

## Part I — Recognition (20)

1. Which best defines a *data type*?
  - a) A set of heterogeneous values and one operation
  - b) A homogeneous collection of values and the operations on them
  - c) A memory block reserved at run time only
  - d) A compiler directive for optimization
2. A type system is used primarily for:
  - a) Code formatting
  - b) Error detection and program organization
  - c) Faster I/O
  - d) GUI rendering
3. A type system typically includes:
  - a) Only built-in types
  - b) New-type mechanisms and rules for equivalence/compatibility/inference
  - c) Garbage collection policy only
  - d) Linker scripts
4. Scalar types are:
  - a) Composite and heterogeneous
  - b) Atomic and can compose other types
  - c) Only booleans and integers
  - d) Only hardware-independent
5. In IEEE-754 single precision, the fields are:
  - a) 1 sign, 11 exponent, 52 fraction
  - b) 1 sign, 8 exponent, 23 fraction
  - c) 0 sign, 10 exponent, 53 fraction
  - d) 1 sign, 7 exponent, 24 fraction
6. In an **enumeration type**, a key design issue is whether:
  - a) Enum constants may appear in more than one enum definition
  - b) The enum must start from value 100
  - c) It must be 64-bit
  - d) It must be printable only as an integer
7. A *subrange type* is:
  - a) A dynamic array
  - b) A contiguous subset of an ordinal type
  - c) Any user class
  - d) A record with only two fields
8. Jagged vs rectangular arrays:
  - a) Jagged use row-major, rectangular use column-major
  - b) Jagged allow rows of different lengths; rectangular have uniform shape
  - c) Rectangular are only in C++
  - d) Jagged are only in Fortran
9. A *slice* of an array/list is:
  - a) A deep copy only

- b) A referencing mechanism for a substructure
  - c) A pointer to the first element only
  - d) Only valid for 1-D arrays
10. In row-major storage, the second subscript varies:
- a) Slowest
  - b) Fastest
  - c) Neither
  - d) Unspecified
11. An *associative array* (map/dict) is indexed by:
- a) Only integers
  - b) Only strings
  - c) Keys chosen by the programmer (hashable or comparable)
  - d) Memory addresses
12. String length strategies include:
- a) Static, limited dynamic, and dynamic length
  - b) Only dynamic
  - c) Only static
  - d) Only limited dynamic
13. A *record* is:
- a) Homogeneous aggregate
  - b) Heterogeneous aggregate with named fields
  - c) Linked list node
  - d) Fixed-point number
14. Two fundamental pointer operations are:
- a) Hashing and concatenation
  - b) Assignment of addresses and dereferencing
  - c) Subtyping and overloading
  - d) Boxing and unboxing
15. A *dangling pointer* is:
- a) A pointer set to null
  - b) A pointer to deallocated storage
  - c) A pointer to constant memory
  - d) A reference parameter
16. Compared to pointers, C++ references:
- a) Can be reseated to another object
  - b) Can be null by default
  - c) Must be bound at initialization and cannot be reseated
  - d) Do not alias their targets
17. *Type equivalence* "by name" means two types are equivalent if:
- a) They have identical structure only
  - b) They have the same declared type name
  - c) They occupy the same number of bytes
  - d) One can be cast to the other
18. *Type compatibility* is best described as:
- a) The same as equivalence

- b) Allowing a value of T wherever S is admissible under certain rules
  - c) Only allowing implicit casts
  - d) Only allowing explicit casts
19. *Coercion vs cast:*
- a) Coercion is explicit; cast is implicit
  - b) Both are explicit
  - c) Coercion is implicit; cast is explicit
  - d) Neither changes representation
20. Polymorphism kinds include:
- a) Ad hoc (overloading) and universal (parametric, subtyping)
  - b) Only subtyping
  - c) Only parametric
  - d) Only templates

## Part II — Application (20)

21. The largest **signed** integer with 7 bits in two's complement is:  
a) 63 b) 64 c) 127 d) 32
22. Assume `char=1B`, `short=2B`, `int=4B`, `float=4B`, 4-byte alignment. What is the size of

```
struct X { char a; int b; char c; short d; };
```

