Data Structures Sorting Technique – Heap Sort

Team Emertxe



Dependency Algorithm

Introduction





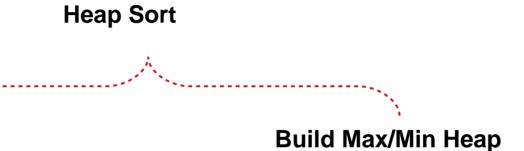


Introduction



Dependency Algorithm:

Max / Min heapify





Max heapify

Introduction



Heapify:

Its a process of converting the given binary tree into heap. It can be either min heap or max heap

•arr[SIZE]



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•arr[SIZE]

SIZE = 10

1	14	10	8	7	9	3	2	4	6

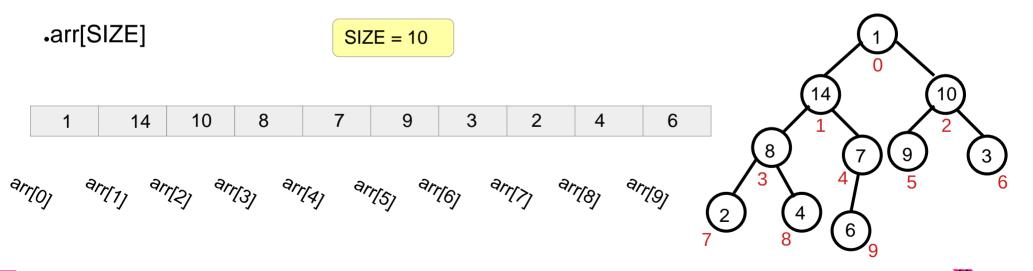
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Introduction

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Its a process of converting the given binary tree into heap. It can be either min heap or max heap





Algorithm

maxheapify(arr,index,size):

Input Specification:

arr : Array to hold elements

Index: Integer value

size: Length of the array



index = 0

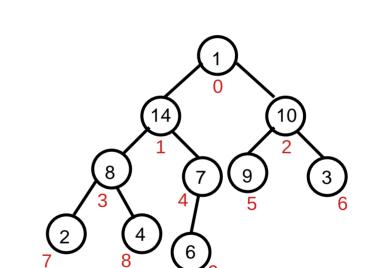
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maxheapify(arr,index,size)
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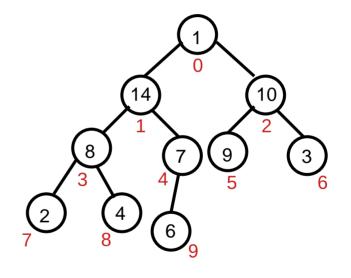




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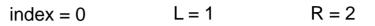


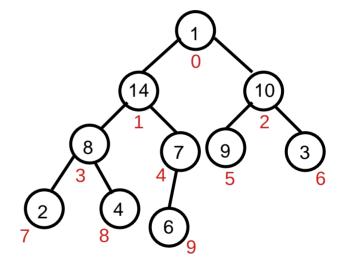




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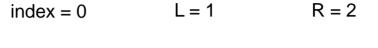


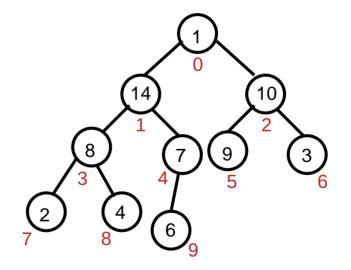




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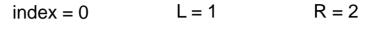


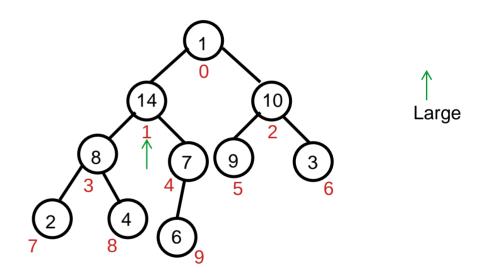




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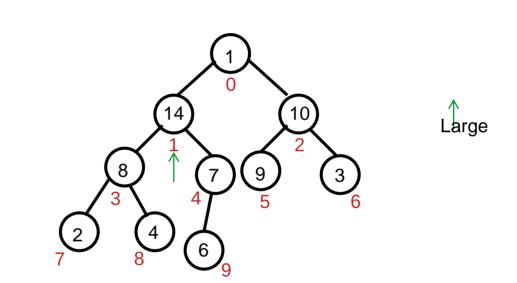


