26
## E Thursday    25
## F Friday      21
## G Saturday    19
```

Package handlers at AP are guaranteed a five-day work week with two consecutive days off. The base wage for the handlers is \$750 per week. Workers working on Saturday or Sunday receive an additional \$25 per day. The possible shifts and salaries for package handlers are:

```
Day_offs_and_wages <- matrix(c(1,2,3,4,5,6,7,
                                "Sunday and Monday","Monday and Tuesday","Tuesday and Wednesday",
                                "Wednesday and Thursday","Thursday and Friday","Friday and Saturday","Saturday and Sunday",
                                "$775","$800","$800","$800","$800","$775","$750"),ncol=3,byrow=F)
colnames(Day_offs_and_wages) <- c("Shift", "Days_Off", "Wage")
as.table(Day_offs_and_wages)
```

```
##   Shift Days_Off      Wage
## A 1      Sunday and Monday $775
## B 2      Monday and Tuesday $800
## C 3      Tuesday and Wednesday $800
## D 4      Wednesday and Thursday $800
## E 5      Thursday and Friday $800
## F 6      Friday and Saturday $775
## G 7      Saturday and Sunday $750
```

Running the lp model

```
solve(table)
```

```
## [1] 0
```

We may determine that there is a model by getting 0 as the value.

Total Cost - Objective Function

```
get.objective(table)
```

```
## [1] 25675
```

The overall cost to the company to achieve the lowest feasible total wage expenses and a sufficient number of people who are available to work each day is “25,675\$”.

How many workers are available each day to work - Variables

```
get.variables(table)
```

```
## [1] 2 4 5 0 8 1 13
```

The variables are labeled from x_1, x_2, \dots, x_7 where,

x_1 = Number of workers assigned to shift 1 = 2

x_2 = Number of workers assigned to shift 2 = 4

x_3 = Number of workers assigned to shift 3 = 5

x_4 = Number of workers assigned to shift 4 = 0

x_5 = Number of workers assigned to shift 5 = 8

x_6 = Number of workers assigned to shift 6 = 1

x_7 = Number of workers assigned to shift 7 = 13

By the variable values attained we can thereby get to see how many workers are available to work each day

with respect to the objective function as well as the constraints framed by the organization,

$$\text{Sunday} = x_2 + x_3 + x_4 + x_5 + x_6 = 18 \text{ Workers}$$

$$\text{Monday} = x_3 + x_4 + x_5 + x_6 + x_7 = 27 \text{ Workers}$$

$$\text{Tuesday} = x_4 + x_5 + x_6 + x_7 + x_1 = 24 \text{ Workers}$$

$$\text{Wednesday} = x_5 + x_6 + x_7 + x_1 + x_2 = 28 \text{ Workers}$$

$$\text{Thursday} = x_6 + x_7 + x_1 + x_2 + x_3 = 25 \text{ Workers}$$

$$\text{Friday} = x_7 + x_1 + x_2 + x_3 + x_4 = 24 \text{ Workers}$$

$$\text{Saturday} = x_1 + x_2 + x_3 + x_4 + x_5 = 19 \text{ Workers}$$