- a) 11 b) 12 c) 14 d) 16
23. Row-major 2-D array `a[0..2][0..3]` of 4-byte ints, base address  $\alpha=1000$ . Address of `a[2][1]` is:  
a) 1016 b) 1024 c) 1036 d) 1048
24. Column-major 2-D array with 1-based indices `A[1..3, 1..4]`, 4-byte ints, base  $\alpha=1000$ . Address of `A[3,2]` is:  
a) 1008 b) 1016 c) 1020 d) 1032
25. The set type `set of -2..13` represented by a bit chain needs how many bits?  
a) 14 b) 15 c) 16 d) 17
26. In C, which output is *well-defined* for

```
union U { int data; unsigned char bt[4]; } x; x.data = 0x00007A12; printf("%u %u\n", x.bt[0], x.bt[1]);
```

(Assume little-endian)

- a) 18 122 b) 122 18 c) 7 162 d) Implementation-defined, but on little-endian it is 18 122
27. For the Pascal-style 3-D array `x[2..4, -3..5, -2..4]` of 4-byte integers stored **column-major** (rightmost subscript varies slowest), base  $\alpha$ . Which linearization formula is correct for address of `x[i,j,k]` ?  
a)  $\alpha + (((i-2)*9 + (j+3))*7 + (k+2))*4$   
b)  $\alpha + (((k+2)*9 + (j+3))*3 + (i-2))*4$

- c)  $\alpha + (((j+3)*3 + (i-2))*7 + (k+2))*4$   
 d)  $\alpha + (((i-2)*7 + (k+2))*9 + (j+3))*4$
28. With 32-bit IEEE-754 single precision, how many fraction bits are stored?  
 a) 22 b) 23 c) 24 d) 52
29. In most languages that allow it, `char name[] = "abc";` initializes the array with length:  
 a) 3 b) 4 (including `'\0'`) c) 5 d) Implementation-defined
30. Given the `slice` in Python:

```
v = [2,4,6,8,10,12]; v[1:5:2]
```

The result is:

- a) `[4,8]` b) `[4,6,8,10]` c) `[4,6,8]` d) `[4,8,12]`
31. In C/C++, which statement about pointers is true?  
 a) `void*` can be dereferenced safely  
 b) Pointer arithmetic on `int* p` adds bytes, not elements  
 c) `p[index]` is syntactic sugar for `*(p+index)`  
 d) `&` returns the value stored at the pointer
32. With 1-byte `char`, 2-byte `short`, 4-byte `int`, structure padding often makes the final struct size:  
 a) A multiple of the smallest member's alignment  
 b) Exactly the sum of field sizes  
 c) A multiple of the largest member's alignment  
 d) Always a power of two
33. In C#, which pair is most accurate?  
 a) `string` is a primitive, fixed-length type  
 b) `string` is immutable and reference-semantics  
 c) `string` is always a 1-byte char array  
 d) `string` can be resized in place
34. Which is **not** a typical string operation listed in the handout?  
 a) Assignment b) Concatenation c) Pattern matching d) Matrix inversion
35. Regarding parameter passing in C++:  
 a) Reference parameters cannot alias the actuals  
 b) References can be resealed by assignment  
 c) `int& r = a;` binds `r` to `a` and `++r` increments `a`  
 d) Taking address of a reference is ill-formed
36. For a set type implemented by a **bit chain**, membership test `x in s` is  $O(1)$  because:  
 a) Hashing is used  
 b) The *i*th bit can be masked directly  
 c) A linked list is traversed  
 d) A binary search tree is used
37. For dynamic arrays in C++ `vector<int> v`, subscripting is:  
 a) Always range-checked  
 b) Never range-checked  
 c) Range-checked by `at`, unchecked by `operator[]`  
 d) Only at compile time