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SIZE = 10

R = 2

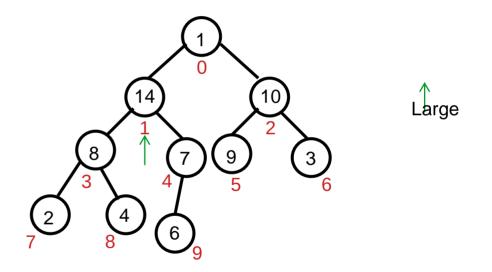
L = 1





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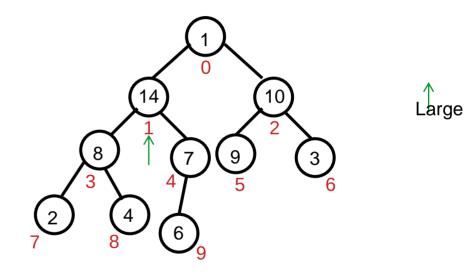
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index = 0 L = 1 R = 2
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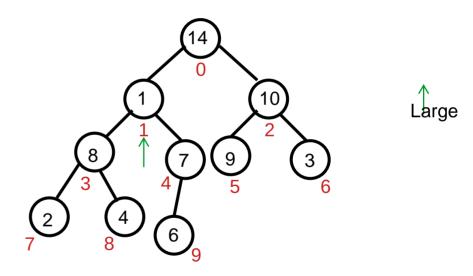


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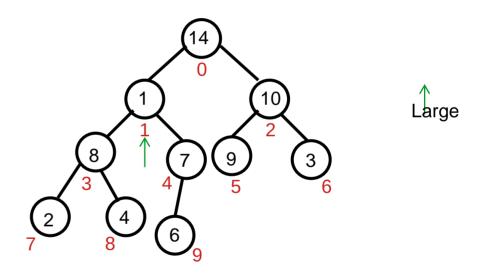
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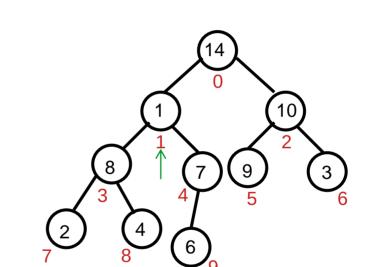
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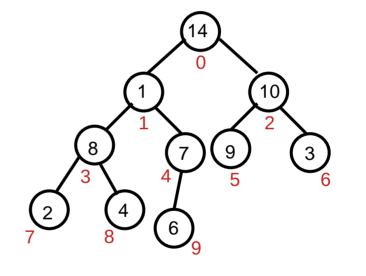


Large

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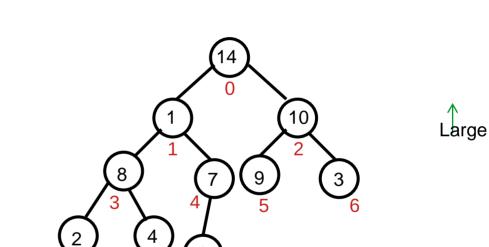


Large

```
SIZE = 10
```

R = 4

```
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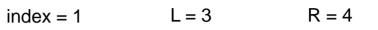


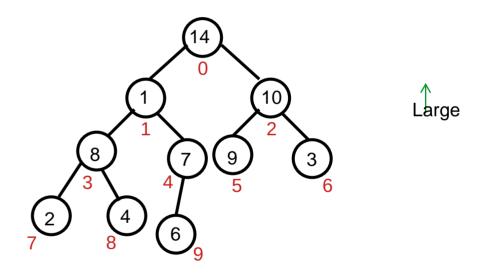
L = 3



```
SIZE = 10
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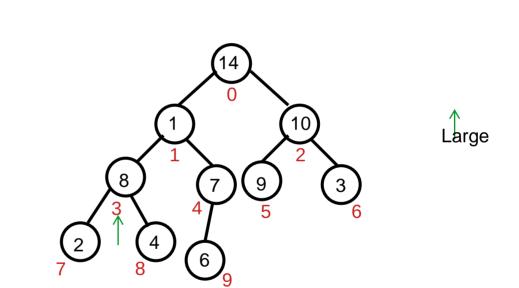




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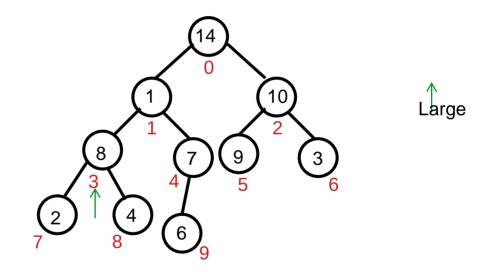


