



## Day 4: Geometric Distribution I ☆

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Terms you'll find helpful in completing today's challenge are outlined below.

### Negative Binomial Experiment

A negative binomial experiment is a statistical experiment that has the following properties:

- The experiment consists of  $n$  repeated trials.
- The trials are independent.
- The outcome of each trial is either success ( $s$ ) or failure ( $f$ ).
- $P(s)$  is the same for every trial.
- The experiment continues until  $x$  successes are observed.

If  $X$  is the number of experiments until the  $x^{th}$  success occurs, then  $X$  is a discrete random variable called a negative binomial.

### Negative Binomial Distribution

Consider the following probability mass function:

$$b^*(x, n, p) = \binom{n-1}{x-1} \cdot p^x \cdot q^{(n-x)}$$

The function above is negative binomial and has the following properties:

- The number of successes to be observed is  $x$ .
- The total number of trials is  $n$ .
- The probability of success of  $1$  trial is  $p$ .
- The probability of failure of  $1$  trial  $q$ , where  $q = 1 - p$ .
- $b^*(x, n, p)$  is the negative binomial probability, meaning the probability of having  $x - 1$  successes after  $n - 1$  trials and having  $x$  successes after  $n$  trials.

**Note:** Recall that  $\binom{n}{x} = \frac{n!}{x!(n-x)!}$ . For further review, see the [Combinations and Permutations Tutorial](#).

## Geometric Distribution

The geometric distribution is a special case of the negative binomial distribution that deals with the number of Bernoulli trials required to get a success (i.e., counting the number of failures before the first success). Recall that  $X$  is the number of successes in  $n$  independent Bernoulli trials, so for each  $i$  (where  $1 \leq i \leq n$ ):

$$X_i = \begin{cases} 1 & \text{if the } i^{\text{th}} \text{ trial is a success} \\ 0 & \text{otherwise.} \end{cases}$$

The geometric distribution is a negative binomial distribution where the number of successes is  $1$ . We express this with the following formula:

$$g(n, p) = q^{(n-1)} \cdot p$$

## Example

Bob is a high school basketball player. He is a **70%** free throw shooter, meaning his probability of making a free throw is **0.70**. What is the probability that Bob makes his first free throw on his fifth shot?

For this experiment,  $n = 5$ ,  $p = 0.7$  and  $q = 0.3$ . So,  $g(n = 5, p = 0.7) = 0.3^4 0.7 = 0.00567$

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