38. In Java, arrays are:
- Value types
  - Reference types with runtime bounds checking
  - Unchecked pointer arithmetic blocks
  - Always jagged with different row lengths enforced
39. Which statement about **unions** is true?
- Java supports C-style unions
  - C free unions do not carry a discriminant for type checking
  - Ada unions are free unions
  - Unions cannot overlap memory
40. Which is a correct *type expression* form?
- `array(I,T)` for index type `I` and element `T`
  - `function(T1,T2)` for product types
  - `pointer → T`
  - `record(name:T1;name:T2)` is not a type expression

## Part III — Advanced Application (20)

For Q41–Q60, assume the following library typings (when used):

- `map : (T1 → T2) × List[T1] → List[T2]`
- `filter : (T → bool) × List[T] → List[T]`
- `reduce : (U × V → U) × U × List[V] → U`
- `index : (T → bool) × List[T] → List[int]`
- `floor : real → int`
- List literal `[ ... ] : List[T]` if elements are of type `T`.

41. Consider pseudo-Python:

```
def foo(x,y,z): return reduce(z(x), y, [])
```

If `x` is an `int`, which is the most precise principal type for `foo`?

- $(\text{int} \times (\text{int} \rightarrow T) \times (T \rightarrow \text{int} \rightarrow T)) \rightarrow T$
- $(\text{int} \times T \times (T \times \text{int} \rightarrow T)) \rightarrow T$
- $(\text{int} \times T \times (T \times \text{int} \rightarrow T)) \rightarrow \text{int}$
- $(\text{int} \times (\text{int} \rightarrow T) \times (\text{int} \times T \rightarrow T)) \rightarrow T$

42. In a strict language, if `y(z(x))` then `x` else `0` type-checks only if:

- `y(z(x)) : bool` and `x, 0` share a common supertype
- `y(z(x)) : int`
- `x : bool`
- `0 : bool`

43. Bit-chain question: `x : set of -2..13`. If the least significant bit encodes the **smallest** element, which pair encodes `{ -2, 5 }`?

- `1000...0001`

- b) `0000...0001`  
 c) A bitstring with bit 0 and bit 7 set  
 d) A bitstring with bit 2 and bit 13 set
44. Column-major 3-D array `A[0..2, 1..3, 0..1]` of 4-byte ints, base  $\alpha=2000$ . Address of `A[2,3,1]` is:  
 (Use order: last index varies slowest.)  
 a) 2012 b) 2032 c) 2060 d) 2084
45. C struct alignment. Assume 8-byte alignment for `double`, 4-byte for `int`, 1-byte for `char`:

```
struct R { char a; double b; int c; char d; };
```

Total size is:

- a) 18 b) 24 c) 32 d) 40

46. Free union punning (little-endian), choose the **most correct** statement:

```
union V { float f; unsigned int u; } v; v.u = 0x3F800000;
```

- a) `v.f` is exactly `1.0f` per IEEE-754  
 b) Behavior is undefined  
 c) It is defined and always yields `0.0f`  
 d) It traps

47. Given:

```
def h(x): return lambda y,z: filter(y, map(z, x))
```

With the library typings above, the principal type of `h` is:

- a) `List[T] → ((T → bool) × (U → T) → List[T])`  
 b) `List[T] → ((T → bool) × (U → T) → List[U])`  
 c) `List[T] → ((U → bool) × (T → U) → List[U])`  
 d) `List[T] → ((U → bool) × (U → T) → List[T])`

48. Consider:

```
def g(x): def k(z): return y(z) + x return k
```

In a statically typed setting with `+` overloaded for `int` and `real` only, pick a valid typing when `y : (int → int)`.

- a) `x : int, result k : (int → int)`  
 b) `x : bool, result k : (int → bool)`  
 c) `x : real, result k : (int → real)`  
 d) a or c

49. Two's complement: the range of an `n`-bit signed integer is:

- a) `[-2^(n-1), 2^(n-1)-1]`  
 b) `[0, 2^n - 1]`  
 c) `[-2^n, 2^n-1]`  
 d) `[-2^(n-1)+1, 2^(n-1)]`