L = 3



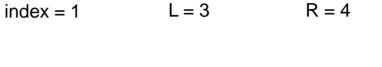
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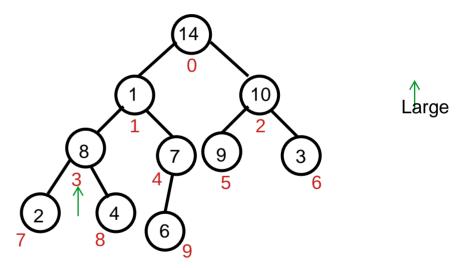
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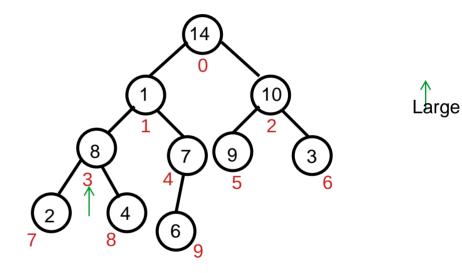


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$$R = 4$$

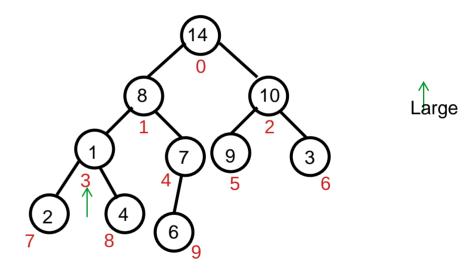




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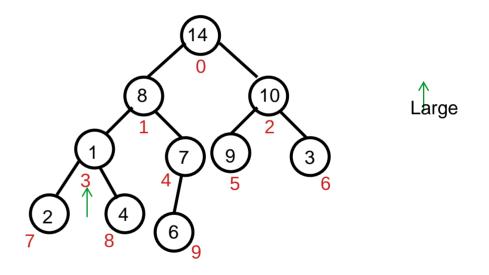


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$$R = 4$$

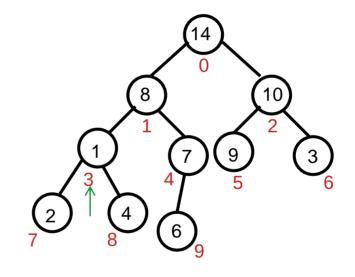




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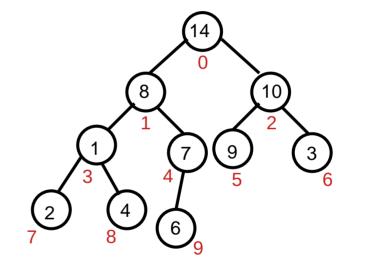


Large

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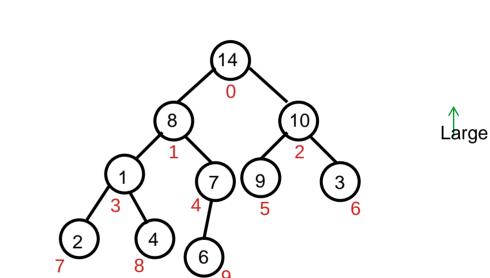


