



$$2) \begin{cases} -x + 2y - z = 3 \\ 2x + y + 3z = 5 \\ 3x + 4y + 5z = 13 \end{cases} \quad \begin{cases} -x + 2y - z = 3 \\ \cancel{2x + y + 3z = 5} \quad 5y + z = 11 \\ 5y + z = 11 \end{cases}$$

$$l_2 = 2l_1 + l_3$$

$$\begin{aligned} -2x + 2y - z &= 3 \\ 2x + y + 3z &= 5 \\ 5y + z &= 11 \end{aligned}$$

$$l_3 = 3l_1 + l_2$$

$$\begin{aligned} -3x + 6y - 3z &= 9 \\ 2x + 4y + 5z &= 13 \\ 10y + 2z &= 22 \\ 5y + z &= 11 \end{aligned}$$

$$\boxed{z = k}$$

$$\begin{cases} -x + 2y - k = 3 \\ 5y + k = 11 \end{cases}$$

$$5y + k = 11 \rightarrow y = \frac{11 - k}{5}$$

$$-x + 2\left(\frac{11 - k}{5}\right) - k = 3 \rightarrow -x + \frac{22 - 2k}{5} - k = 3$$

$$-x + 22 - 7k = 15 \rightarrow -x = \frac{15 - 22 + 7k}{5}$$

$$-x = \frac{-7 + 7k}{5} \rightarrow x = \frac{7 - 7k}{5}$$



$$5-) a) \begin{vmatrix} 5 & 3 \\ 8 & 5 \end{vmatrix} \quad 25 - 24 = 1$$

$$\begin{vmatrix} 5 & 3 \\ 8 & 5 \end{vmatrix} \cdot \begin{vmatrix} x & y \\ a & b \end{vmatrix} = \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix}$$

$$\begin{matrix} 5x + 3a \\ 8x + 5a \end{matrix} \begin{matrix} 5y + 3b \\ 8y + 5b \end{matrix} = \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix}$$

$$\begin{cases} 5x + 3a = 1 \\ 8x + 5a = 0 \end{cases} \begin{cases} -40x + 24a = 28 \\ 40x + 25a = 0 \end{cases}$$

$$\boxed{a = -8}$$

$$5x + 3(-8) = 1 = 25$$

$$5x = 29 \Rightarrow \boxed{x = 5}$$

$$\begin{cases} 5y + 3b = 0 \\ 8y + 5b = 1 \end{cases} \begin{cases} -40y + 24b = 0 \\ 40y + 25b = 5 \end{cases} \begin{cases} 5y + 3(-5) = 0 \\ 5y + 15 \end{cases}$$

$$\boxed{b = 5}$$

$$\boxed{y = -5}$$

$$\begin{vmatrix} 5 & -3 \\ -8 & 5 \end{vmatrix}$$

$$b) \begin{vmatrix} & S & & I \\ 1 & 0 & 0 & \\ 3 & 1 & 0 & \\ 5 & 7 & 1 & \\ 1 & & & 0 \end{vmatrix} \quad 1 + 0 + 0 - (0 + 0 + 0)$$

$$\text{Det } Z = 1$$

$$\begin{vmatrix} 1 & -3 & 16 \\ 0 & 1 & -7 \\ 0 & 0 & 1 \end{vmatrix}$$

$$A_{11} = (-1)^{1+1} = \begin{vmatrix} 1 & 0 \\ 7 & 1 \end{vmatrix} = 1 \quad A_{12} = (-1)^{1+2} = \begin{vmatrix} 3 & 0 \\ 5 & 1 \end{vmatrix} = -3$$

$$A_{13} = (-1)^{1+3} = \begin{vmatrix} 3 & 1 \\ 5 & 7 \end{vmatrix} = 21 - 5 = 16 \quad A_{21} = (-1)^{2+1} = \begin{vmatrix} 1 & 0 \\ 7 & 1 \end{vmatrix} = 1$$

$$A_{22} = (-1)^{2+2} = \begin{vmatrix} 1 & 0 \\ 7 & 1 \end{vmatrix} = 1 \quad A_{23} = (-1)^{2+3} = \begin{vmatrix} 1 & 0 \\ 5 & 7 \end{vmatrix} = 7(-1) = -7$$

$$A_{31} = (-1)^{3+1} = \begin{vmatrix} 0 & 0 \\ 1 & 0 \end{vmatrix} = 0 \quad A_{32} = (-1)^{3+2} = \begin{vmatrix} 1 & 0 \\ 3 & 1 \end{vmatrix} = 1$$

$$A_{33} = (-1)^{3+3} = \begin{vmatrix} 1 & 0 \\ 3 & 1 \end{vmatrix} = 1$$

D S T Q Q S S

columnas para linha

linha para column

$$\begin{array}{ccc|c|ccc} 1 & -3 & 16 & -x & 1 & 0 & 0 \\ 0 & 1 & -7 & = & -3 & 1 & 0 \\ 0 & 0 & 1 & & 16 & -7 & 1 \end{array}$$

$$A^{-1} = \frac{1}{1} \begin{pmatrix} 1 & -7 & 16 \\ 0 & 1 & -7 \\ 0 & 0 & 1 \end{pmatrix} z$$





$$6-a) \begin{vmatrix} 4 & & & 4 \\ 1 & \times & 1 & 2 \\ 2 & \times & 3 & 4 \\ 4 & & 5 & 4 \\ 1 & & & 2 \end{vmatrix} \begin{array}{l} 12 + 16 + 20 - (24 + 8 + 20) \\ 48 - 52 \\ \text{Det} = -4 \end{array}$$

$$b) \begin{vmatrix} 4 & 1 \\ 2 & 0 \end{vmatrix} \begin{array}{l} 0 - 2 \\ \text{Det} = -2 \end{array}$$

$$c) \begin{vmatrix} 1 & 3 & 4 \\ 2 & 1 & 0 \\ 0 & 1 & 1 \end{vmatrix} \begin{array}{l} 1 + 0 + 2 - (0 + 6 + 0) \\ 3 - 6 \\ \text{Det} = -3 \end{array}$$

$$d) \begin{vmatrix} 1 & 2 & 1 \\ 2 & 1 & 3 \\ 1 & 0 & 1 \end{vmatrix} \begin{array}{l} 1 + 6 + 0 - (1 + 4 + 0) \\ 7 - 5 \\ \text{Det} = 2 \end{array}$$

$$e) \begin{vmatrix} 1 & 0 & 0 & 0 \\ 3 & 2 & 0 & 0 \\ 1 & 1 & 4 & 0 \\ 4 & 0 & 4 & -1 \end{vmatrix}$$

$$\begin{vmatrix} 2 & 0 & 0 \\ 1 & 4 & 0 \\ 0 & 1 & -1 \\ 2 & 0 & 0 \end{vmatrix} \rightarrow 1$$

$$(-8 + 0) - (0 + 0 + 0)$$

$$\boxed{\text{Det} = -8}$$

$$A \begin{vmatrix} 1 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 2 \end{vmatrix} \quad z \begin{vmatrix} 3 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 2 \end{vmatrix}$$

$$\boxed{\text{Det} = 24}$$