50. IEEE-754 single precision. Which bit pattern encodes **-0.0**?
- Sign=1, all exponent and fraction bits 0
  - Sign=0, exponent all ones, fraction nonzero
  - Sign=0, exponent bias, fraction all zeros
  - Sign=1, exponent all ones, fraction all zeros
51. With `index : (T→bool) × List[T] → List[int]` and `floor : real → int`, consider:

```
def q(u,v): return index(v, map(floor, u))
```

A principal type for `q` is:

- `(List[real] × (int → bool)) → List[int]`
  - `(List[int] × (real → bool)) → List[int]`
  - `(List[real] × (real → bool)) → List[int]`
  - `(List[T] × (T → bool)) → List[int]`
52. Name vs structural equivalence. Which pair is **equivalent by structure** but not by name?
- Two distinct typedefs of the same record layout
  - An `int` and a `float`
  - `array(0..9, int)` and `array(1..10, int)`
  - A class and its subclass

53. Parametric polymorphism example:

```
template <class T> void swap(T& x, T& y) { T t=x; x=y; y=t; }
```

Which is true?

- Works only for built-ins
- Requires `T` to be a pointer
- Works for any `T` with copy/move semantics
- Requires virtual dispatch

54. Subtyping polymorphism example:

```
struct Polygon { virtual float area() = 0; }; struct Rect : Polygon { float area(){return h*w;}} float h,w; }; Polygon* p = new Rect{3,4};
```

The dynamic call `p->area()` is resolved:

- At compile time by static type
  - At run time via dynamic dispatch
  - By template instantiation
  - Never, because abstract
55. Python lists are:
- Immutable and fixed-length
  - Mutable, dynamic, and can contain heterogeneous elements
  - Only numeric
  - Value-semantics like C arrays

56. In C, which causes a **dangling pointer**?

- `int *p = NULL;`

- b) `int *p = malloc(4); free(p); *p = 5;`
- c) `int a=3; int *p=&a;`
- d) `int *p = (int*)0x0;`

57. Consider:

```
def r(f, xs): return reduce(lambda acc, t: acc + [f(t)], [], xs)
```

Given list concatenation and single-element append via `acc + [f(t)]`, the principal type is:

- a)  $((T \rightarrow U) \times \text{List}[T]) \rightarrow \text{List}[U]$
- b)  $((T \rightarrow U) \times \text{List}[U]) \rightarrow \text{List}[T]$
- c)  $((T \rightarrow \text{bool}) \times \text{List}[T]) \rightarrow \text{List}[T]$
- d)  $(T \times \text{List}[T]) \rightarrow \text{List}[T]$

58. Column-major `B[1..4, 1..5]` of 8-byte doubles, base  $\alpha=5000$ . Address of `B[4,5]` is:

- a)  $5000 + ((5-1)*4 + (4-1))*8$
- b)  $5000 + ((4-1)*5 + (5-1))*8$
- c)  $5000 + (45)*8$
- d)  $5000 + ((5-1)*5 + (4-1))*8$

59. Record vs array comparison (from the evaluation slide). Which is accurate?

- a) Arrays are heterogeneous, records homogeneous
- b) Arrays are processed in the same way per element; record fields can be processed differently
- c) Records support dynamic subscripting
- d) Arrays never allow dynamic subscripting

60. Reference vs pointer in C++. Which is valid?

- a) `int& r = a; r++;` mutates `a` and `r` cannot be reseated
- b) `int& r;` is fine without initialization
- c) `int* p = &a; p = &b;` reseats pointer the same way a reference reseats
- d) References can be null by default

## Answer Key (letters)

- 1 b
- 2 b
- 3 b
- 4 b
- 5 b
- 6 a
- 7 b
- 8 b
- 9 b
- 10 b
- 11 c
- 12 a
- 13 b
- 14 b



15 b  
16 c  
17 b  
18 b  
19 c  
20 a  
21 a  
22 b  
23 c  
24 c  
25 c  
26 d  
27 b  
28 b  
29 b  
30 a  
31 c  
32 c  
33 b  
34 d  
35 c  
36 b  
37 c  
38 b  
39 b  
40 a  
41 b  
42 a  
43 c  
44 d  
45 c  
46 b  
47 a  
48 d  
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58 a  
59 b  
60 a