Large

```
SIZE = 10
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R = 8

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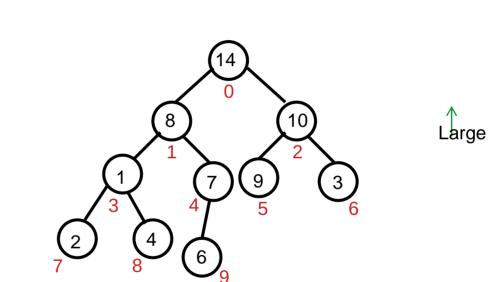
L = 7



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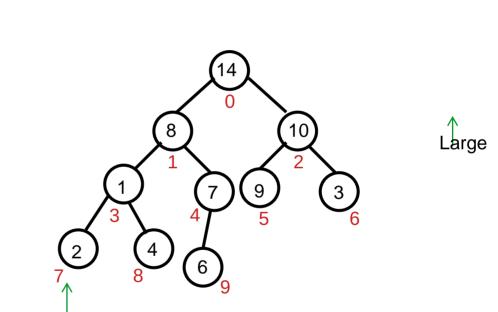
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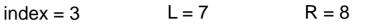
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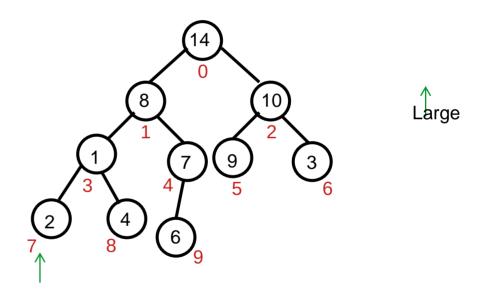


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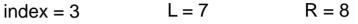
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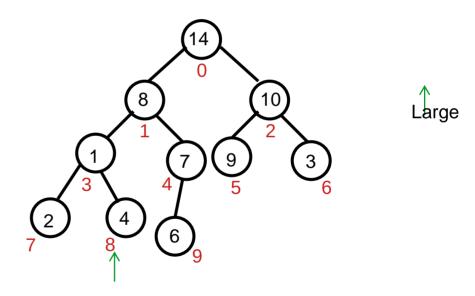






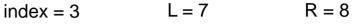
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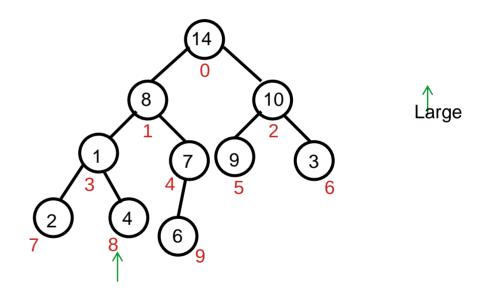






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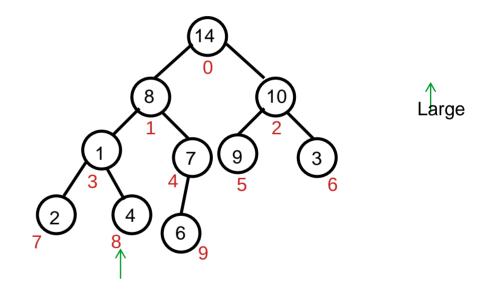






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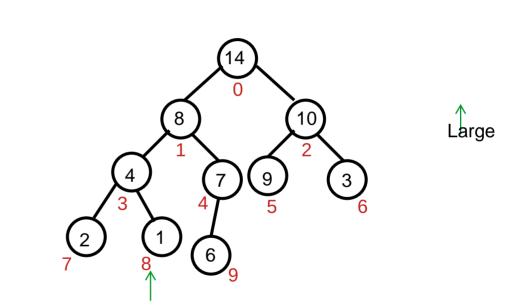
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SIZE = 10

L = 7

index = 3

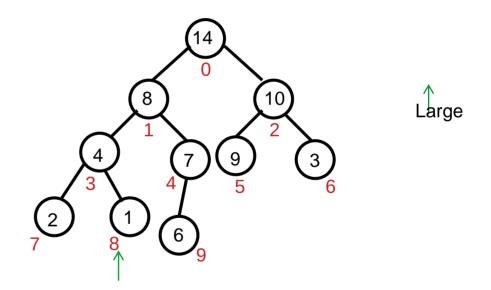
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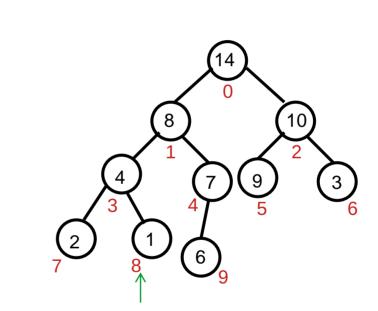
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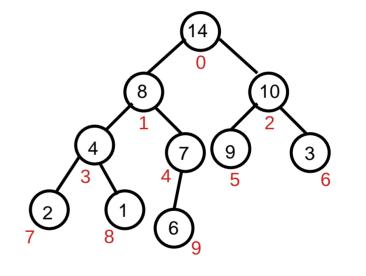




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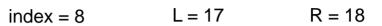


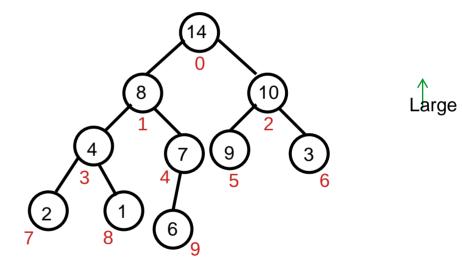


Large

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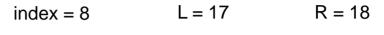


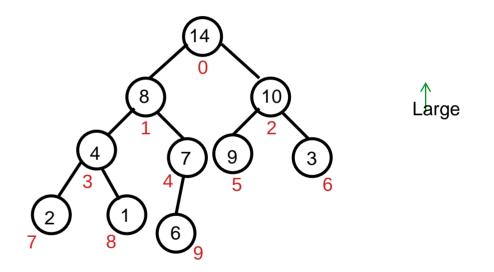




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else
 large = index
if(R < size AND arr[large] < arr[R])</pre>
 large = R
if(index != large)
 swap(arr[large],arr[index])
 maxheapify(arr,large,size)
```



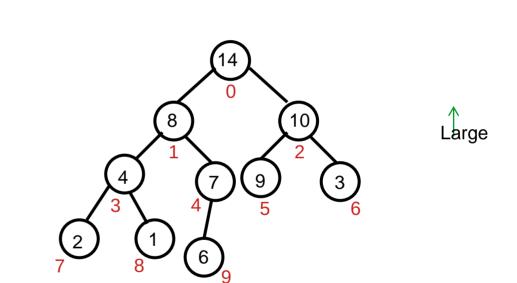




```
SIZE = 10
```

R = 18

```
L = 2*index +1
R = 2*index+2
if(L < size AND arr[index] < arr[L])</pre>
 large = L
else
 large = index
if(R < size AND arr[large] < arr[R])</pre>
 large = R
if(index != large)
 swap(arr[large] ,arr[index])
 maxheapify(arr,large,size)
```



L = 17

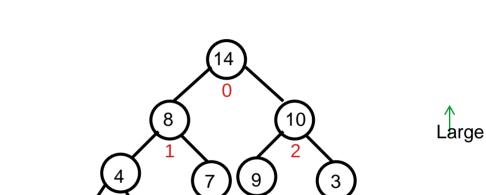
index = 8



```
SIZE = 10
```

R = 18

```
L = 2*index +1
R = 2*index+2
if(L < size AND arr[index] < arr[L])</pre>
 large = L
else
 large = index
if(R < size AND arr[large]< arr[R])</pre>
 large = R
if(index != large)
 swap(arr[large] ,arr[index])
 maxheapify(arr,large,size)
```

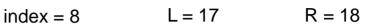


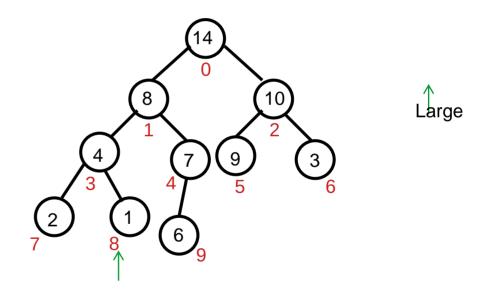
L = 17

index = 8



```
L = 2*index +1
R = 2*index+2
if(L < size AND arr[index] < arr[L])
 large = L
else
 large = index
if(R < size AND arr[large] < arr[R])</pre>
 large = R
if(index != large)
 swap(arr[large],arr[index])
 maxheapify(arr,large,size)
```

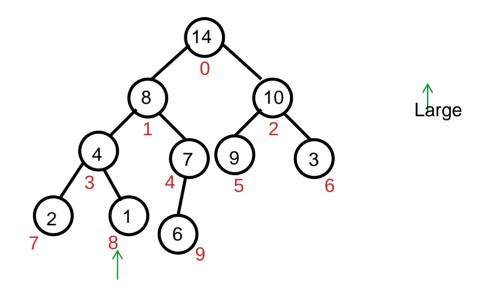






```
L = 2*index +1
R = 2*index+2
if(L < size AND arr[index] < arr[L])</pre>
 large = L
else
 large = index
if(R < size AND arr[large] < arr[R])</pre>
 large = R
if(index != large)
 swap(arr[large] ,arr[index])
 maxheapify(arr,large,size)
```

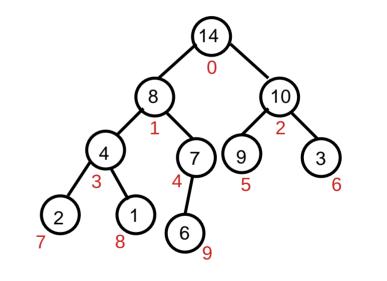
```
index = 8 L = 17 R = 18
```





SIZE = 10

```
L = 2*index +1
R = 2*index+2
if(L < size AND arr[index] < arr[L])</pre>
 large = L
else
 large = index
if(R < size AND arr[large] < arr[R])</pre>
 large = R
if(index != large)
 swap(arr[large] ,arr[index])
 maxheapify(arr,large,size)
```





Large

Build Maxheap